



# Model-free Neuromuscular Electrical Stimulation by Stochastic Extremum Seeking

Prof. Tiago Roux Oliveira

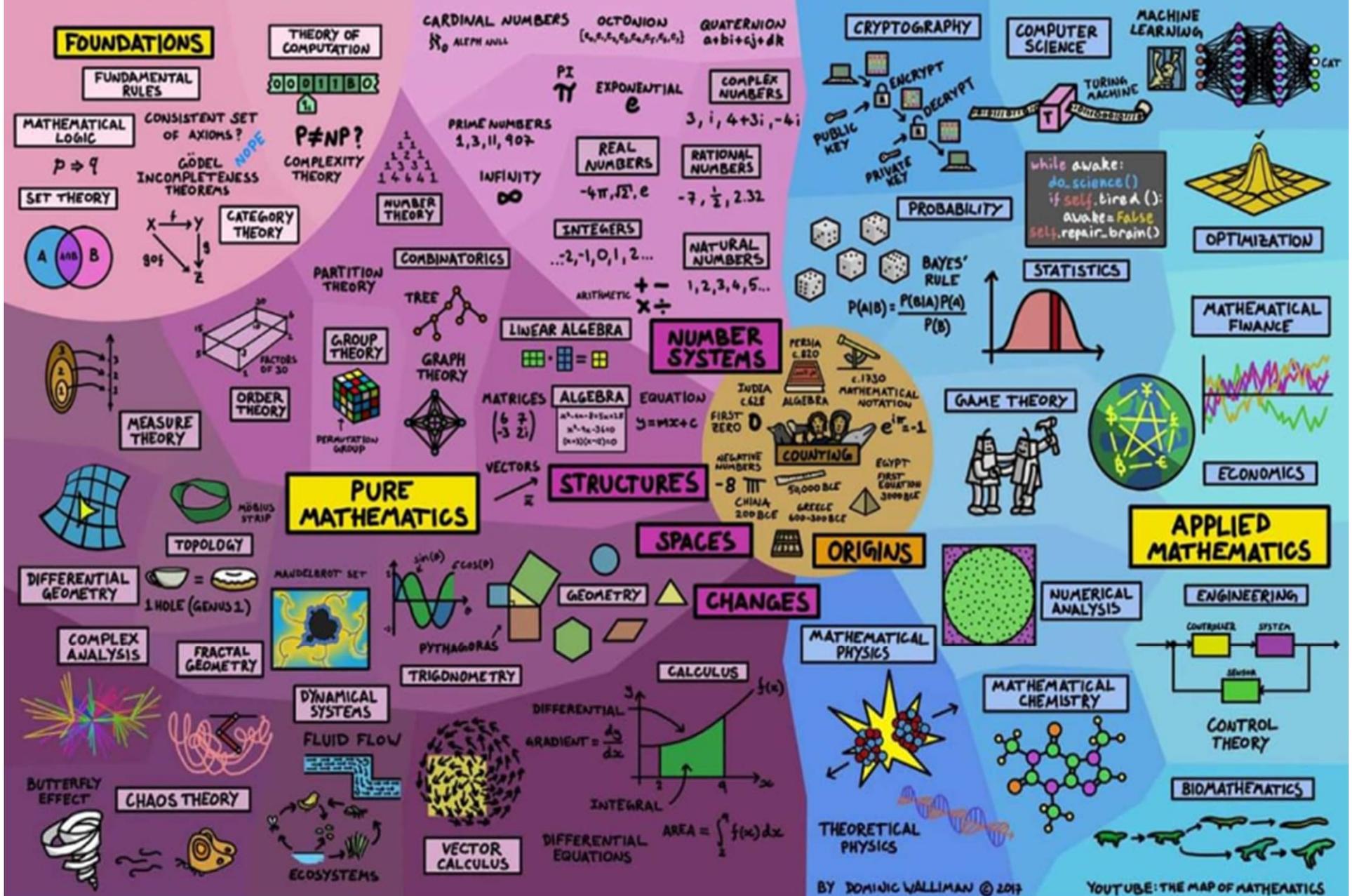


Rio de Janeiro, 23 de Maio de 2019

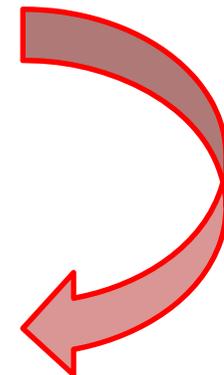
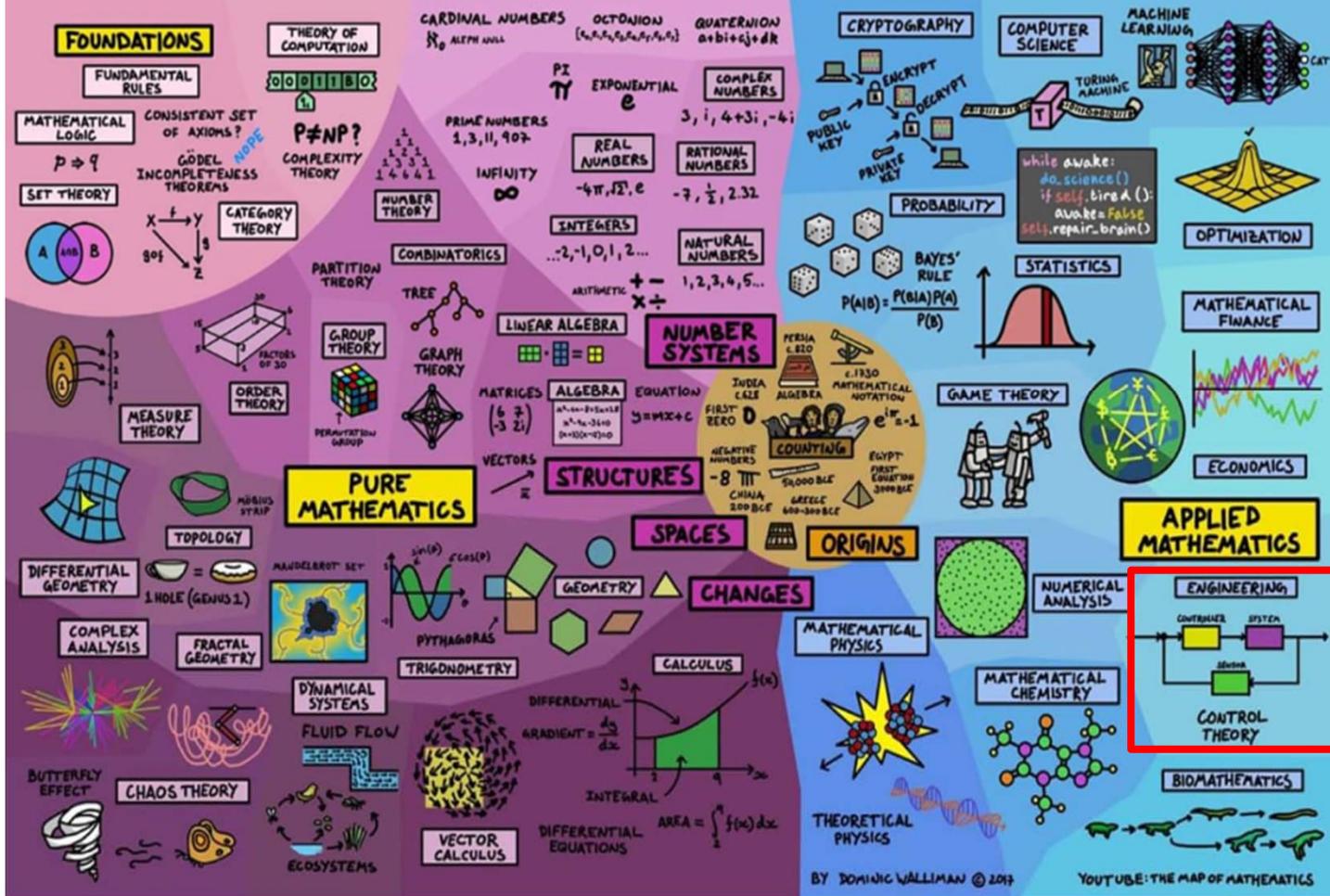
# OUTLINE

- ✓ THE MAP OF MATHEMATICS
- ✓ CAREER ACHIEVEMENTS
- ✓ MOTIVATION
- ✓ NMES DEFINITION
- ✓ TEST PROTOCOL
- ✓ MATERIALS AND METHODS
- ✓ STOCHASTIC EXTREMUM SEEKING
- ✓ EXPERIMENTAL RESULTS
- ✓ CONCLUSION
- ✓ TALKS AND PUBLICATIONS

# THE MAP OF MATHEMATICS



# THE MAP OF MATHEMATICS



- ✓ NONLINEAR SYSTEMS
- ✓ ADAPTIVE CONTROL / EXTREMUM SEEKING
- ✓ SLIDING MODE CONTROL
- ✓ TIME DELAYS
- ✓ PDEs

# CAREER ACHIEVEMENTS

## EDUCATION

- 2006-2010**      **Ph.D. in Electrical Engineering (Control Theory), COPPE/UFRJ**  
Federal University of Rio de Janeiro, under the supervision of Prof. Liu Hsu
- 2004-2006**      **M.Sc. in Electrical Engineering (Control Theory), COPPE/UFRJ**  
Federal University of Rio de Janeiro, under the supervision of Prof. Liu Hsu
- 2004-2006**      **B.Sc. in Electrical Engineering (Telecommunications), UERJ**  
State University of Rio de Janeiro, under the supervision of Prof. Alexandre Assis

