

# Water: A Complex Liquid

Marcia C. Barbosa



What is the mystery?

Why should we care?

What are the clues?

What is our hypothesis?

What are our results?

What do we predict?

Conclusions

# Our Group



What is the mystery?

M. Chaplin, Water structure and science (2010).

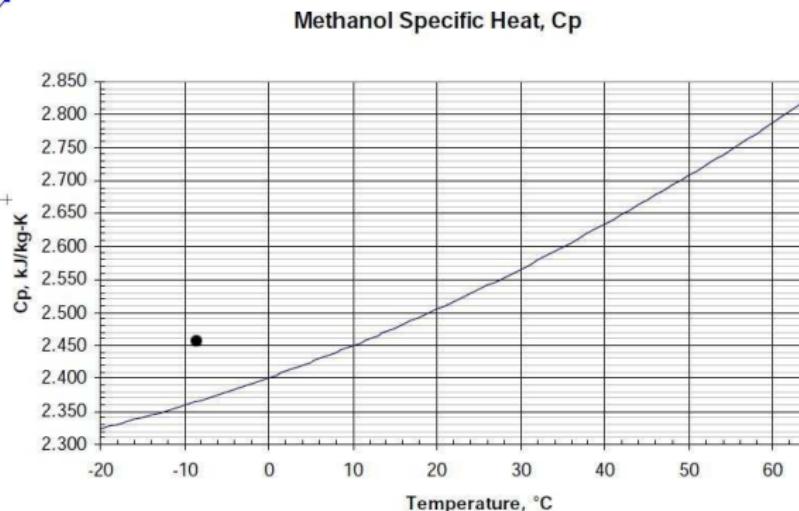
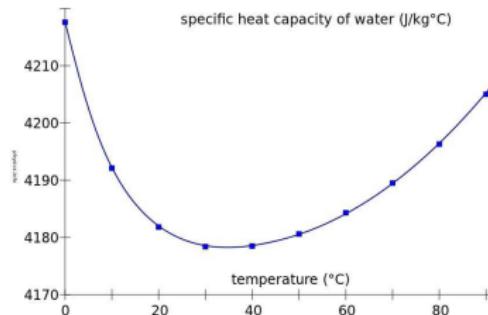
Such a simple liquid

69 anomalies

# Specific Heat

methanol: Lombari, Ferrari, Salvetti, CPL 300 (99)

$$\triangleright C_P = \left\{ \frac{dQ}{dT} \right\}_P$$

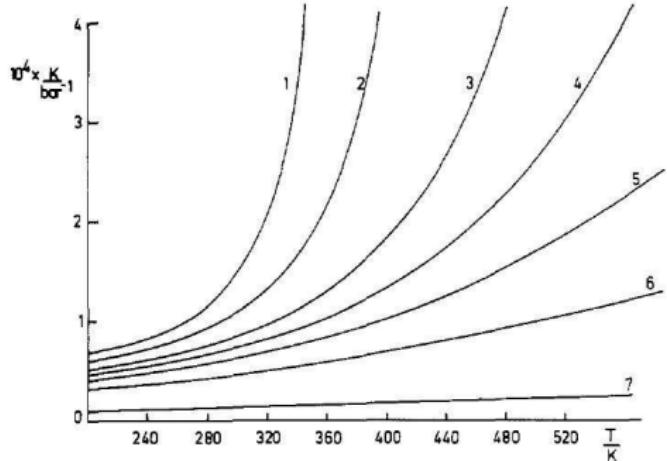
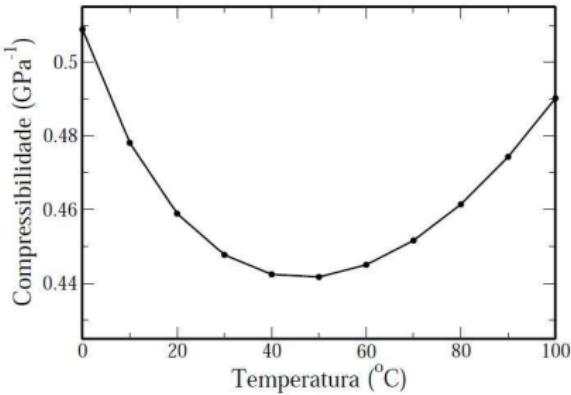


# Compressibility

water: Speedy, Angell, JCP 65, 351 (76)

toluene: Minassian, Bouzar, Alba, JPC 92, 487 (88)

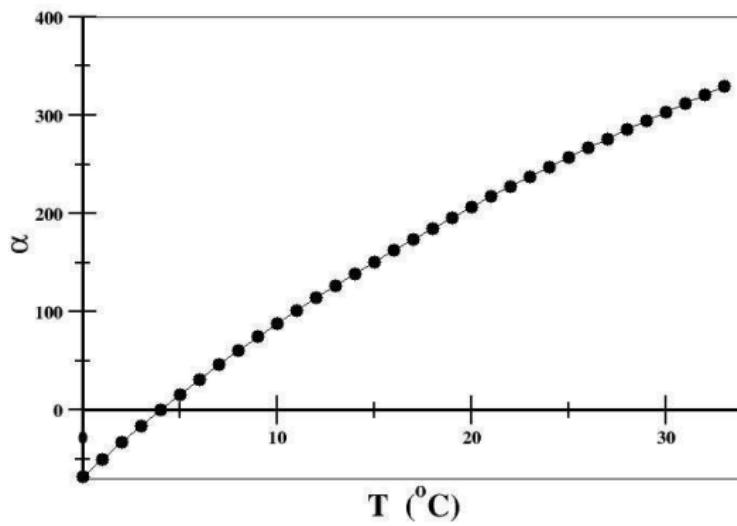
$$\blacktriangleright K_T = -\frac{1}{V} \left\{ \frac{\partial V}{\partial P} \right\}_T$$



# Thermal Expansion

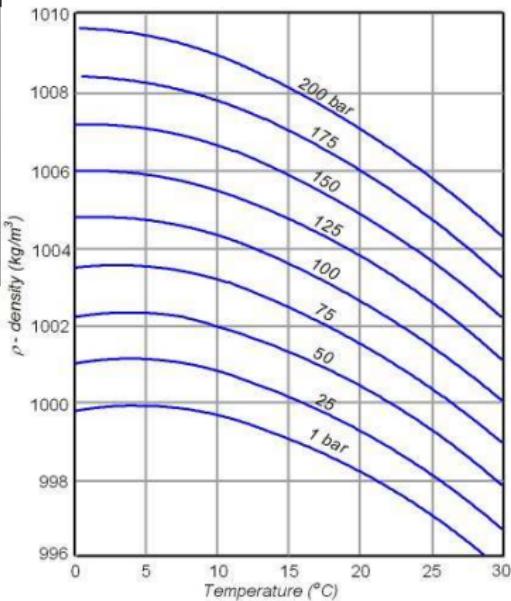
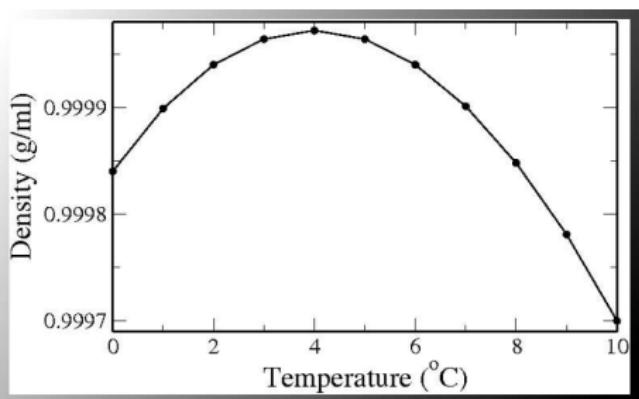
Kell, J. Chem. Eng. Data 20, 97 (75)

►  $\alpha_P = \frac{1}{V} \left\{ \frac{\partial V}{\partial T} \right\}_P$



# Density

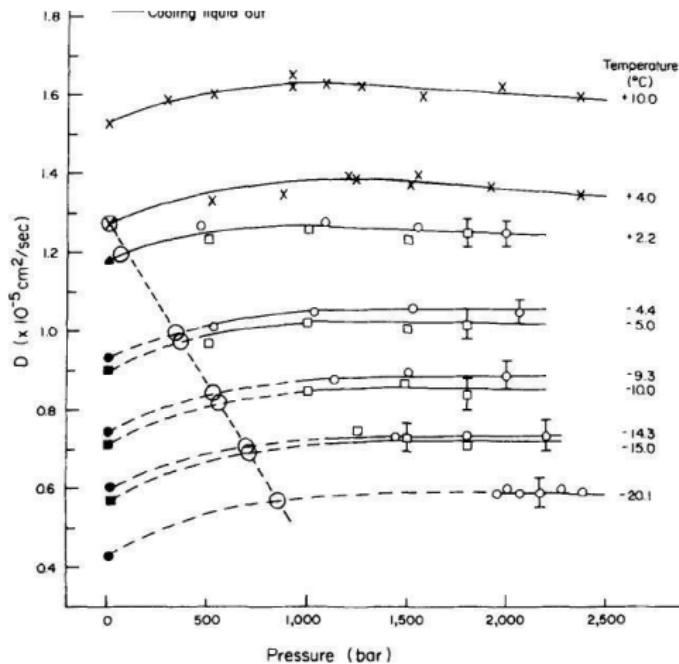
Kell, J. Chem. Eng. Data 12, 66 (67)



# Diffusion

Angell, Finch, Bach 65, 3063 (76)

►  $\langle r(t)r(0) \rangle = 6Dt$



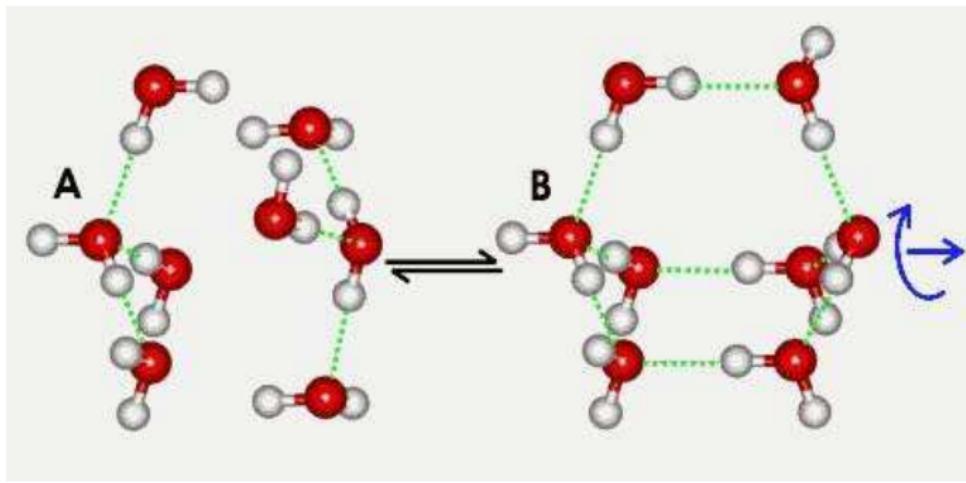
# Why should we care?

- ▶ Specific Heat, Thermal Conductivity, High Vaporization Heat – Life
- ▶ Low Compressibility – More land
- ▶ Density – Rivers freeze on top
- ▶ Diffusion anomaly – Transport of nutrients

# What are the clues?

- ▶ Bonds
  
- ▶ Polarizability
  
- ▶ Aggregates

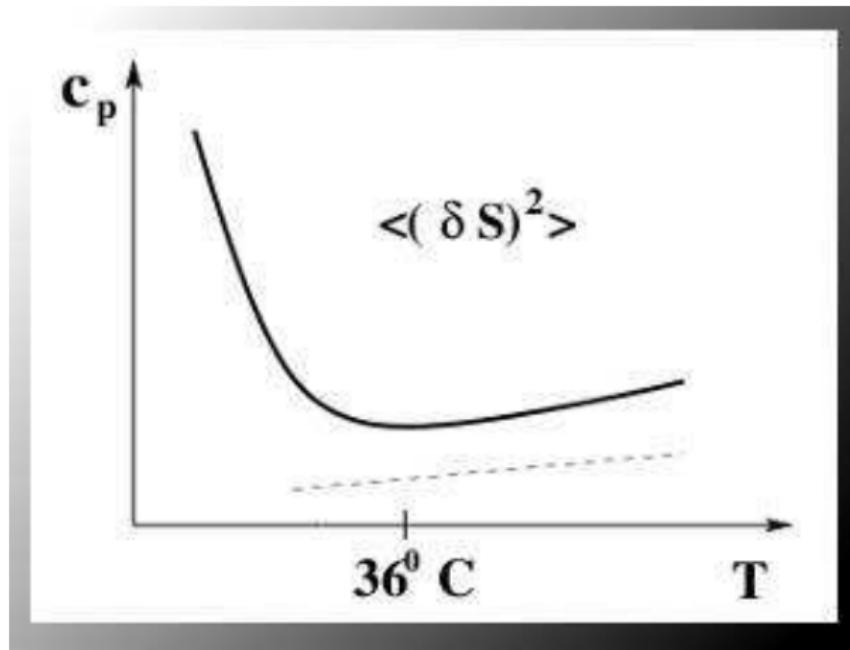
## Two Scales



# Specific Heat = Fluctuation in the Entropy

Stanley, Pramana 53, 53 (99)

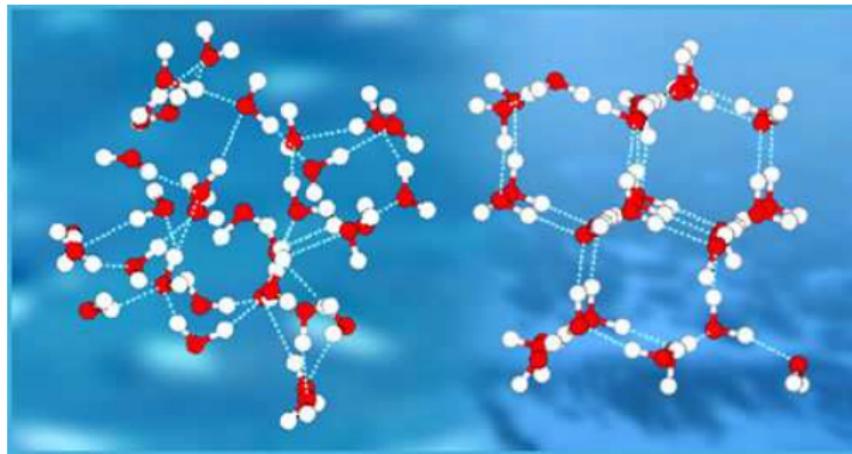
- ▶  $C_p \propto \langle (S - \langle S \rangle)^2 \rangle$