## EMPLOYMENT AND SERVICES

- 2010 - ...**      **State University of Rio de Janeiro (UERJ), Brazil - Associate Professor**
- 2014-2015**      **University of California - San Diego (UCSD), California, USA - Visiting Scholar/Researcher, Cymer Center for Control Systems and Dynamics, under the supervision of Prof. Miroslav Krstic**
- 2014 - ...**      **International Federation on Automatic Control (IFAC) - Member of Technical Committee, Adaptive/Learning Systems (TC1.2) & Control Design (TC2.1)**
- 2016 - ...**      **Technical Committee on Variable Structure & Sliding Mode Control (IEEE) - Member Roster**
- 2016**      **International Journal of Adaptive Control and Signal Processing (Wiley) - Guest Editor**
- 2017 - ...**      **Journal The Franklin Institute (Elsevier) - Associate Editor**
- 2018 - ...**      **IEEE Latin America Transactions - Associate Editor**
- 2018 - ...**      **Brazilian Academy of Sciences (ABC), Brazil - Affiliate Member**

**PUBLICATIONS:      45 journal papers, 91 Conference papers, 09 Book Chapters**



**FUNDING AGENCIES :**



**H-Factor Google Scholar: 14**  
**Index i10 Google Scholar: 20**

## CAREER ACHIEVEMENTS

- Prêmio CAPES de Teses 2011



## CAREER ACHIEVEMENTS

- Pós-Doutorado: University of California (2014 - 2015)



Prof. Miroslav Krstic

## CAREER ACHIEVEMENTS

- **Membro Academia Brasileira de Ciências 2017 - 2021**



Prof. Liu Hsu



## CAREER ACHIEVEMENTS

- **IEEE Senior Member (2018)**

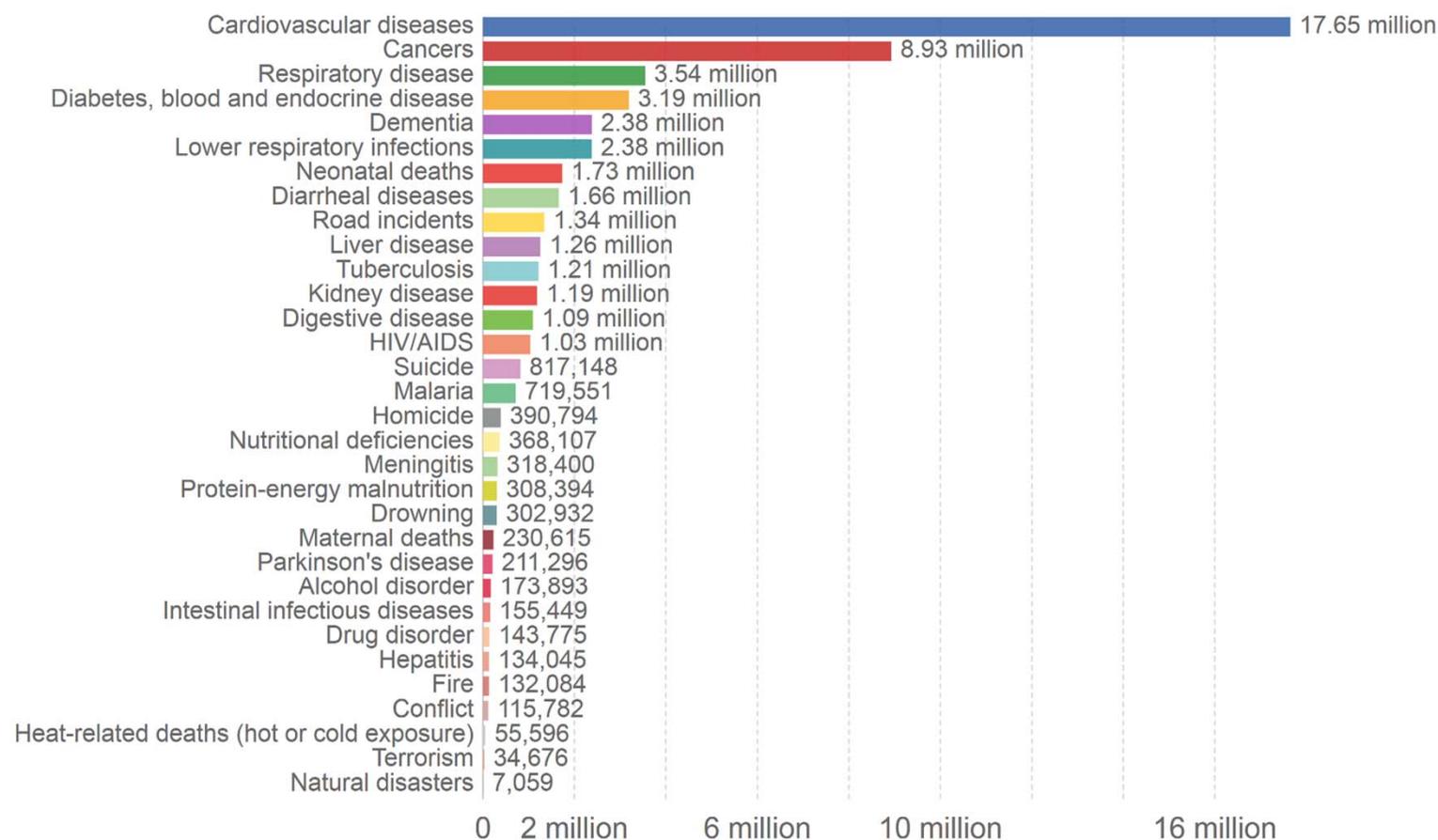


# MOTIVATION

## STROKE DISEASE IN THE WORLD

### Annual number of deaths by cause, World, 2016

Data refers to the specific cause of death, which is distinguished from risk factors for death, such as air pollution, diet and other lifestyle factors. See sources for further details on definitions of specific cause categories.



Source: Institute for Health Metrics and Evaluation (IHME); Global Terrorism Database (GTD); Amnesty International  
OurWorldInData.org/causes-of-death/ • CC BY-SA

# MOTIVATION



Impact in social life / Depression

- ✓ motor disorder
- ✓ spasticity



Traditional Physiotherapy

## FES/NMES – AUTOMATED PHYSIOTHERAPY

## APPLICATION TO FUNCTIONAL ELECTRICAL STIMULATION (FES)

Definition (Wikipedia):

**FES** is a technique that **uses low energy electrical pulses to** artificially generate body movements in individuals who have been paralyzed due to injury to the central nervous system. More specifically, FES can be used to **generate muscle contraction** in otherwise paralyzed limbs to produce functions such as grasping, walking, bladder voiding and standing ...

**Human-in-the-loop!**

**(NMES – Neuromuscular Electrical Stimulation)**

# ASSISTIVE ROBOTICS FOR STROKE PATIENTS

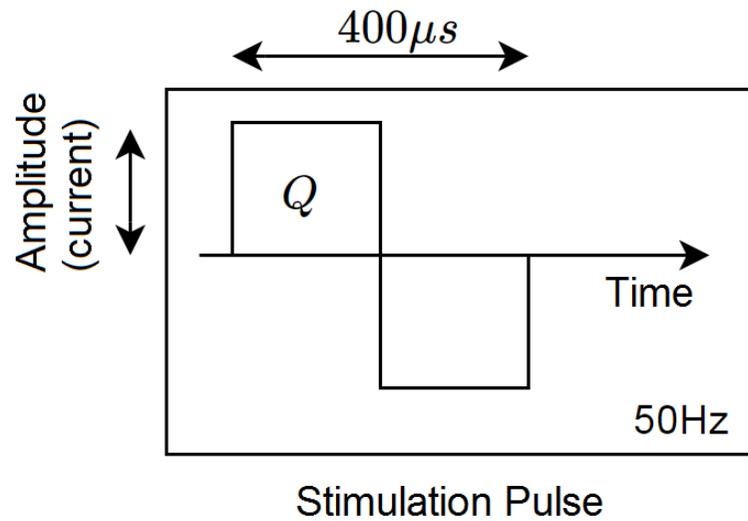
- Motor disorder
- Spasticity (hypertonia)
- Physiotherapy