# Specific Heat = Fluctuation in the Entropy

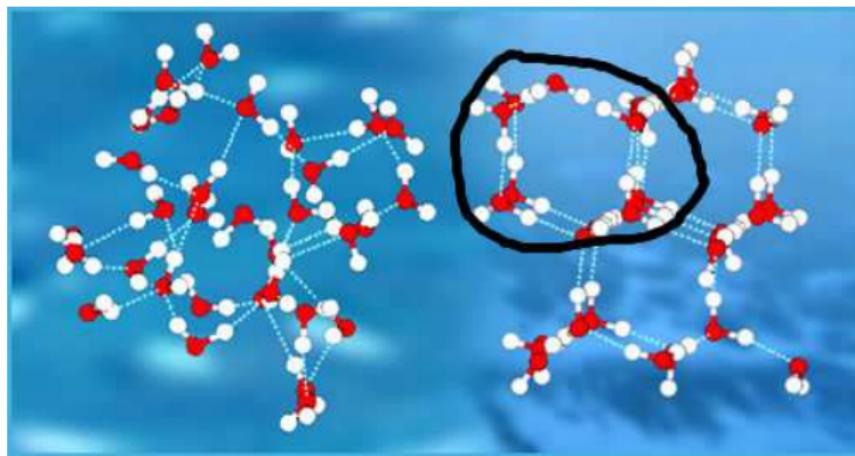
Stanley, Pramana 53, 53 (99)

- ▶  $C_p \propto \langle (S - \langle S \rangle)^2 \rangle$



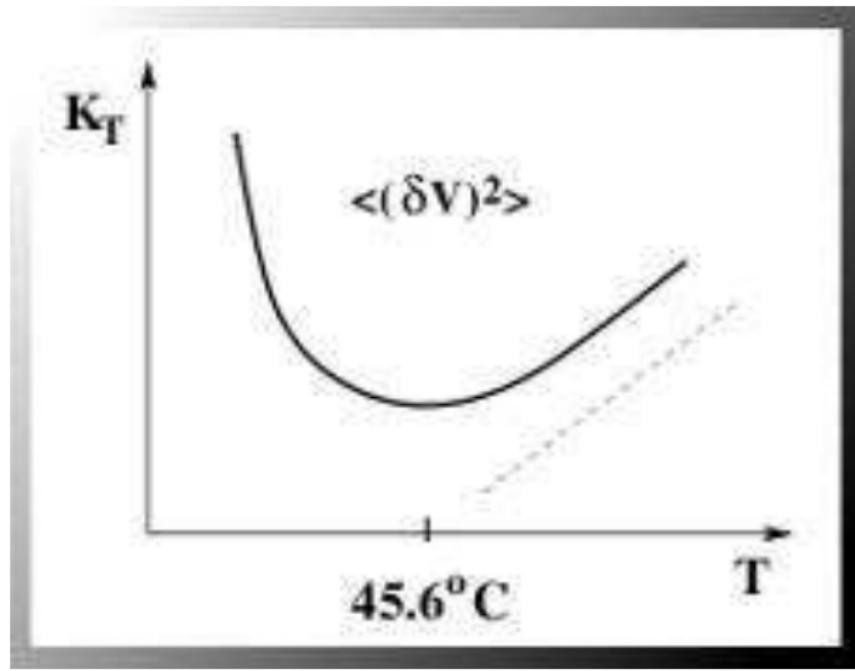
# Specific Heat = Fluctuation in the Entropy

- ▶  $C_p \propto \langle (S - \langle S \rangle)^2 \rangle$



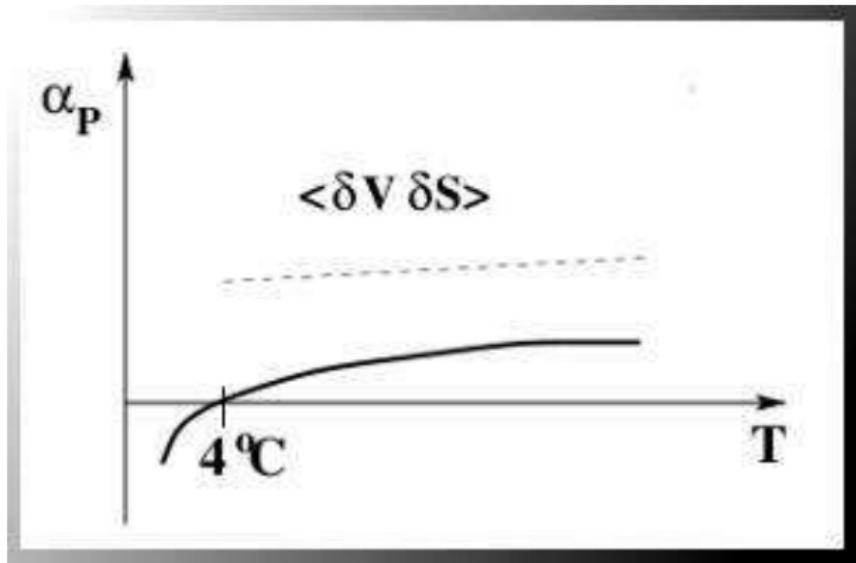
## Compressibility = Fluctuation in the Volume

- ▶  $K_T \propto \langle (V - \langle V \rangle)^2 \rangle$



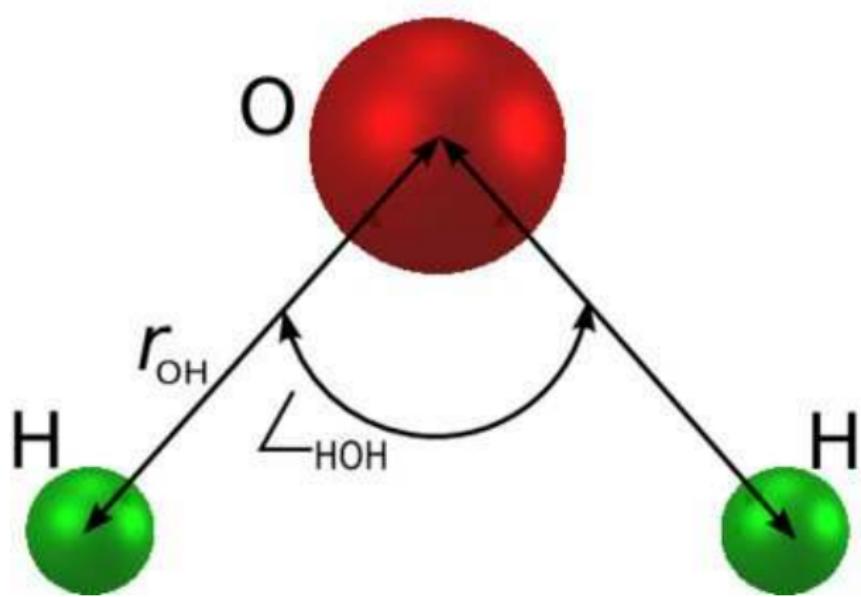
# Thermal Expansion = Fluctuation in the Volume and Entropy

- ▶  $\alpha \propto \langle (S - \langle S \rangle)(V - \langle V \rangle) \rangle$



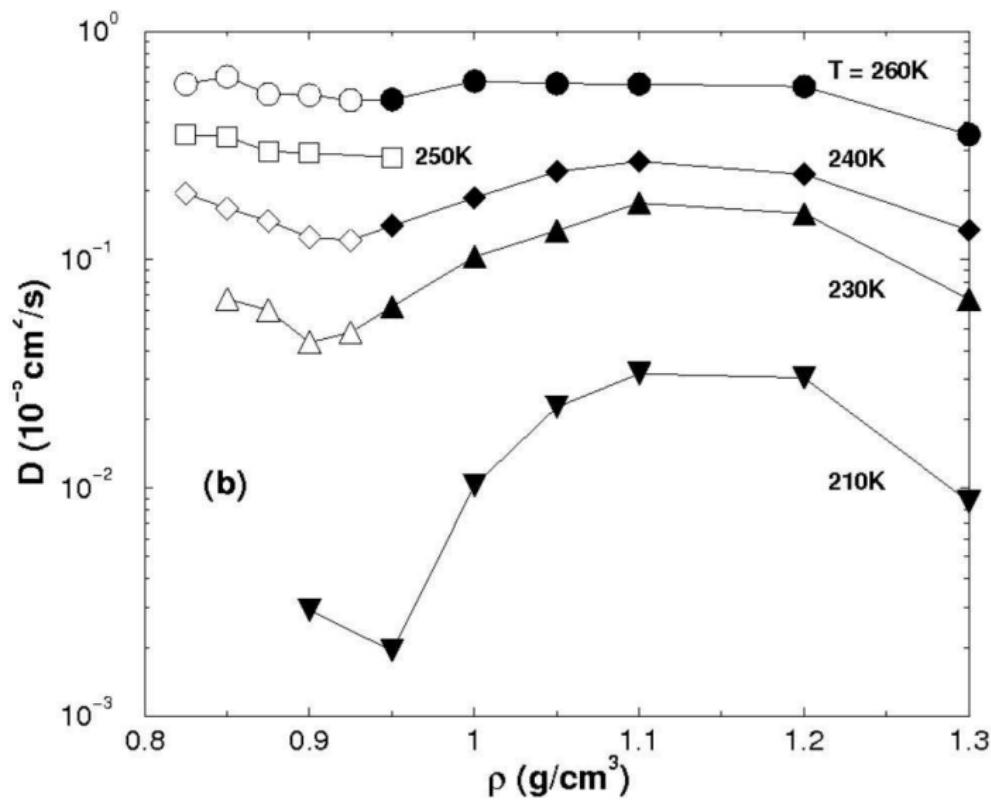
# Diffusion - SPC/E

Berendsen, Grigera, Straatsma, JCP 91, 6269 (87)



# Diffusion - SPC/E

Netz, Starr, Stanley, Barbosa JCP 115, 344 (01)

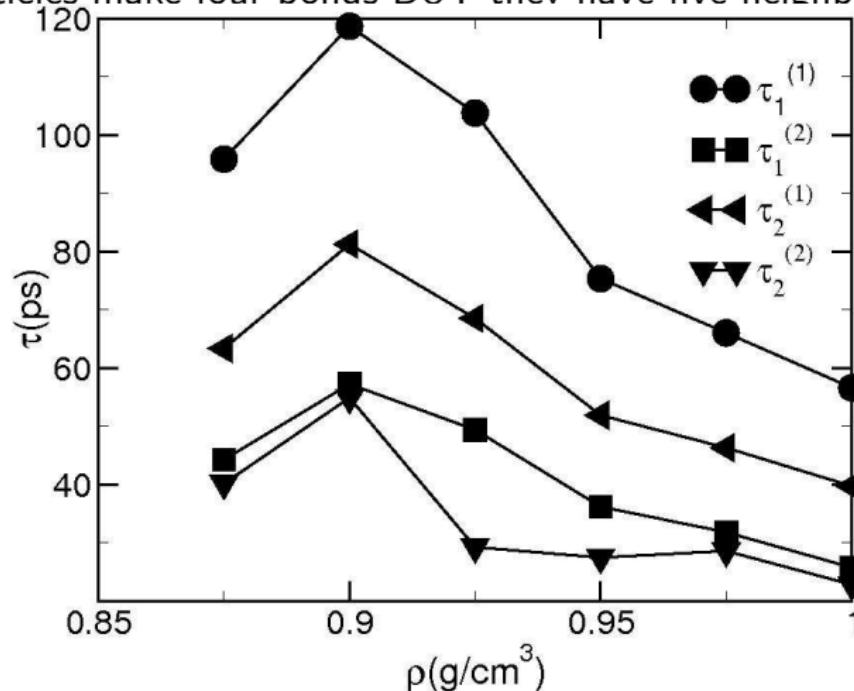


# Rotation Diffusion - SPC/E

Netz, Starr, Barbosa, Stanley, JML 101, 159-168 (02)

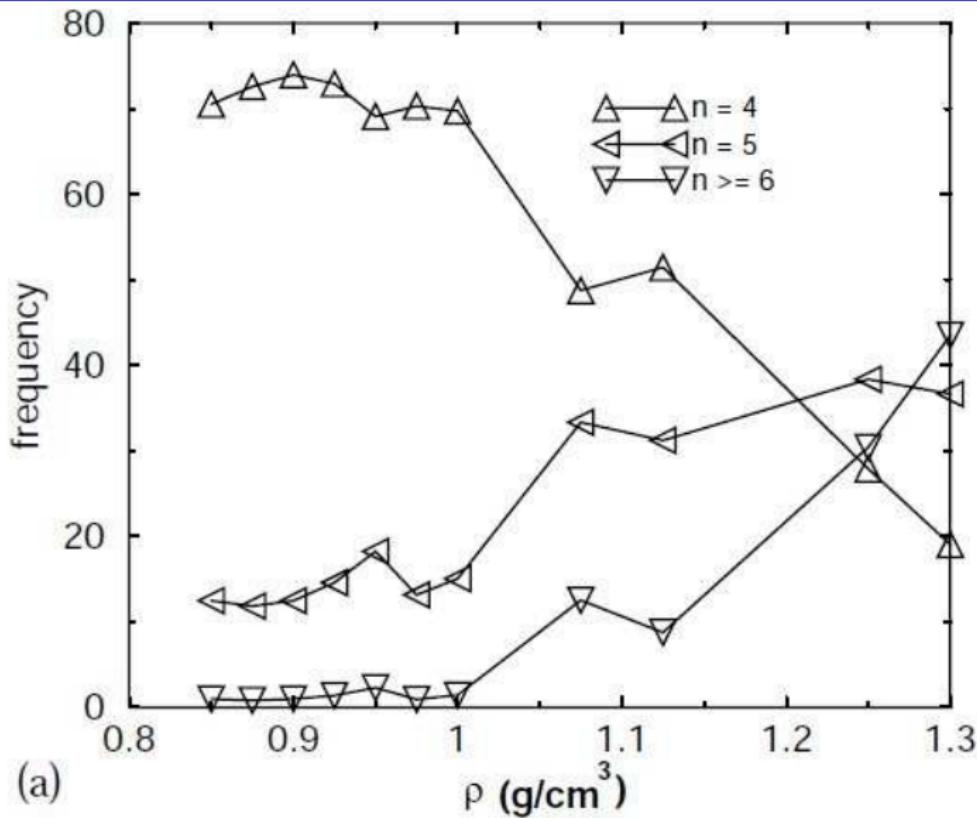
Mazza, Giovanbaptista, Stanley, Starr, PRE 76, 31203 (07)

- Particles make four bonds BUT they have five neighbors!!!