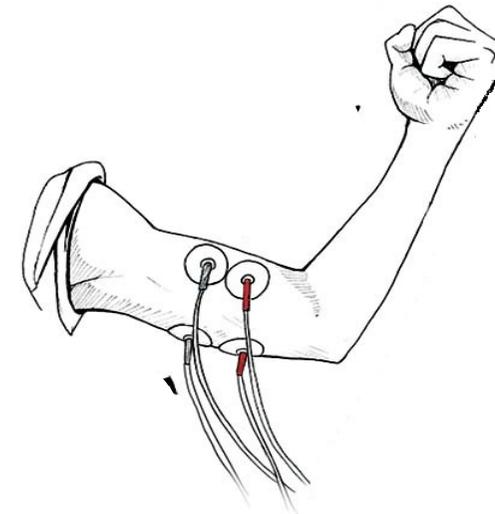
## Rehabilitation

- Passive or active movement
- **Closed-loop feedback** aids patients' recovery
- Design **control laws** for NMES

# ELECTRODES AND ELECTRICAL SIGNAL



(Pulse Amplitude Modulation)



(Flexion and Extension  
for Upper limbs)

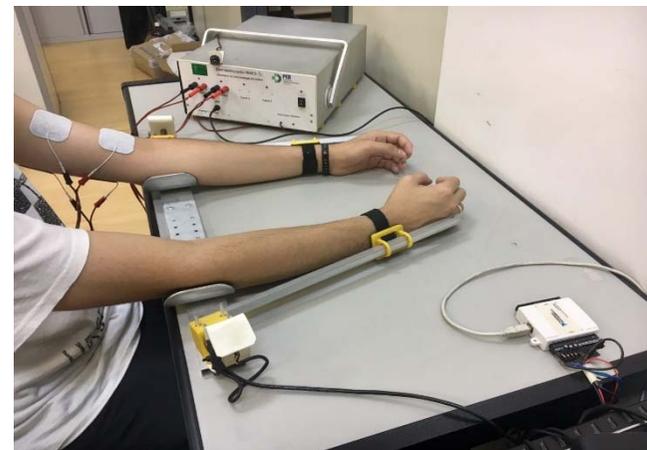
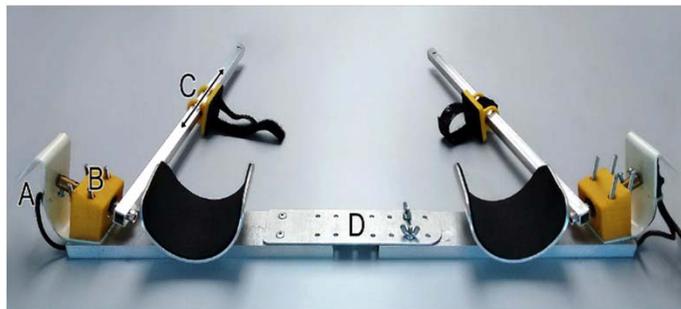
# MATERIALS AND METHODS

## Instrumentation

- Goniometer to obtain the elbow angle
- Programmable NMES (to avoid discomfort to the patient)
- Interface and control code developed using LabVIEW 12.0