# Frequency - SPC/E

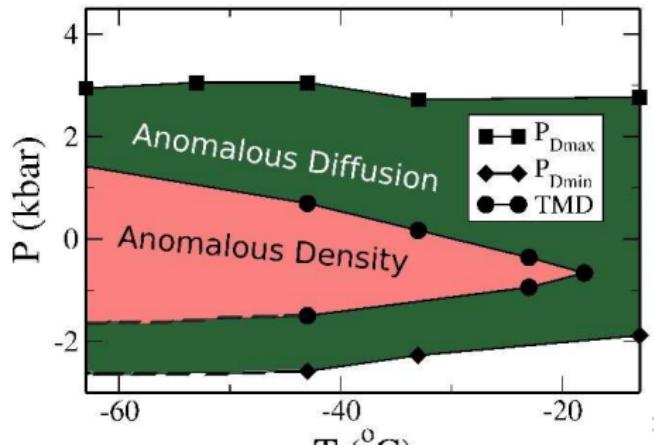
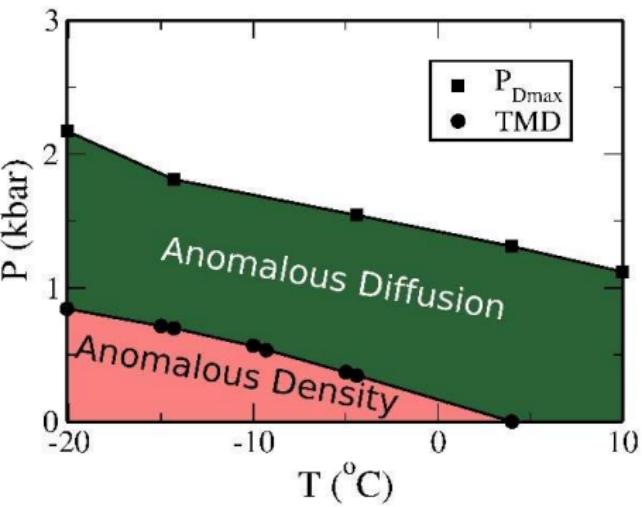
Netz, Starr, MCB and Stanley, Physica A 314, 470 (2002)



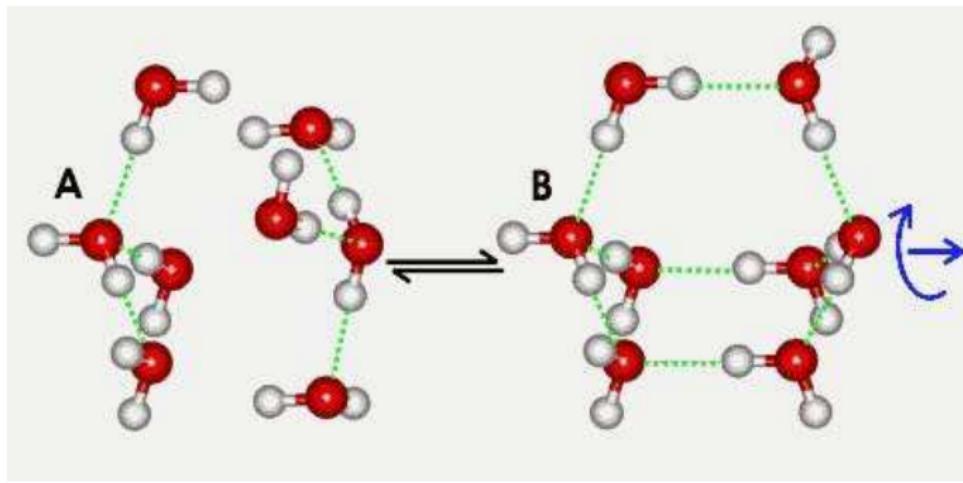
# Water SPC/E

Angell, Finch, Bach 65, 3063 (76)

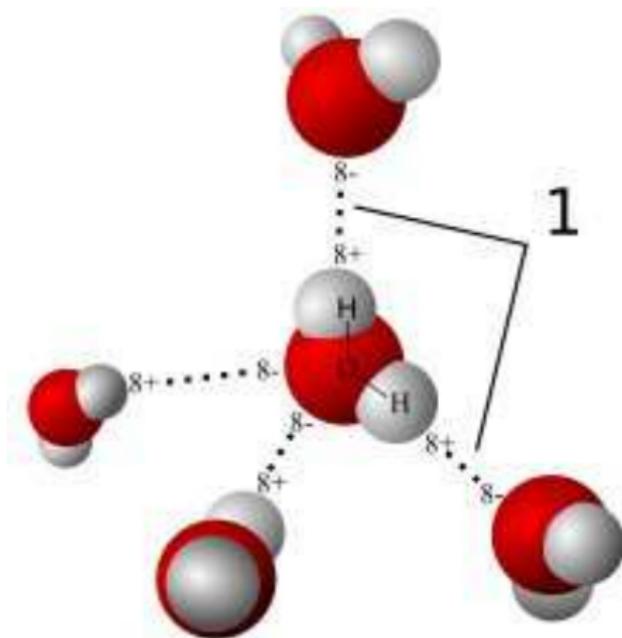
Netz, Starr, Stanley, Barbosa JCP 115, 344 (01)



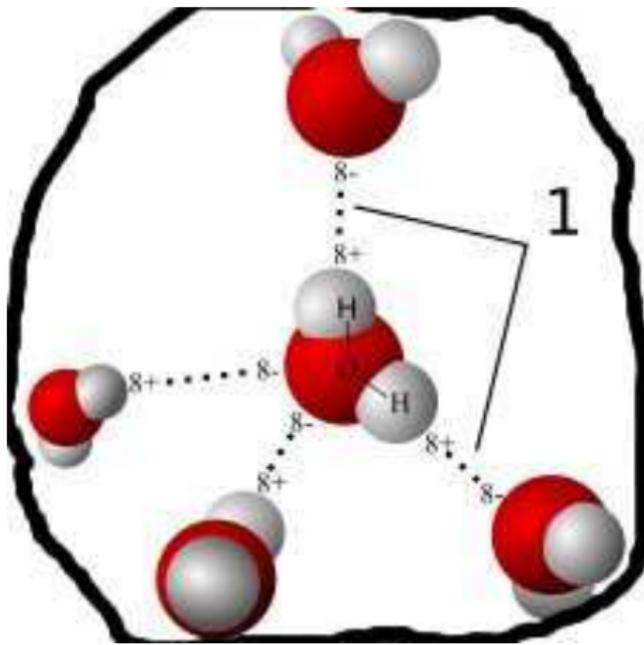
# Two Length Scales Potential



# Structure

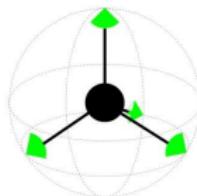
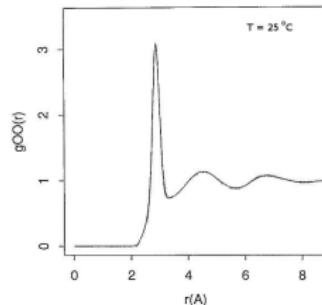


# Structure



# Effective Potential

- Radial Distribution Function of WATER:



$$\sigma_o = 2,86 \times 10^{-10} \text{ m}$$
$$\epsilon = 0,006 \frac{\text{kcal}}{\text{mol}}$$

- Ornstein-Zernike Equation:

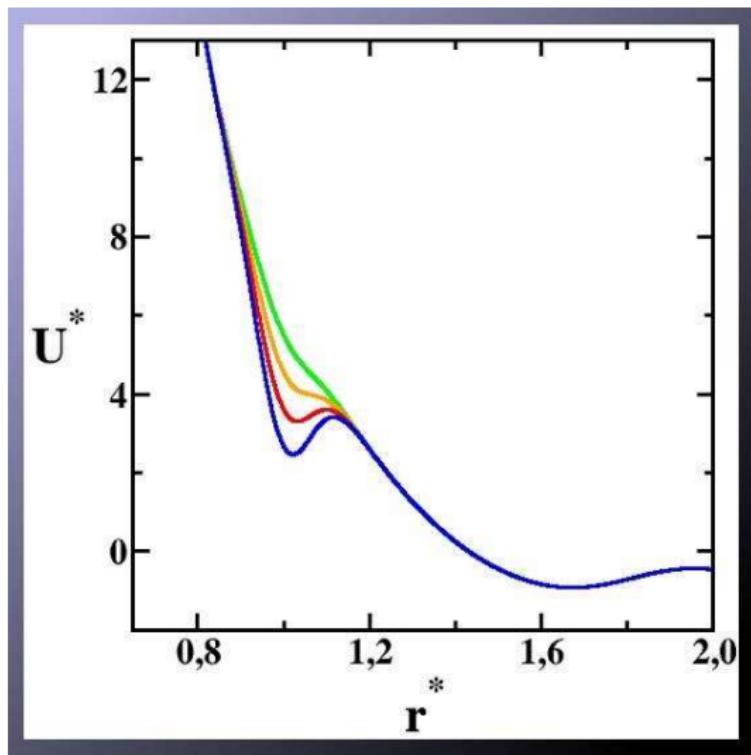
$$h(r) = g(r) - 1 = c(r) + \rho \int c(r - r') h(r') dr'$$

- Hypernetted Chain Approximation (HNC):

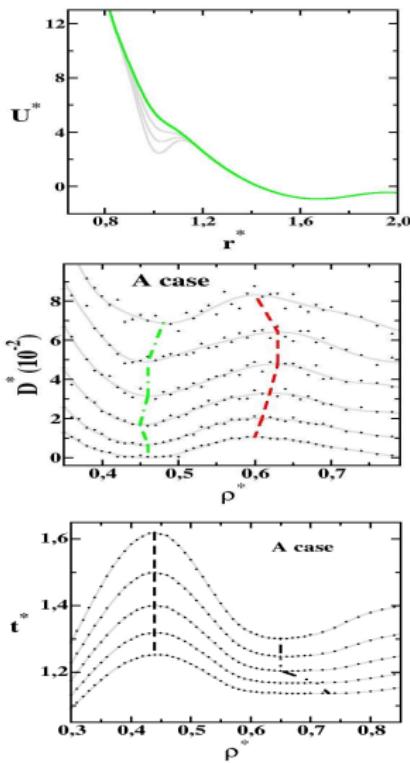
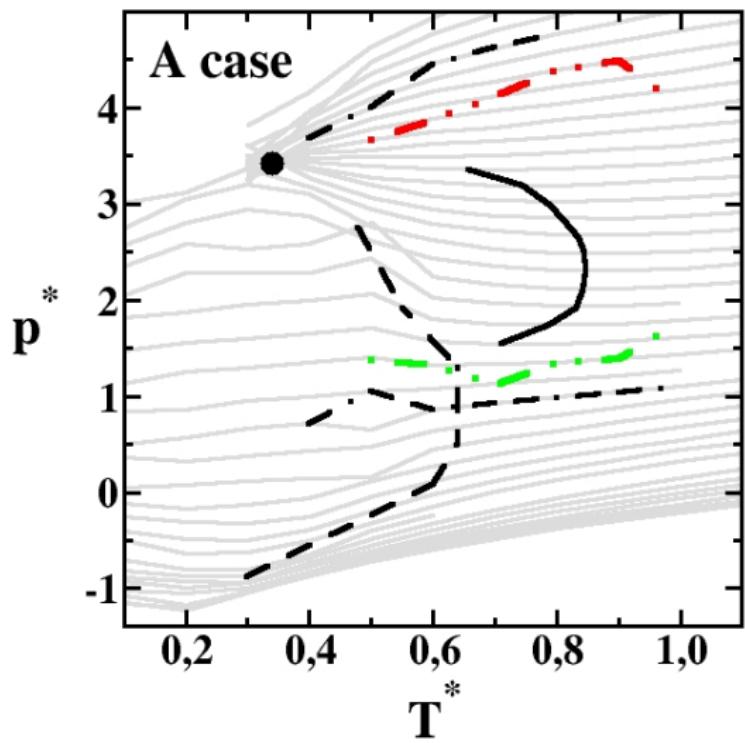
$$U(r) = k_B T \{ g(r) - 1 - \ln[g(r)] - c(r) \}$$

# Effective Potential

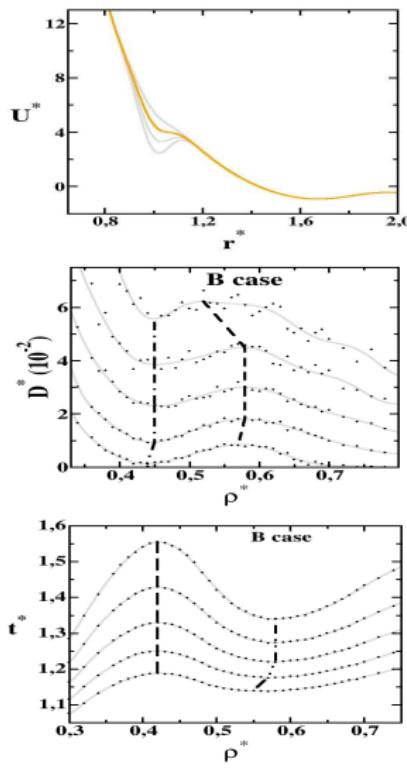
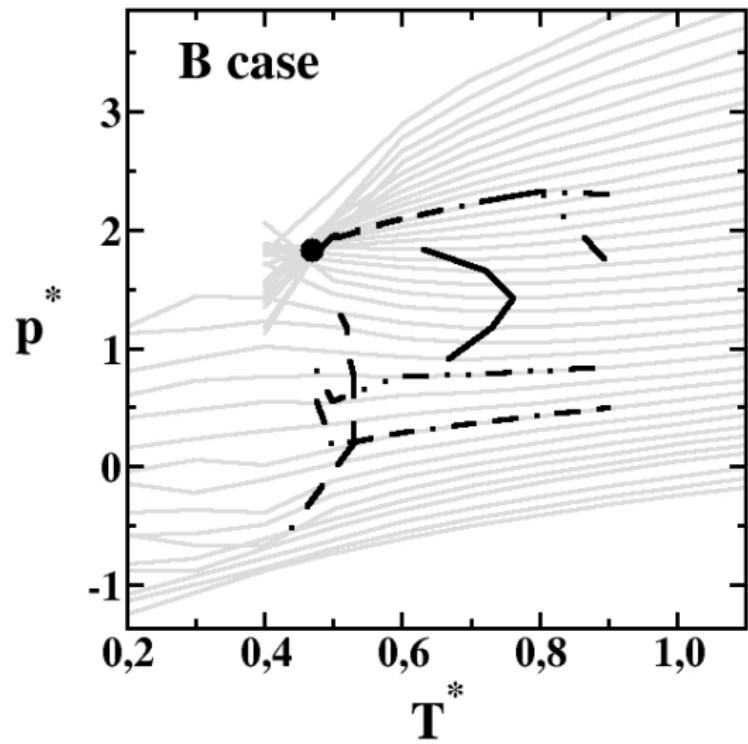
Barraz, Salcedo, Barbosa, JCP 131, 094504 (09)



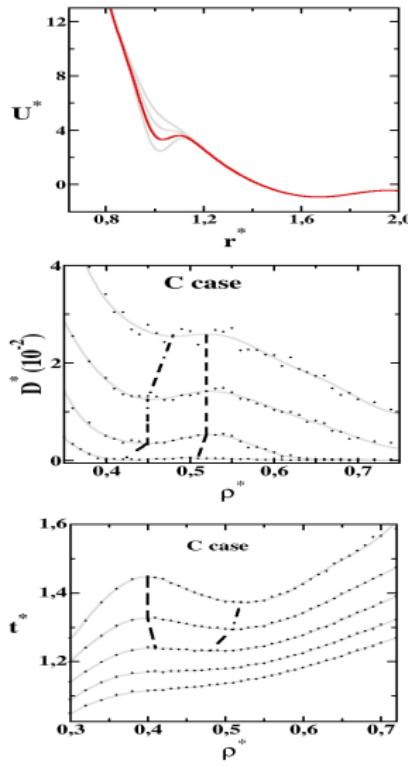
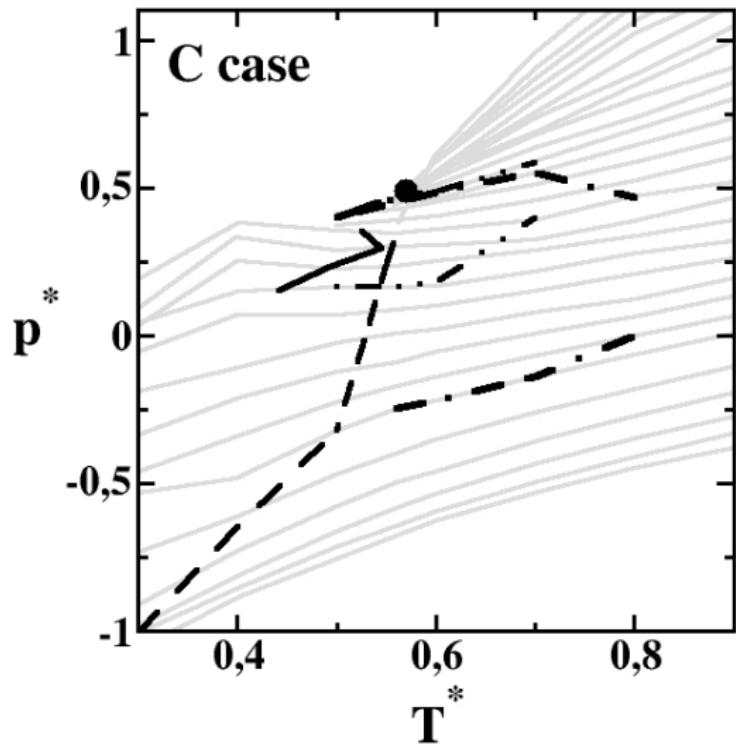
# Phase Diagram



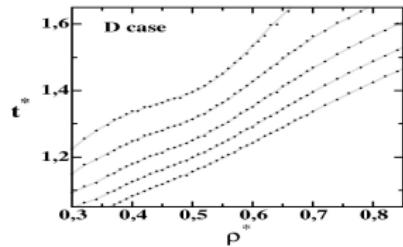
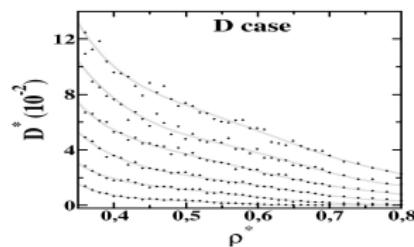
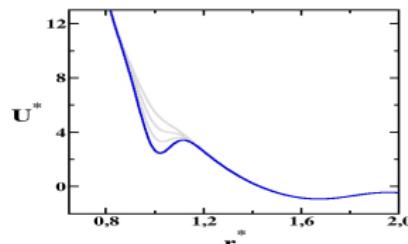
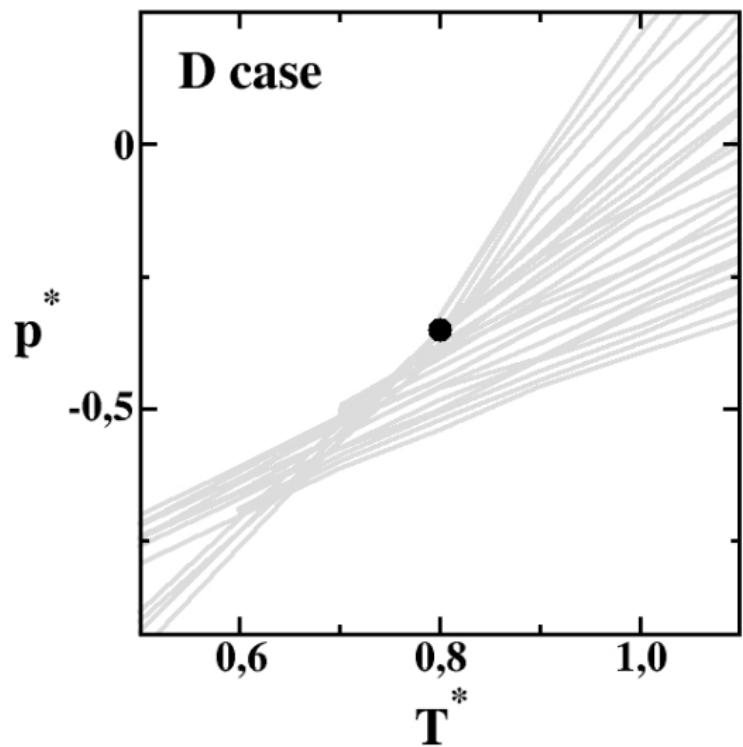
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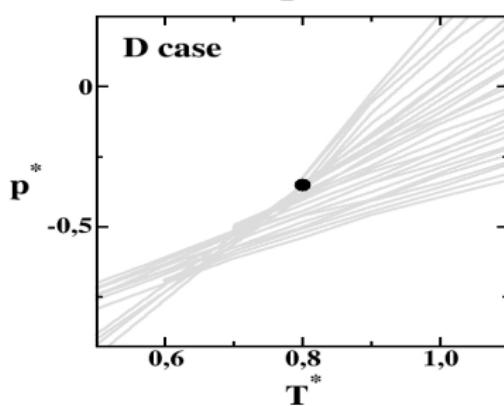
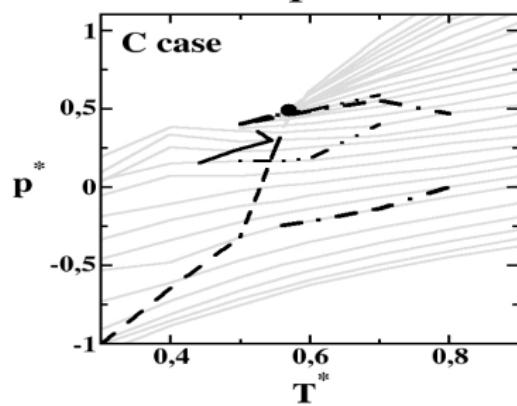
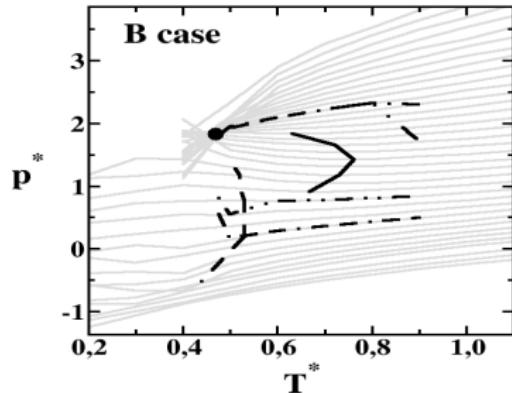
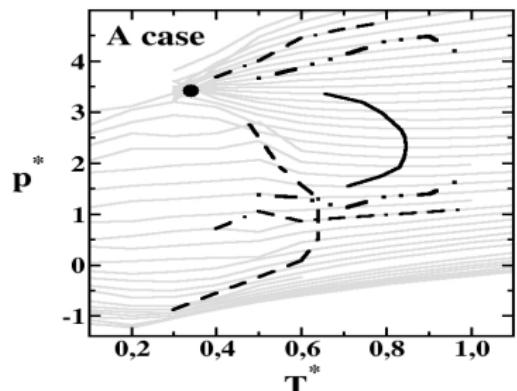
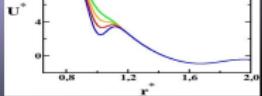
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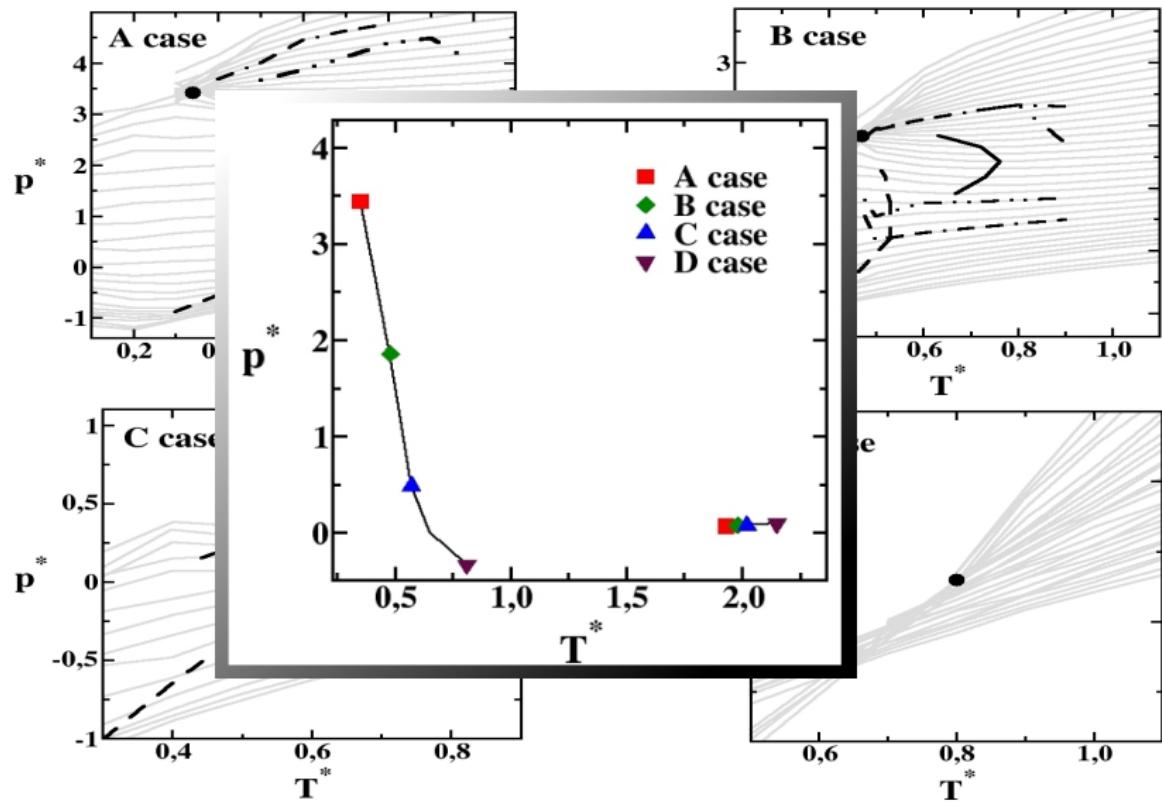
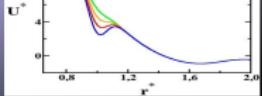
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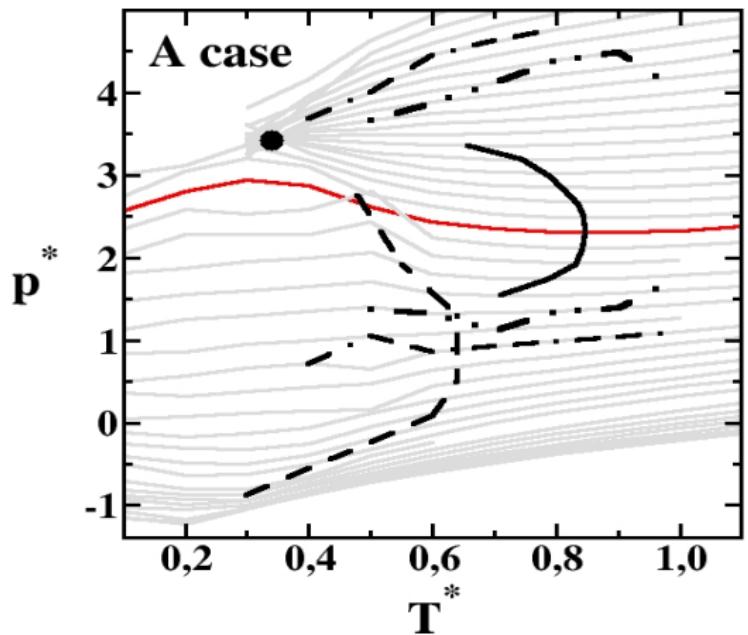
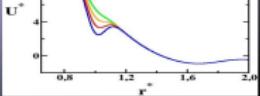
# Critical Points



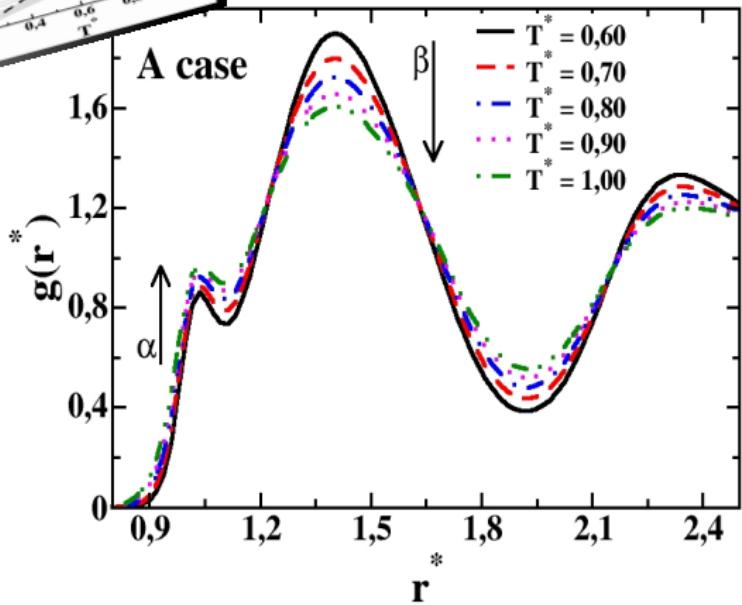
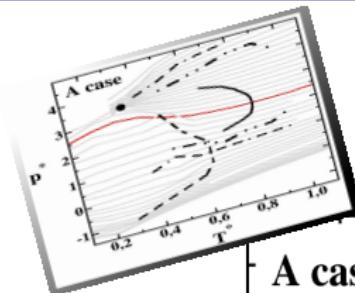
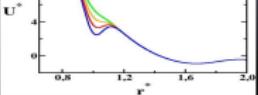
# Critical Points