## Mechanical Apparatus and Experimental Setup

- a single degree of freedom

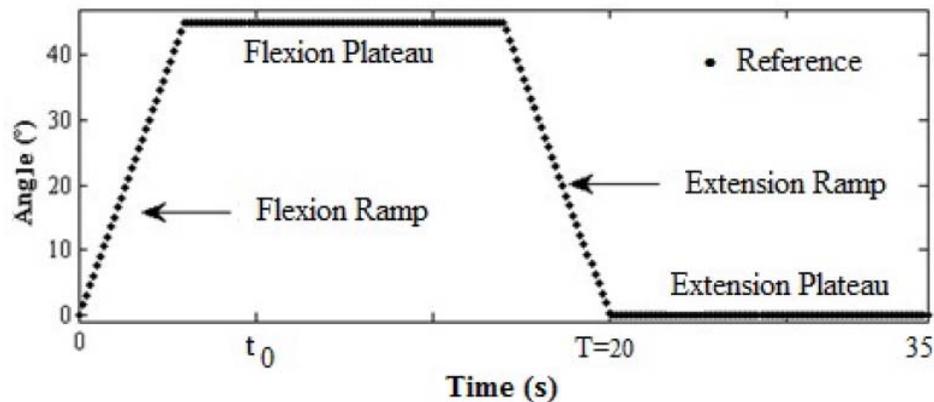


# MATERIALS AND METHODS

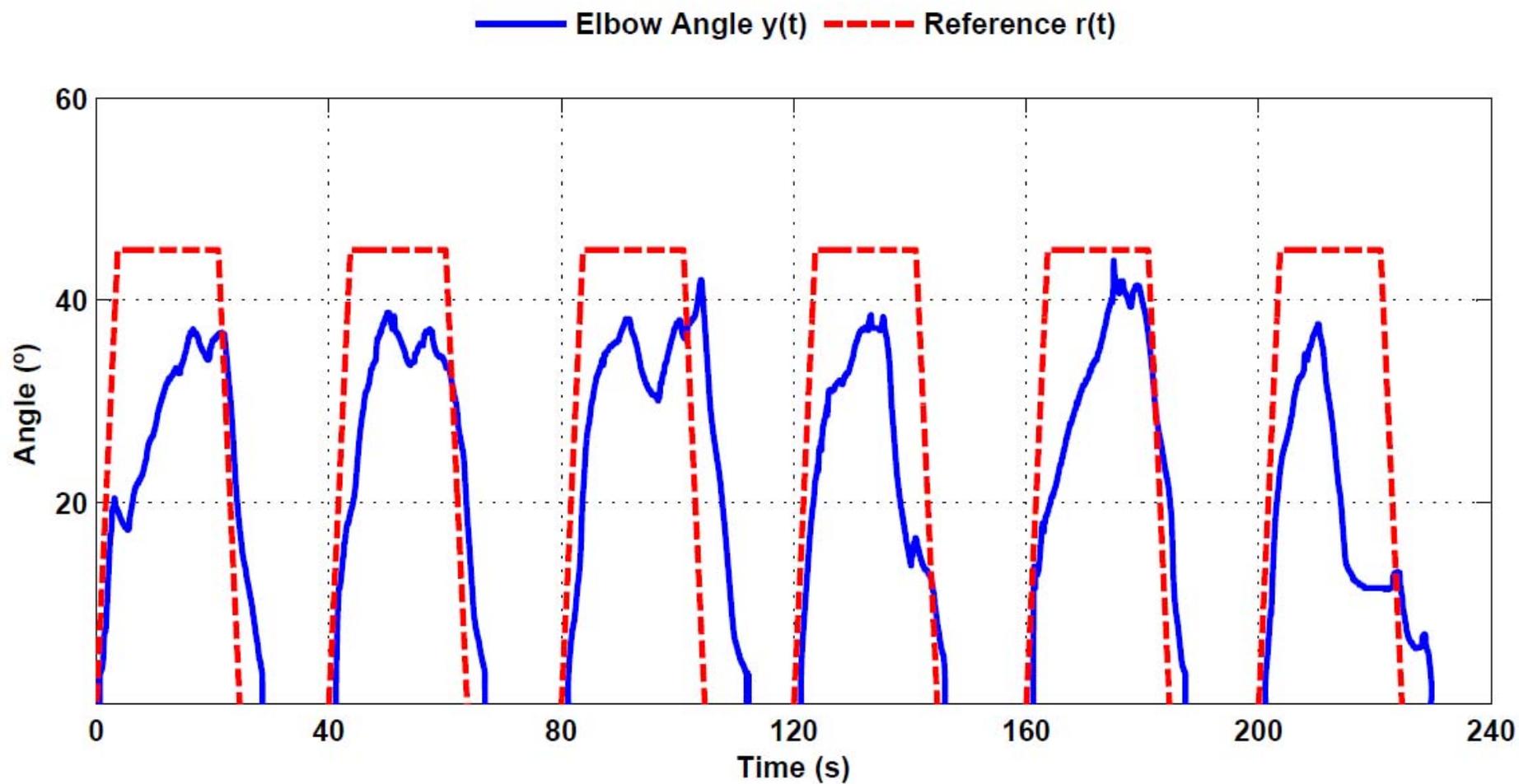
## Volunteers

- Healthy volunteers
- Stroke Patients
- Focus on upper limbs
- Extension and flexion movements
- Four sets of movements up to  $45^\circ$

(measured angle  $y$ )

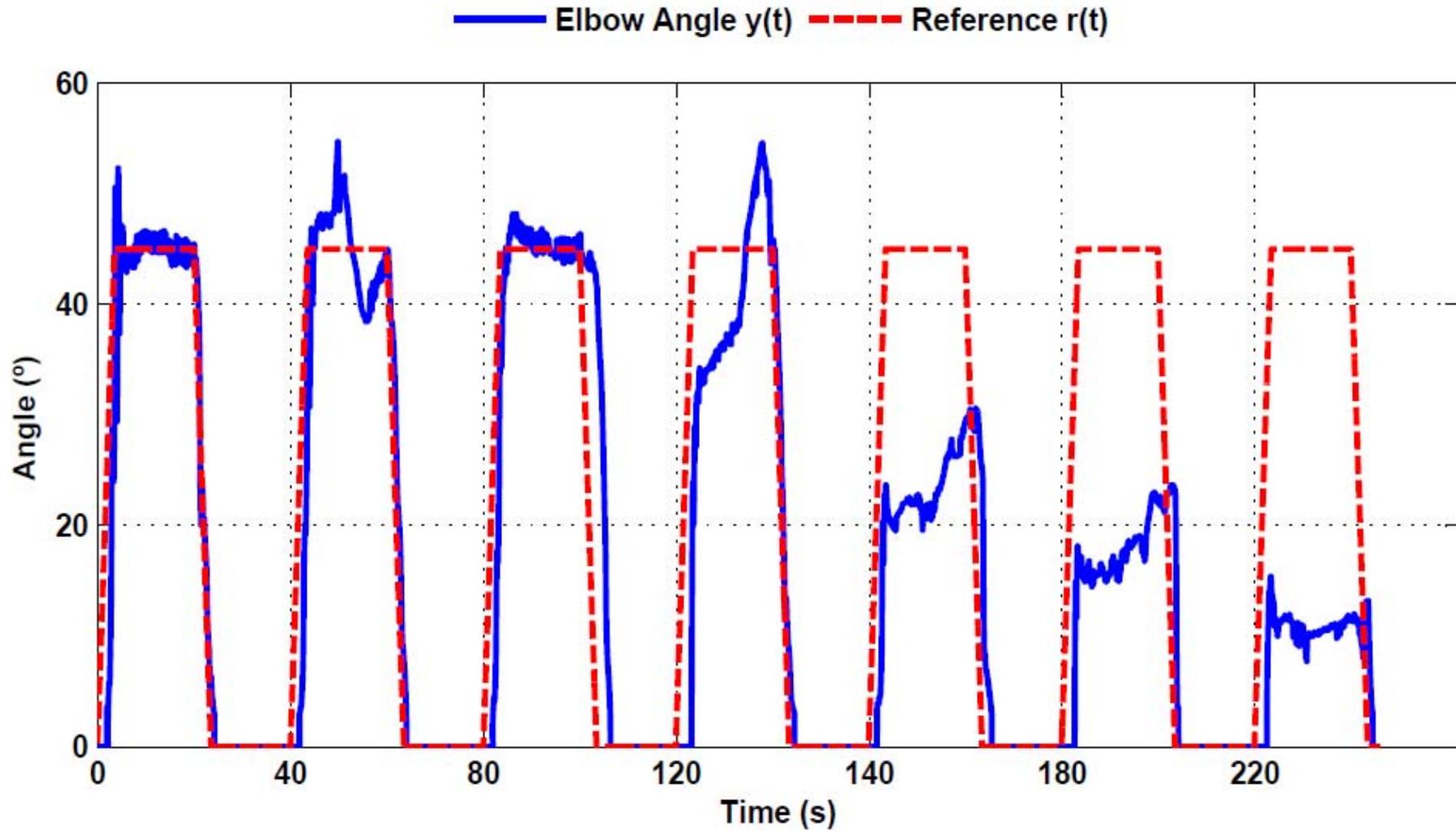


# EXPERIMENTS WITH STROKE PATIENT WITHOUT STIMULATION

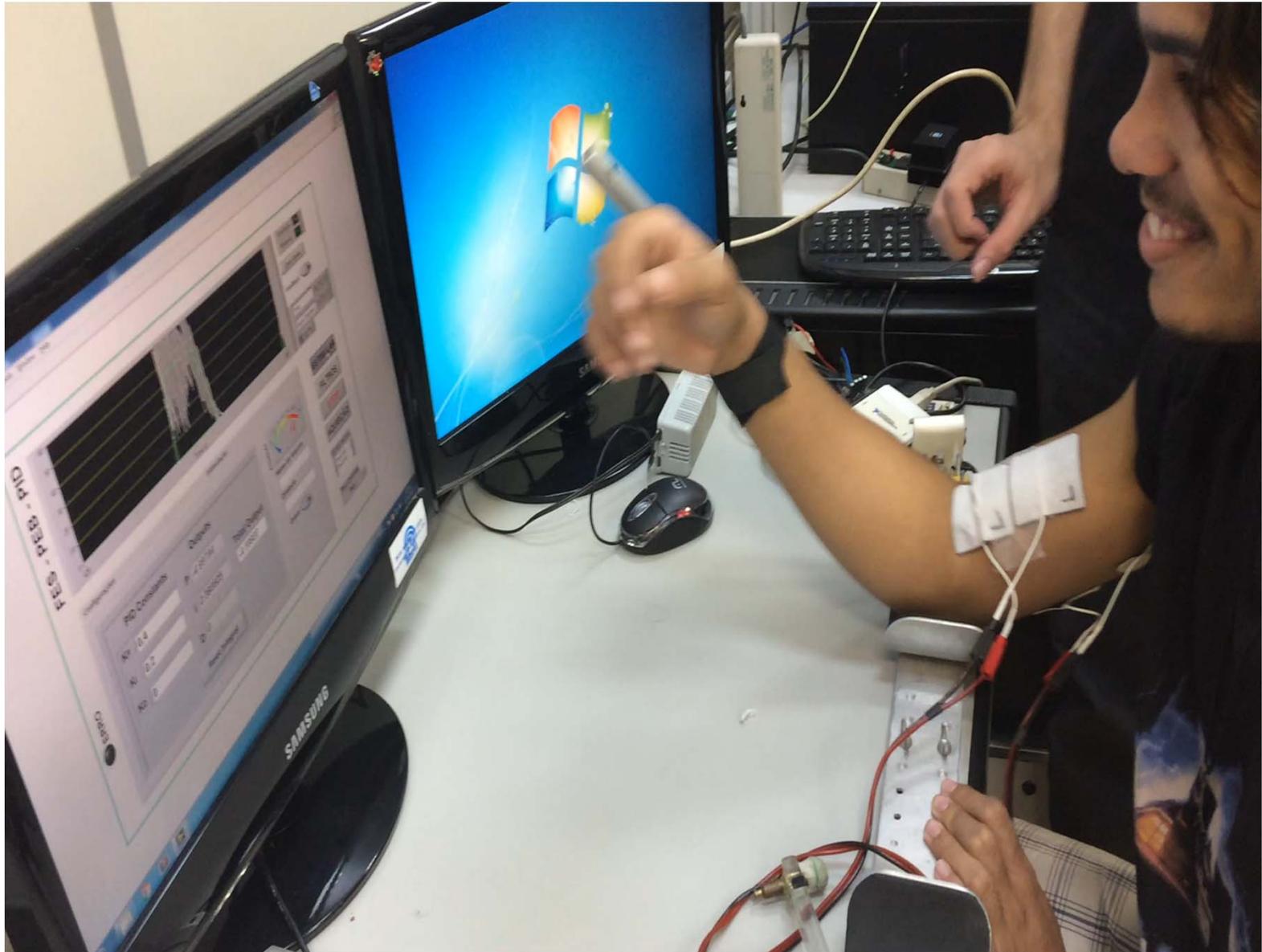


# EXPERIMENTS WITH STROKE WITH PID CONTROLLER

## PID WITH FIXED GAINS

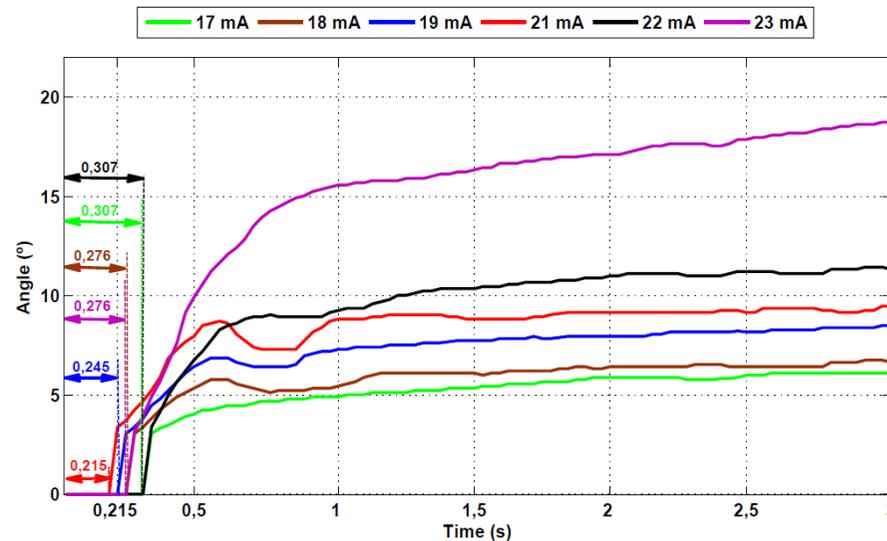


## FIXED GAINS – BAD TUNE



## CHALLENGES FOR MODELING AND ACTUATION

- **Different kinds of lesion** (parametric/relative degree uncertainties)
- Patient response changes over time (**time-varying system**)
- Saturation, dead-zone and fatigue (**nonlinear phenomena**)
- **Gravity action** (disturbances for upward movements)
- Hybrid bidirectional actuator (**biceps and triceps**)
- **Time delays** (small but present)