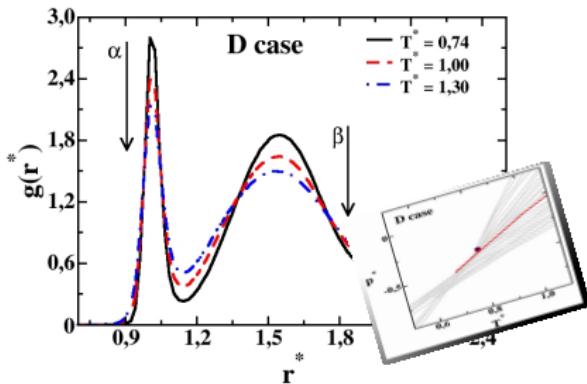
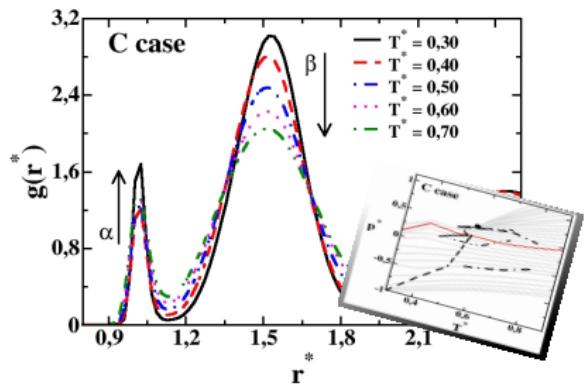
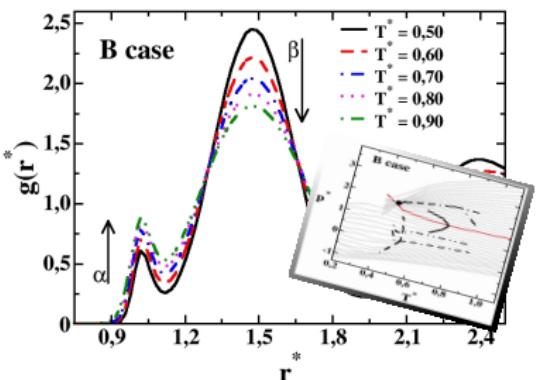
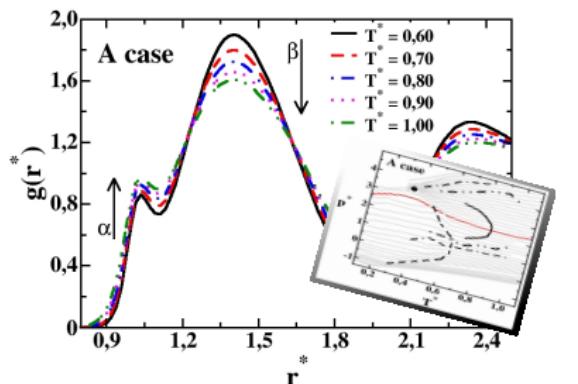
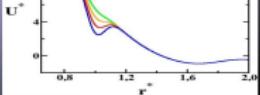
# Radial Distribution Function



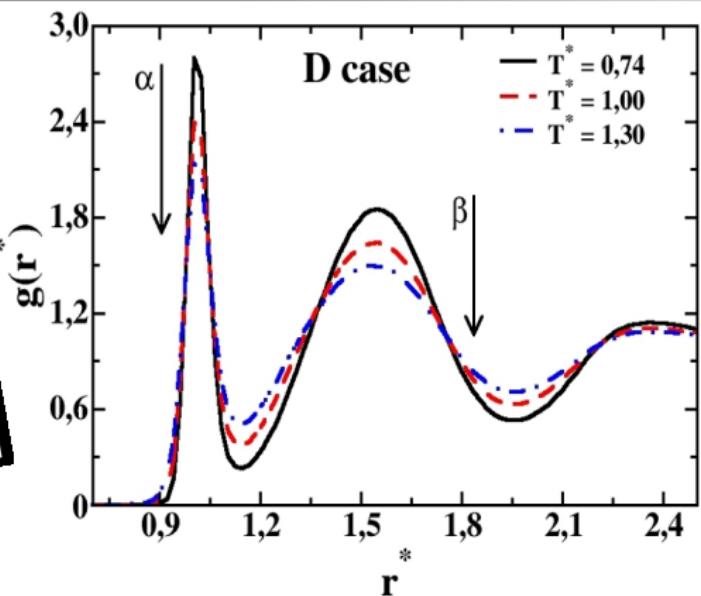
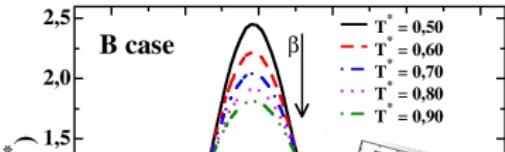
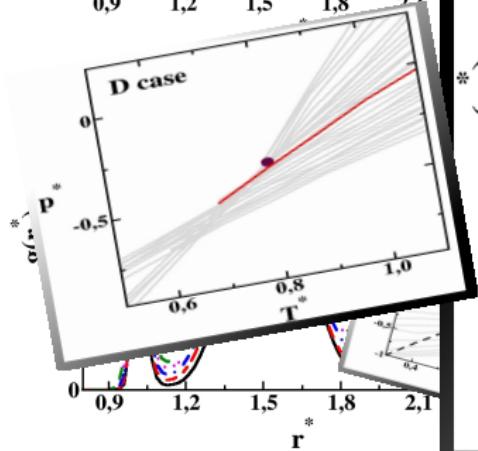
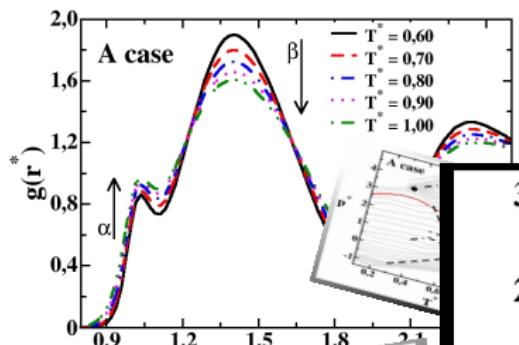
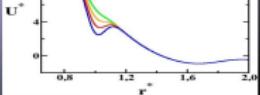
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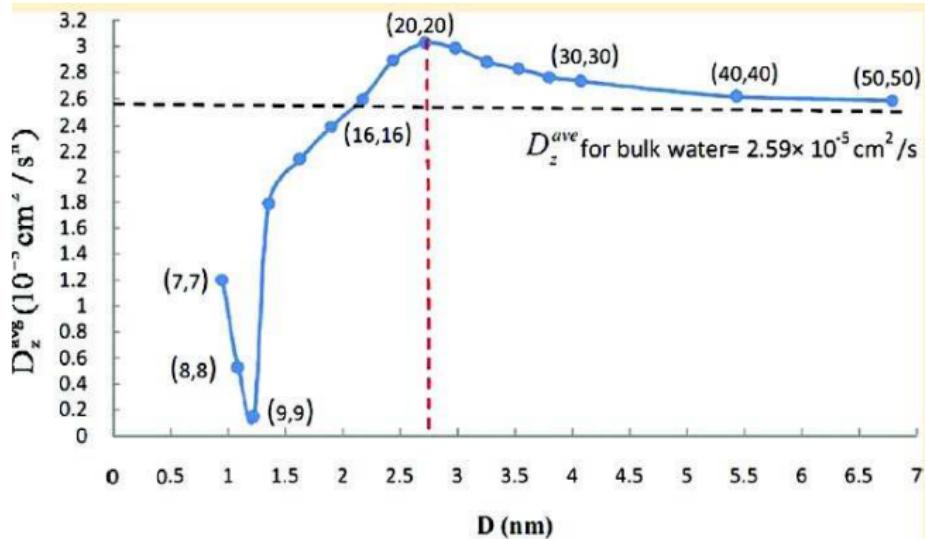


# Radial Distribution Function

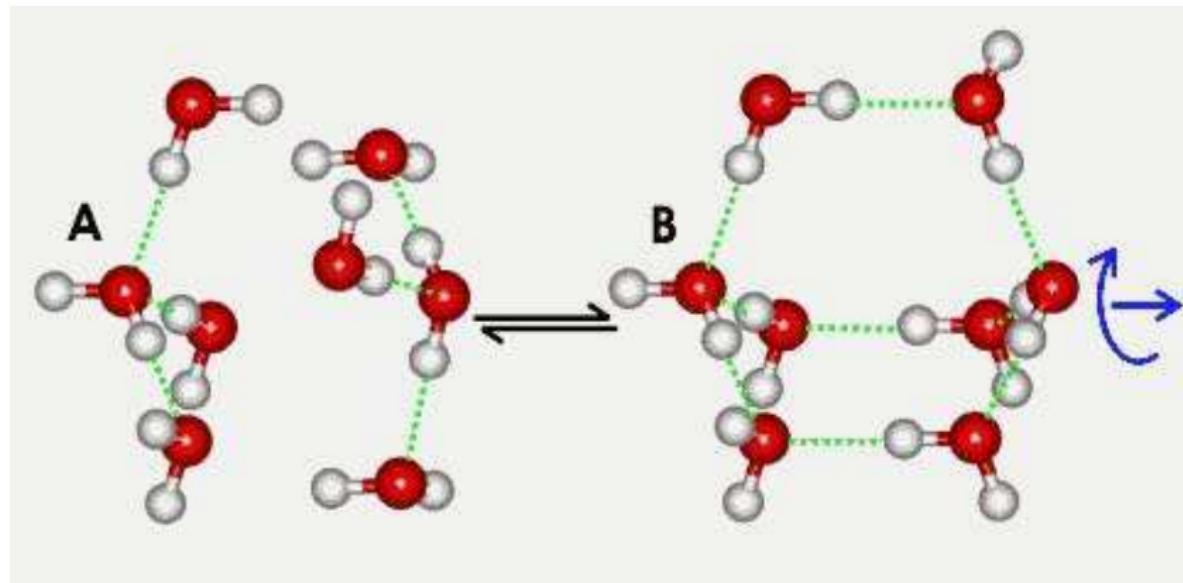


# Rapid Flow in Nanotubes - Simulations

A.B. Farinami, JPCB 115, 12145 (2012)