## CONTROL OBJECTIVES

- To apply **Extremum Seeking** algorithms to adapt the **PID** gains in order to achieve robustness for different patients
- Previous Works:
  - **Simple PI controller** (demands a long process of tuning)
  - **Filtered Sliding Mode Control + Time-scaling technique** (time dilation of the system responses, Padé approximations, singular perturbation theory)
  - Combination of both...

# PREVIOUS WORK WITH STROKE PATIENTS



ELSEVIER

Contents lists available at [ScienceDirect](https://www.sciencedirect.com)

Medical Engineering and Physics

journal homepage: [www.elsevier.com/locate/medengphy](http://www.elsevier.com/locate/medengphy)

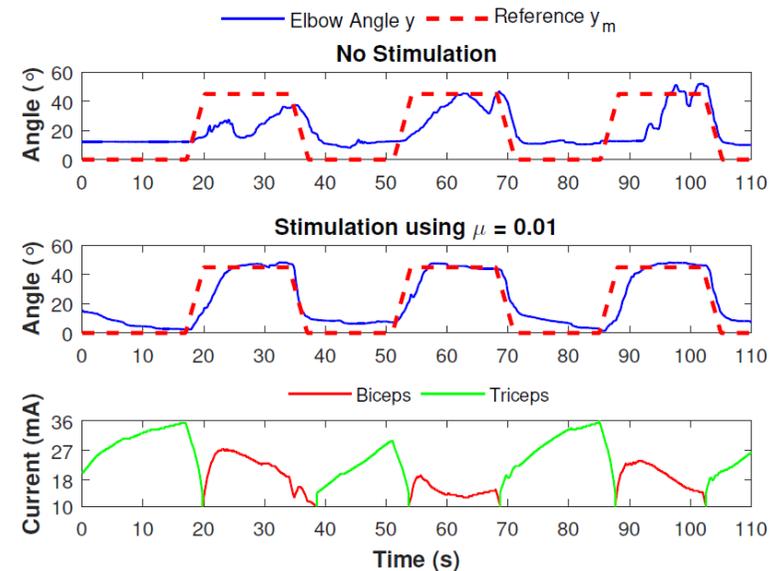
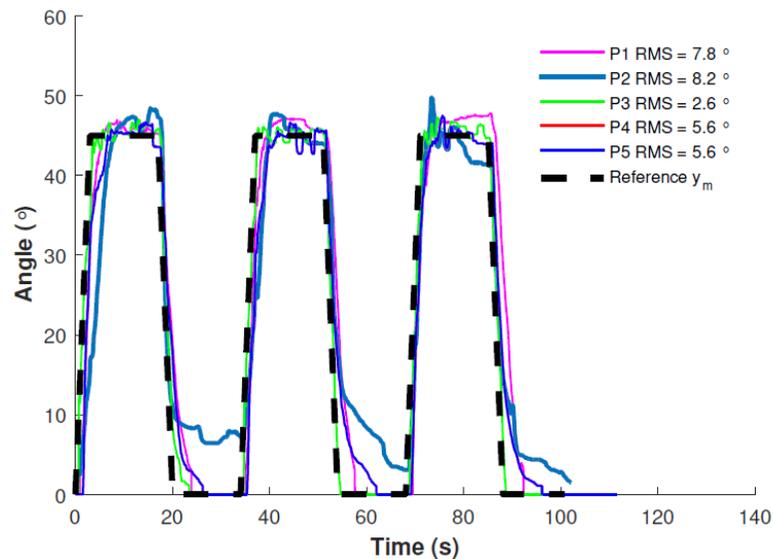


## Time-scaling based sliding mode control for Neuromuscular Electrical Stimulation under uncertain relative degrees

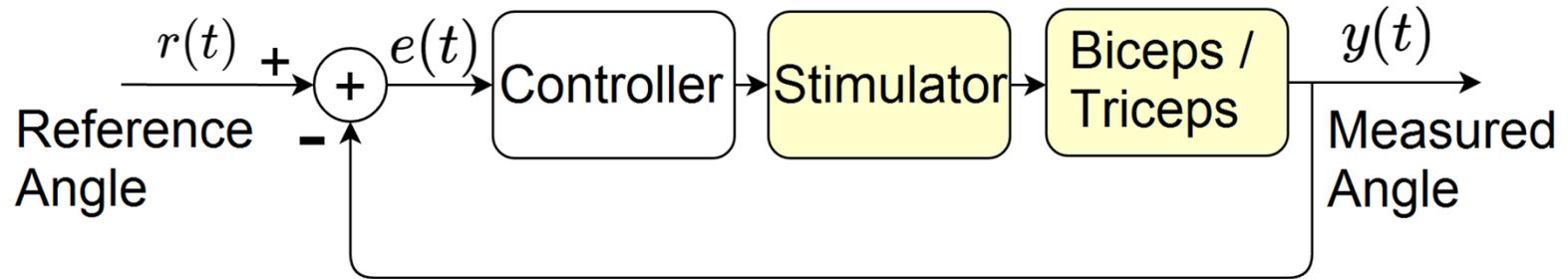
Tiago Roux Oliveira<sup>a,\*</sup>, Luiz Rennó Costa<sup>b</sup>, Joao Marcos Yamasaki Catunda<sup>b</sup>, Alexandre Visintainer Pino<sup>b</sup>, William Barbosa<sup>a</sup>, Marcio Nogueira de Souza<sup>b</sup>