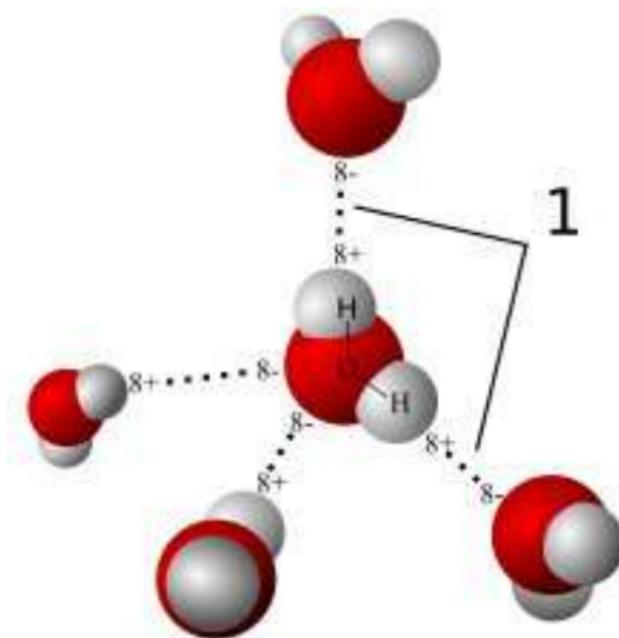


# Water Channels- What is our Model?



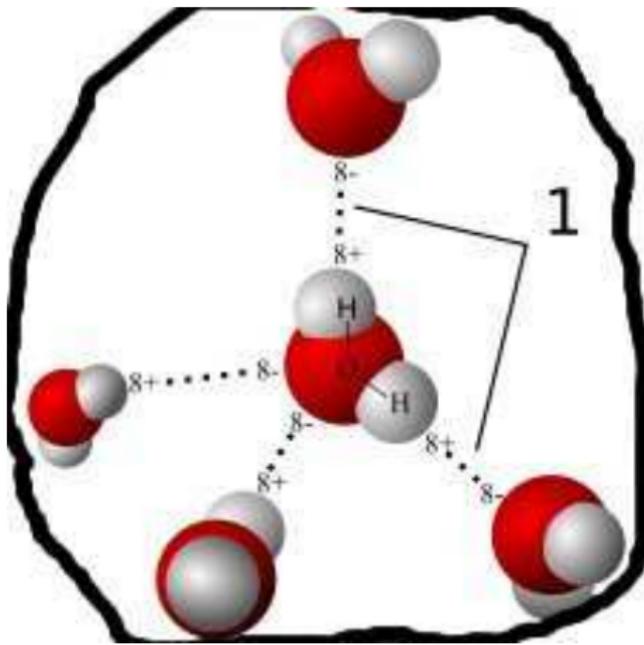
# Structure

N. M. Barraz, E. Salcedo and MCB, JCP 135 104507 (2011)



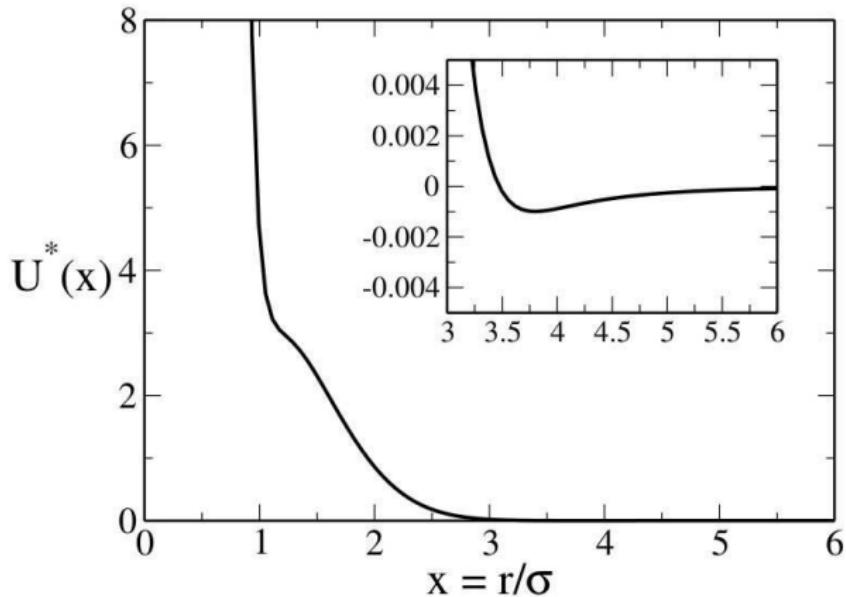
# Structure

N. M. Barraz, E. Salcedo and MCB, JCP 135 104507 (2011)



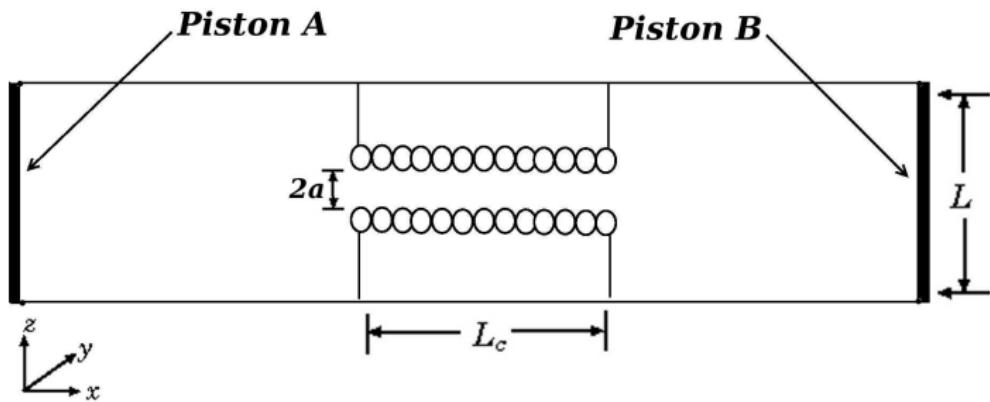
# Effective Potential

A. B. de Oliveira, P. E. Netz, T. Colla and MCB, JCP 124 84505 (2006)



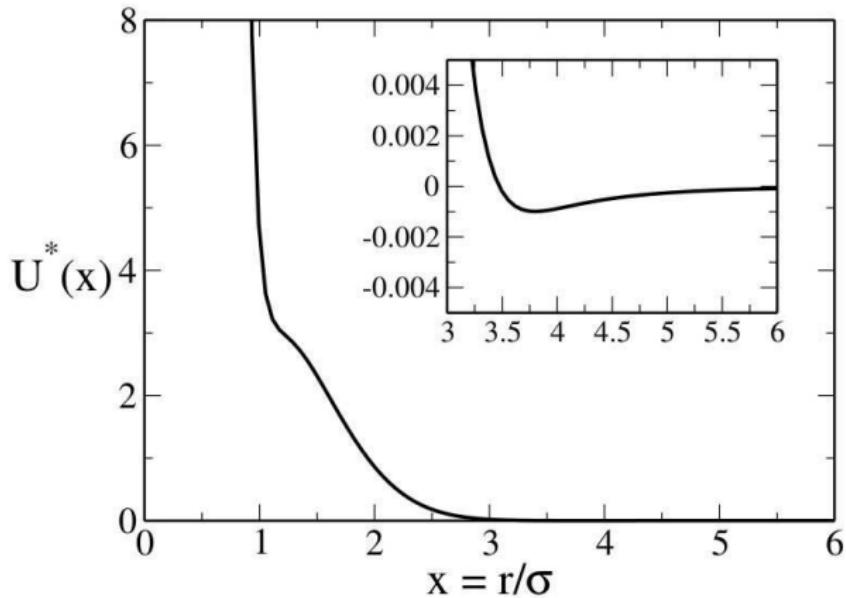
# Model for Confining

J. R. Bordin, A. Diehl and MCB, PRE (2013)



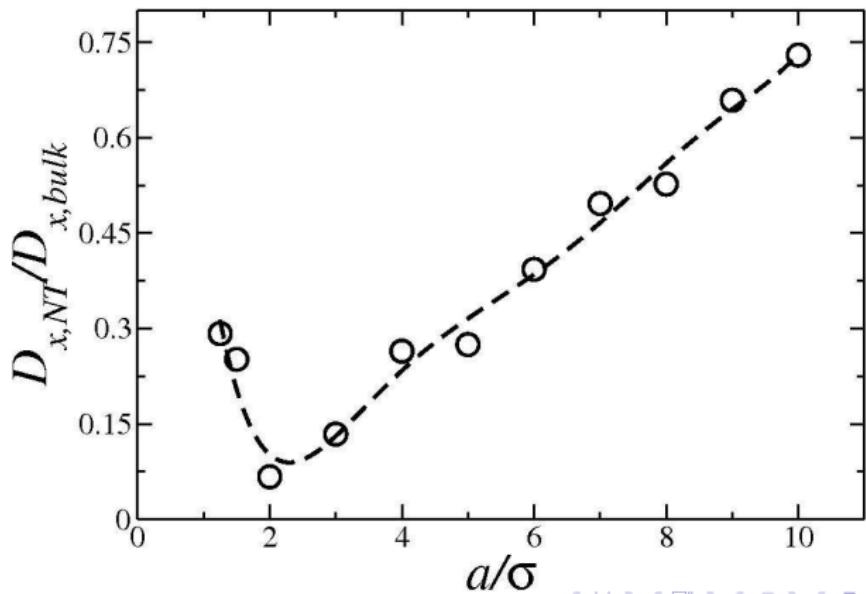
# Effective Potential

J. R. Bordin, A. Diehl and MCB, PRE (2013)



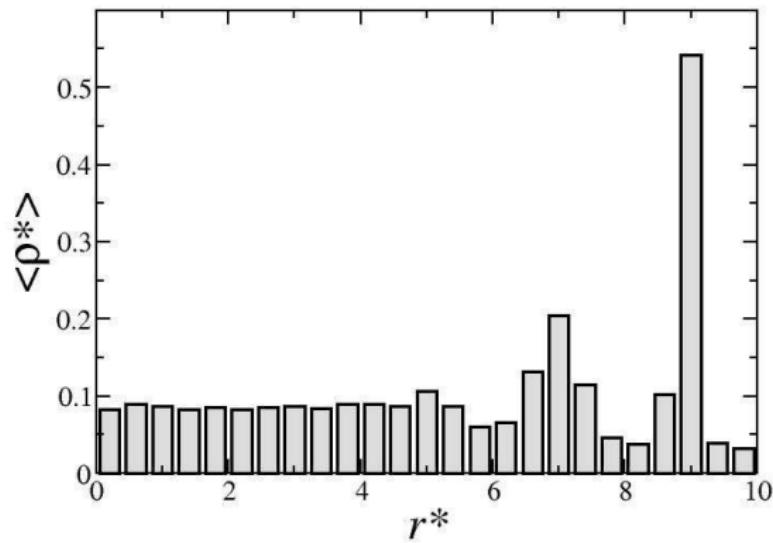
# Diffusion

J. R. Bordin, A. Diehl and MCB, PRE (2013)



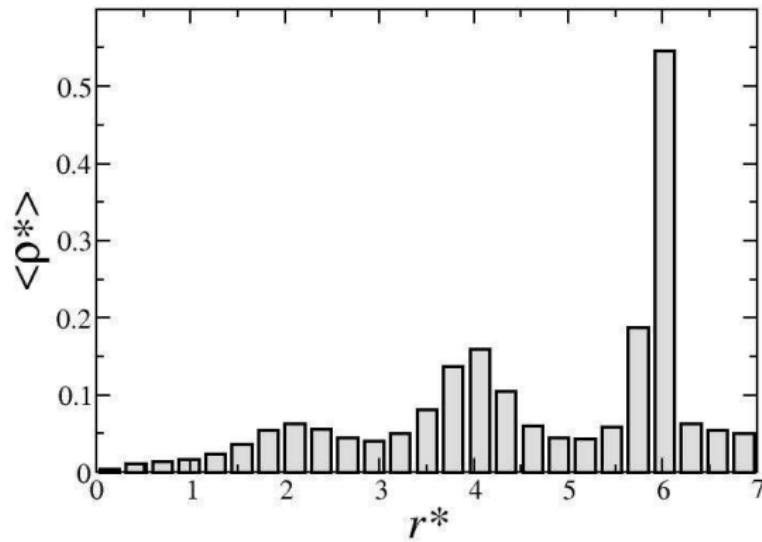
# Density vs. $r$ - $a=10$

J. R. Bordin, A. Diehl and MCB, PRE (2013)



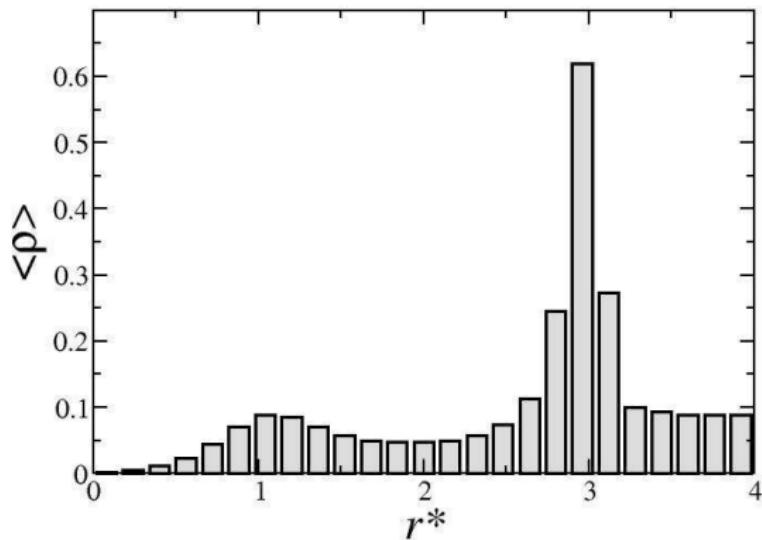
# Density vs. $r$ - $a=7$

J. R. Bordin, A. Diehl and MCB, PRE (2013)



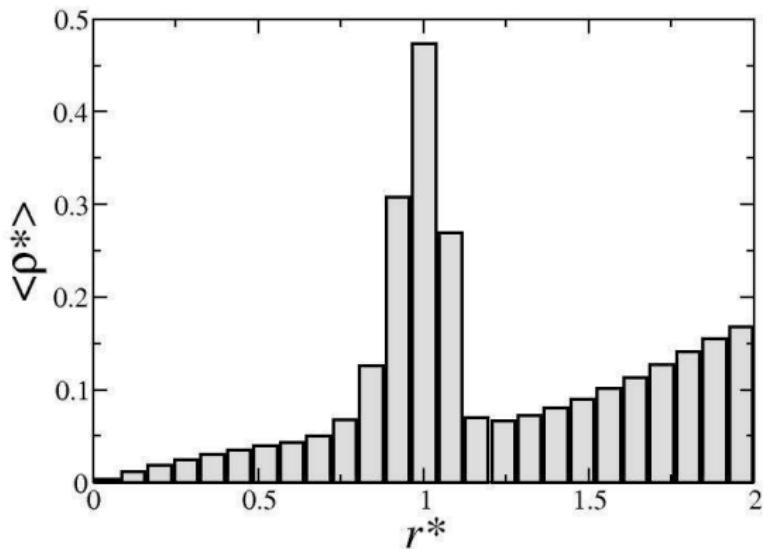
# Density vs. $r - a=4$

J. R. Bordin, A. Diehl and MCB, PRE (2013)



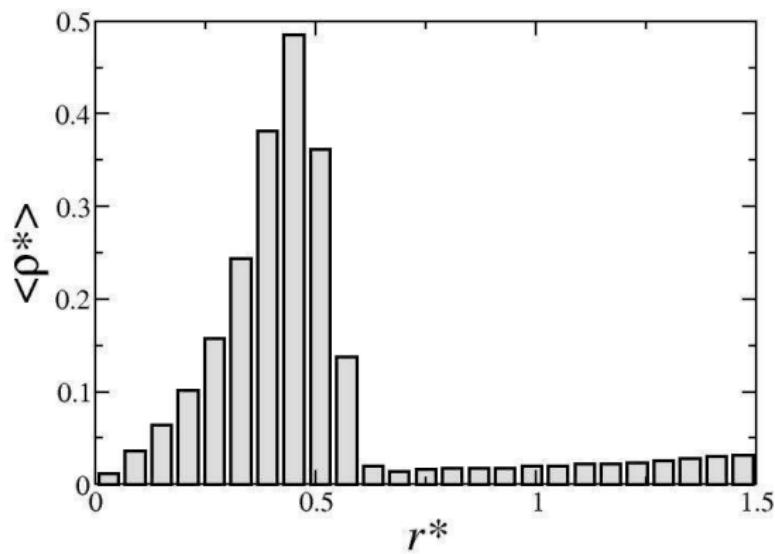
# Density vs. $r$ - $a=2$

J. R. Bordin, A. Diehl and MCB, PRE (2013)



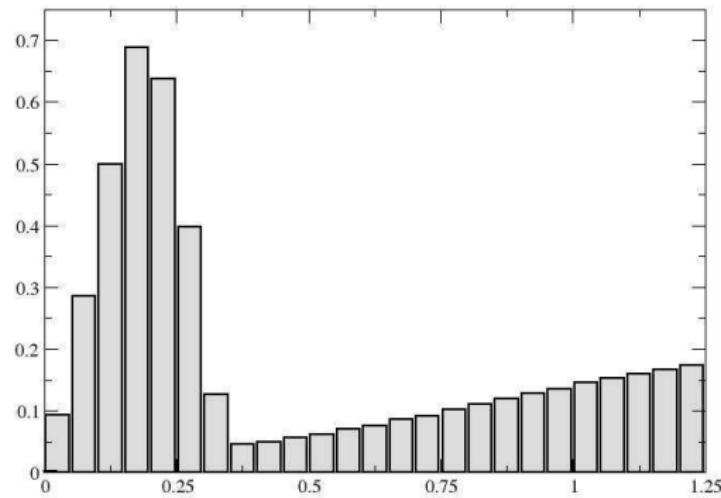
# Density vs. $r$ - $a=1.5$

J. R. Bordin, A. Diehl and MCB, PRE (2013)



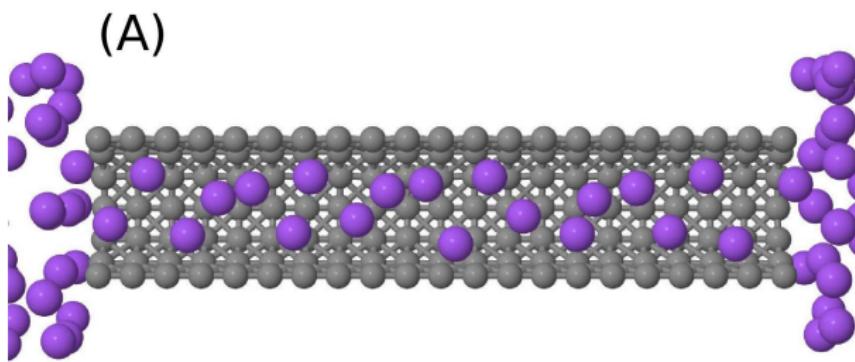
# Density vs. $r$ - $a=1.25$

J. R. Bordin, A. Diehl and MCB, PRE (2013)



# Density vs. $r$ - $a=1.25$

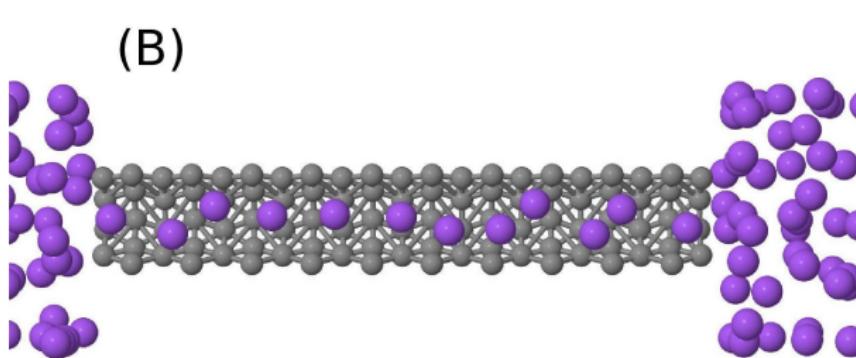
J. R. Bordin, A. Diehl and MCB, PRE (2013)



# Density vs. $r - a = 1.25$

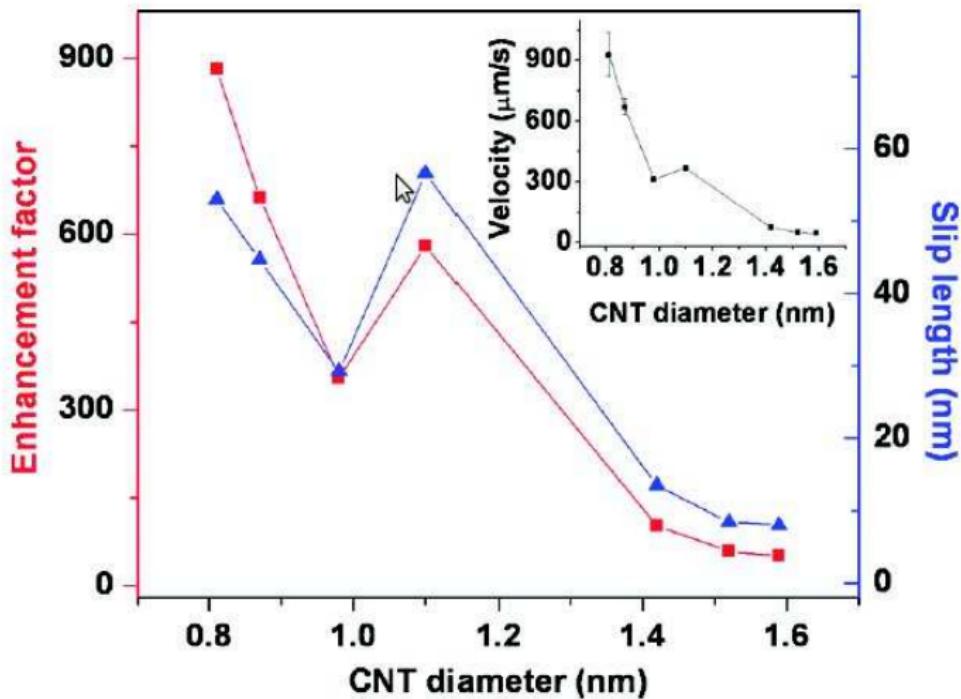
J. R. Bordin, A. Diehl and MCB, PRE (2013)

(B)



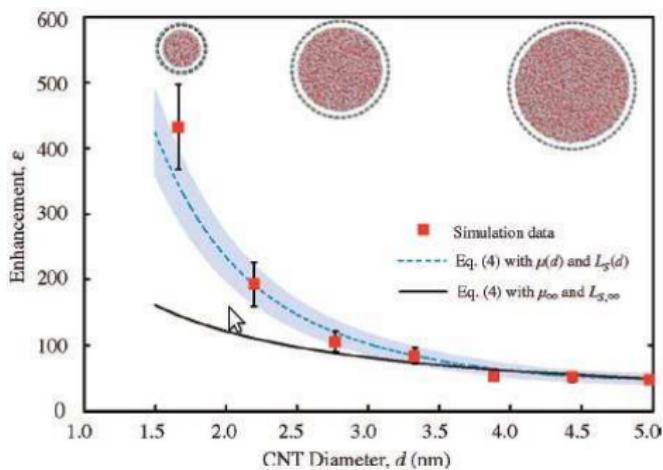
# Flux in Nanotubes

X. Qin et al, Nanoletters 11, 2173 (2011) - experimental - SPC/E



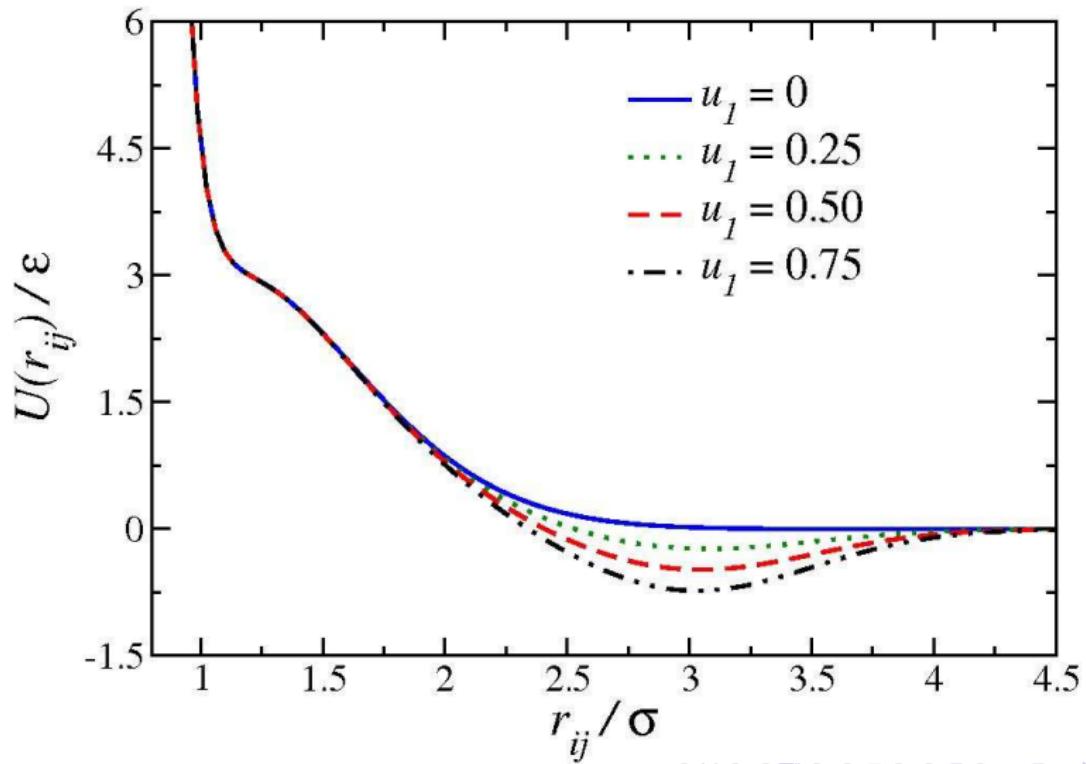
# Water Channel - Enhancement Flow

J. A. Thomas and A. J. H. McGaughey, Nanoletters 8, 2788 (2008)



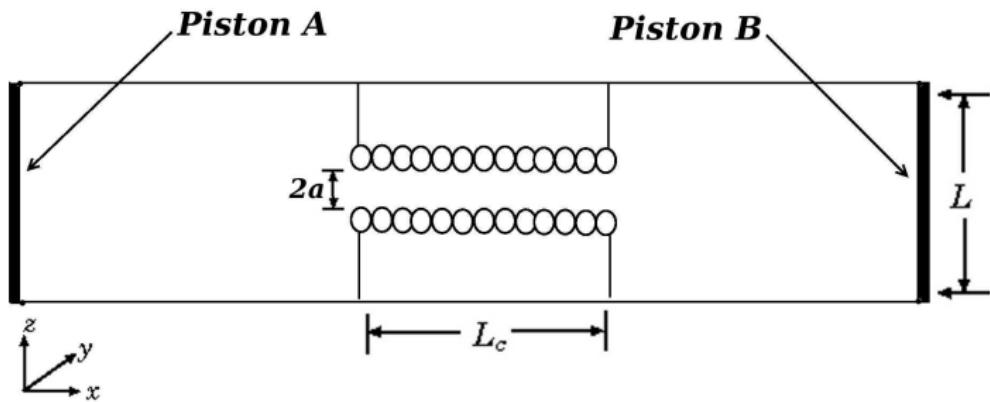
# Effective Potential

J. da Silva and MCB, JCP (2010)



# Model for Nanotubes

J. R. Bordin, A. Diehl and MCB, JPCB (2013)



# Enhancement Flow

J. R. Bordin, A. Diehl and MCB, JPCB (2013)

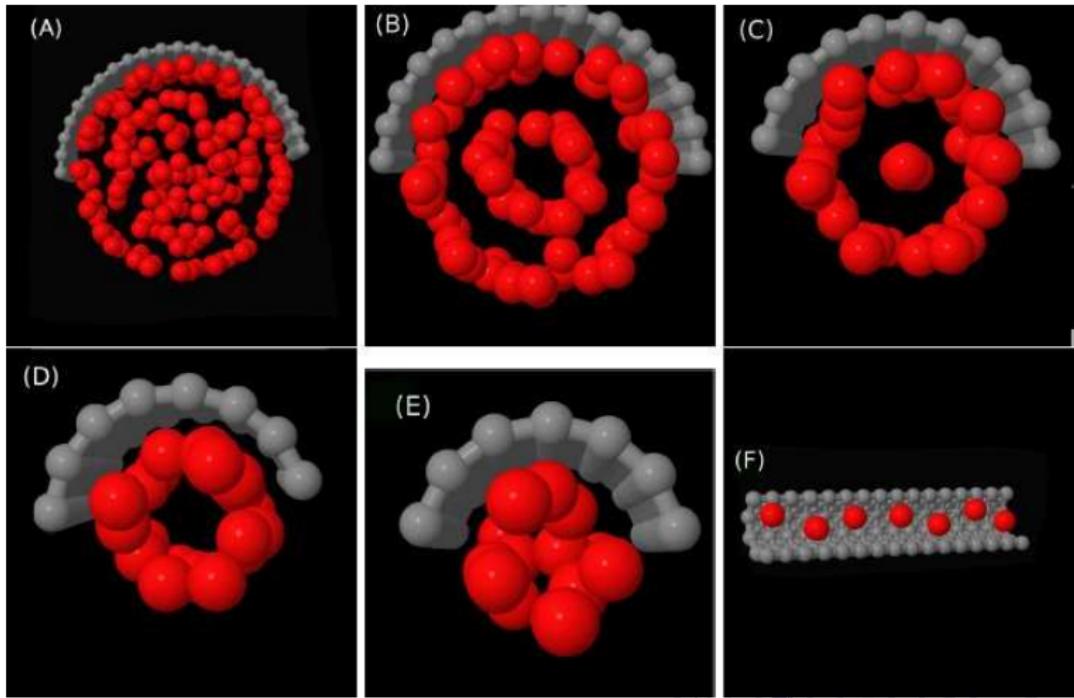
$$\begin{aligned}\langle v_x \rangle &= \gamma_{HP} \frac{\Delta p}{L_{NT}} \\ \gamma_{HP} &= \frac{a^2}{8\eta} \\ \eta &= \frac{k_B T}{3\pi\sigma D_x}\end{aligned}$$

$$\langle v_x \rangle = \gamma_{MD} \frac{\Delta p}{L_{NT}}$$

$$\epsilon = \frac{\gamma_{MD}}{\gamma_{HP}} \quad (1)$$

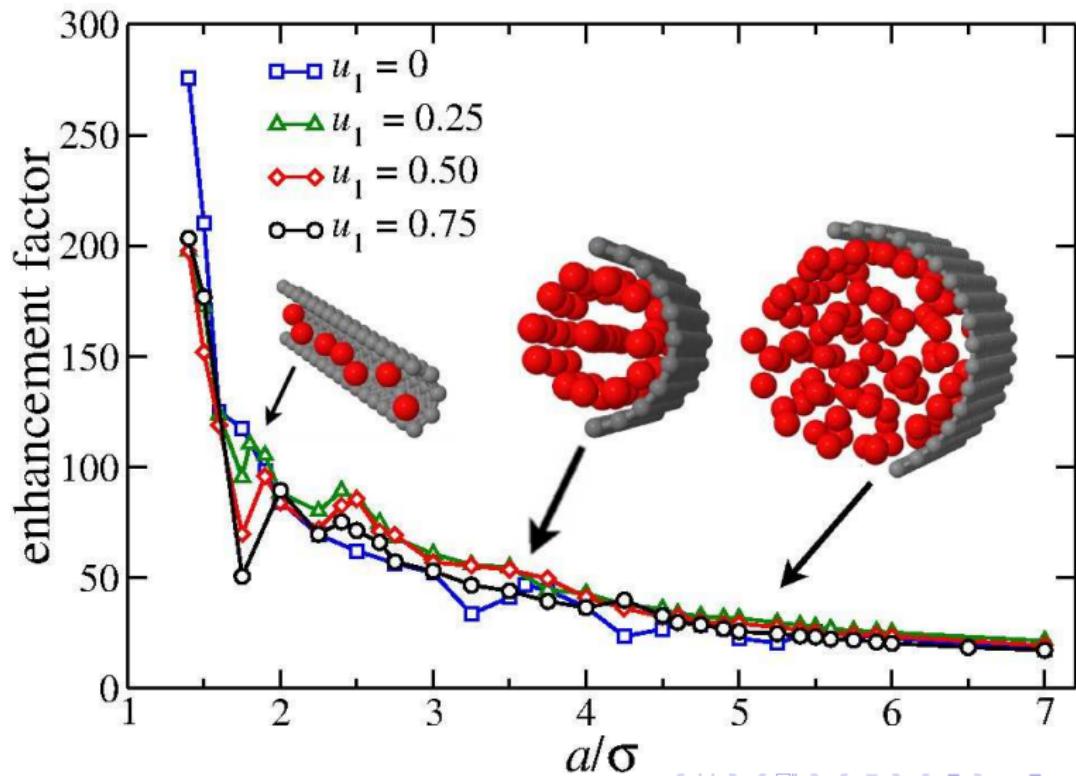
# Layers

J. R. Bordin, A. Diehl and MCB, JPCB (2013)



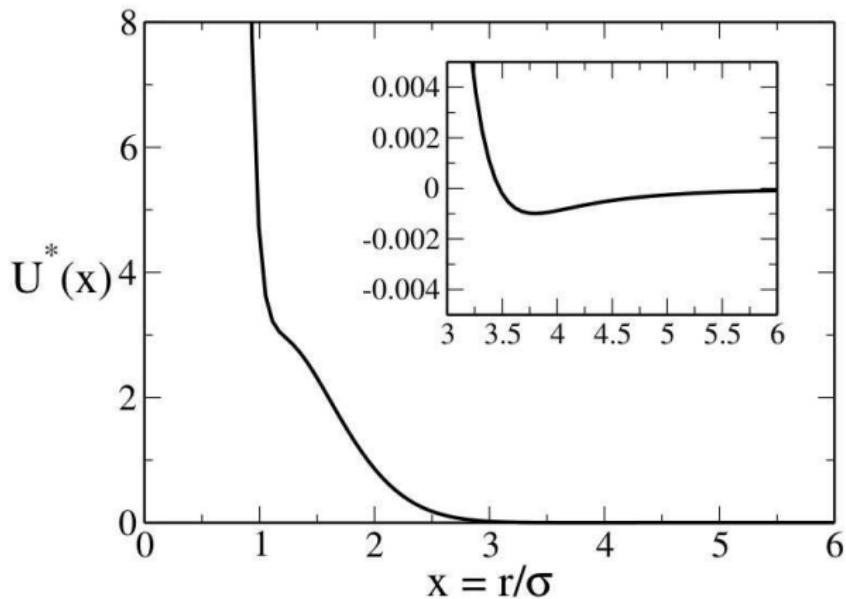
# Enhancement Flow

J. R. Bordin, A. Diehl and MCB, JPCB (2013)



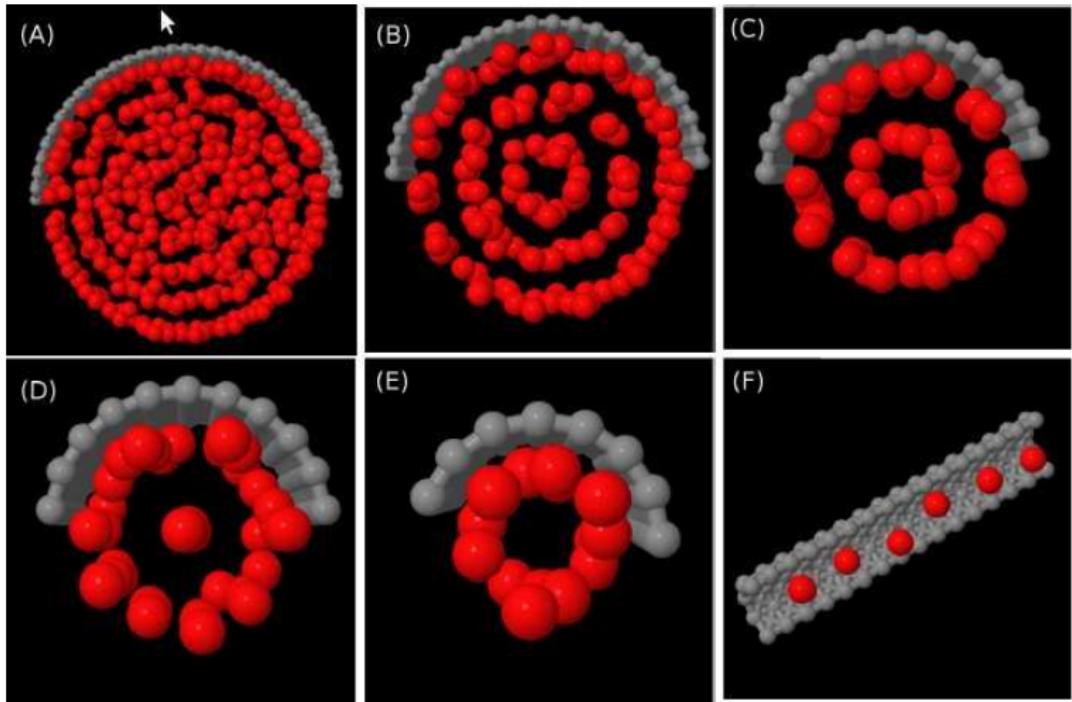
# Potential

J. R. Bordin, A. Diehl and MCB, JPCB (2013)



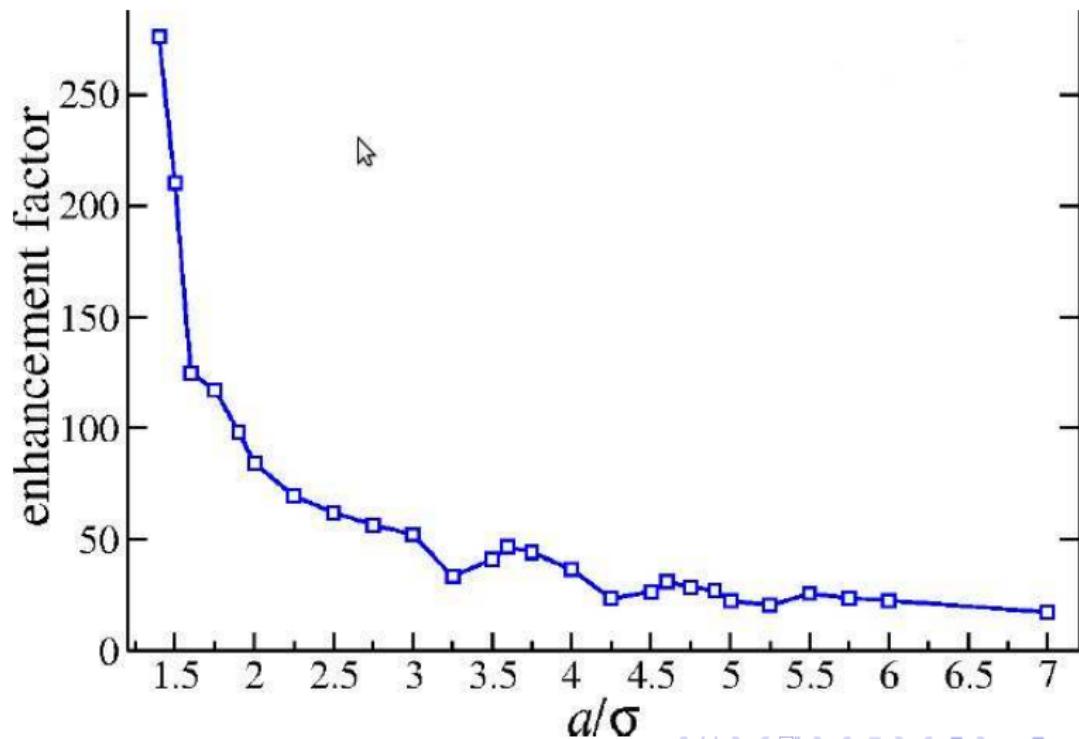
# Layers

J. R. Bordin, A. Diehl and MCB, JPCB (2013)



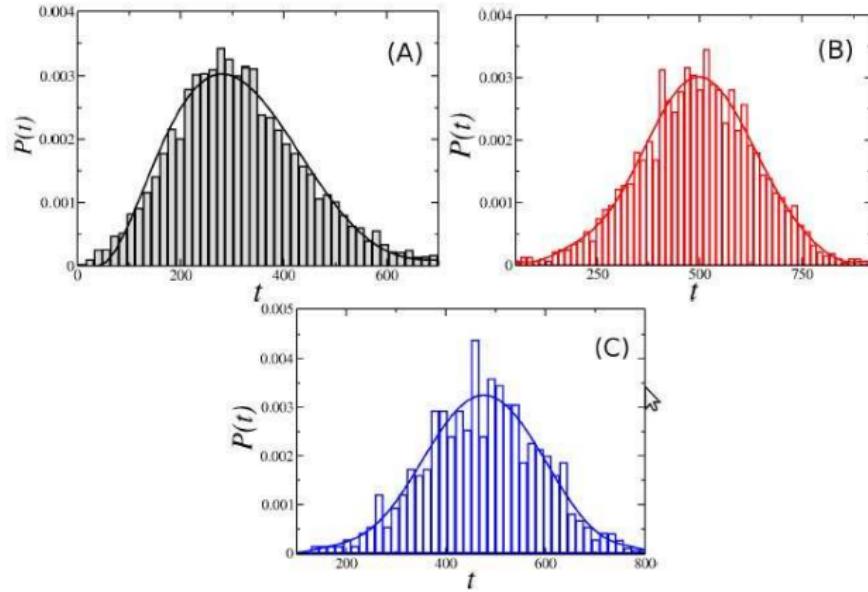
# Enhancement Flow

J. R. Bordin, A. Diehl and MCB, JPCB (2013)



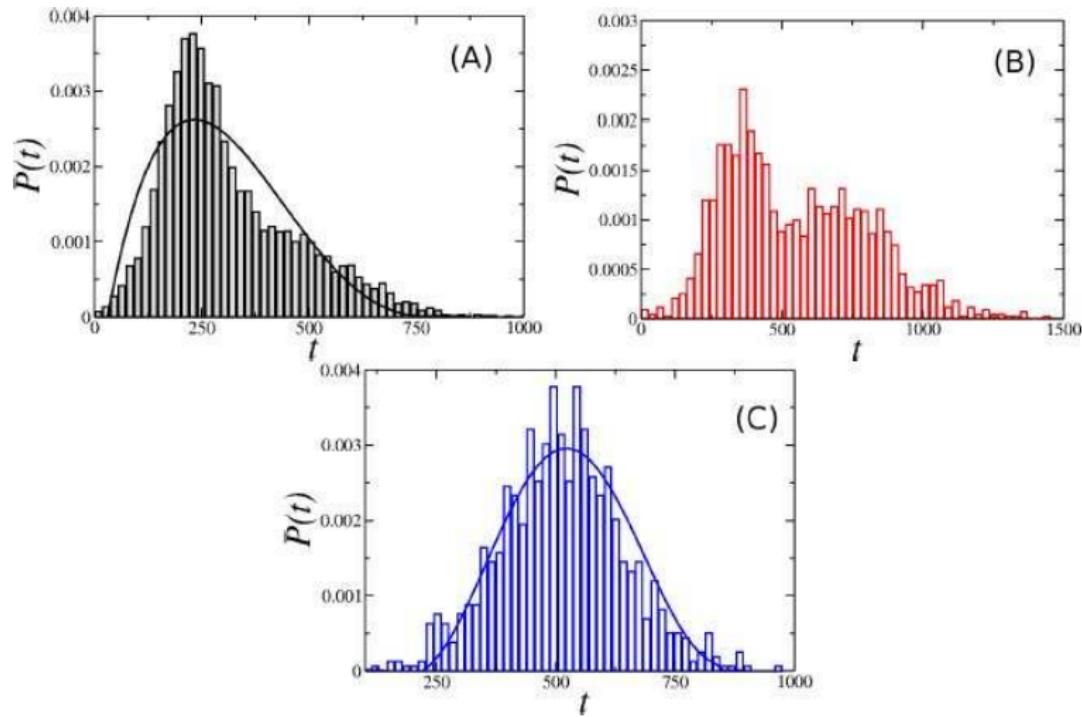
# Distribution - Attractive

J. R. Bordin, A. Diehl and MCB, JPCB (2013)



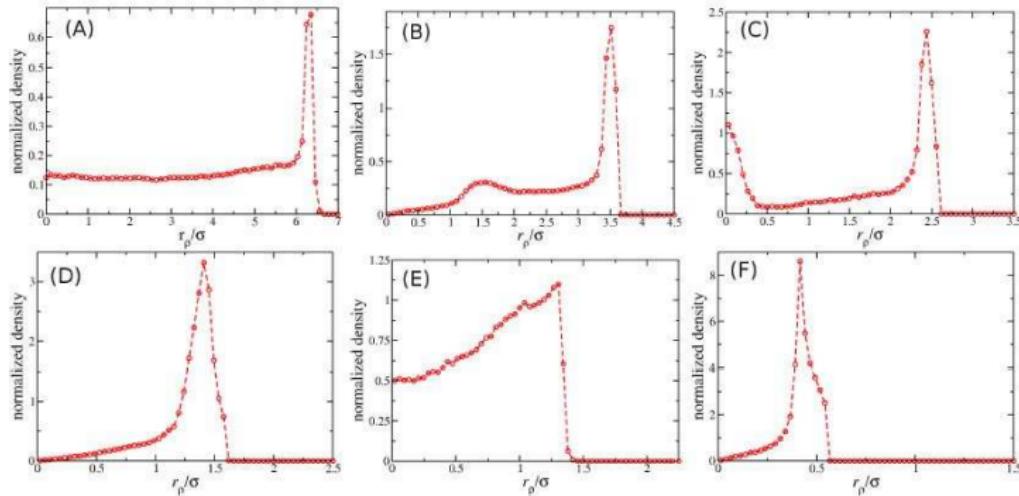
# Distribution - Repulsive

J. R. Bordin, A. Diehl and MCB, JPCB (2013)



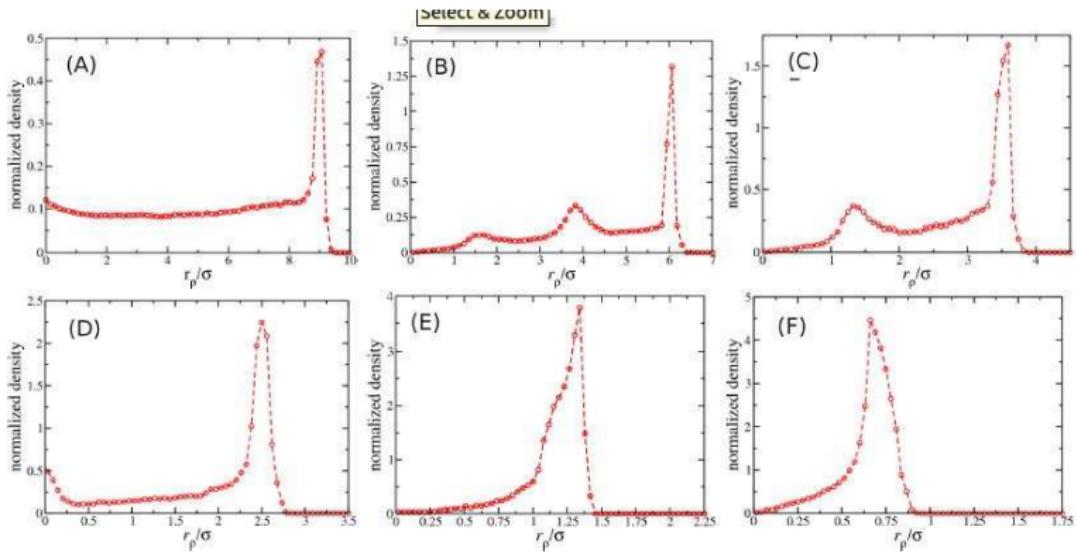
# Density - Attractive

J. R. Bordin, A. Diehl and MCB, JPCB (2013)



# Density - Repulsive

J. R. Bordin, A. Diehl and MCB, JPCB (2013)



# Conclusions

- ▶ Effective Model Reproduces the Thermodynamic Anomalies of Water
- ▶ Effective Model Reproduces the Dynamic Anomalies of Water