<sup>a</sup>Department of Electronics and Telecommunication Engineering, State University of Rio de Janeiro (UERJ), Rio de Janeiro, RJ 20550-900, Brazil

<sup>b</sup>Biomedical Engineering Program, Federal University of Rio de Janeiro (COPPE/UFRJ), P.O. Box 68510, Rio de Janeiro, RJ 21945-970, Brazil



## ADAPTIVE CONTROL STRATEGY



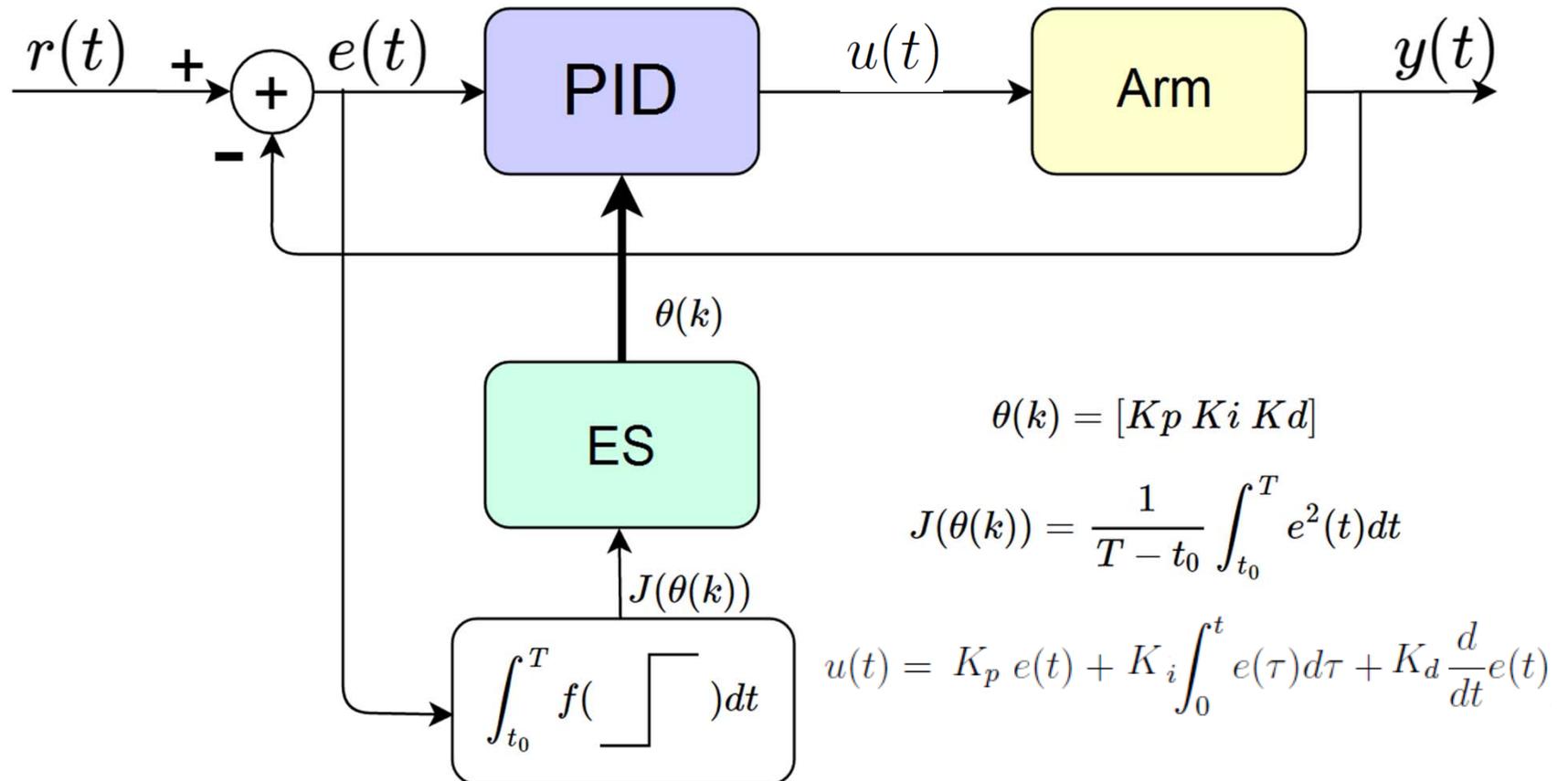
### Which Controller? Adaptive Control!

- Conventional Adaptive Control (control parametrization)
- Model Reference Adaptive Control (delays/relative degree obstacles)
- **PID with Extremum Seeking for adaptation**

### Automatic controller tuning: adaptation

- May solve the huge gap between healthy volunteers and stroke patients

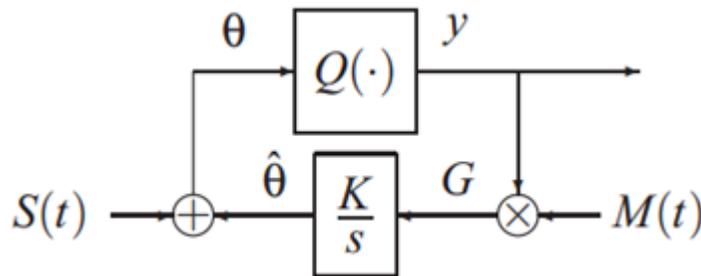
## PROPOSED CONTROLLER (PID + ES)



# BASICS OF DETERMINISTIC EXTREMUM SEEKING

**Standard ES for Quadratic Map:**

$$Q(\theta) = Q^* + \frac{H}{2}(\theta - \theta^*)^2$$



**Hessian  $H > 0$ : Minimization**  
**Hessian  $H < 0$ : Maximization**

**Dither Signals:**

$$S(t) = a \sin(\omega t)$$

$$M(t) = \frac{2}{a} \sin(\omega t)$$

**Averaging System:**

$$\frac{d\tilde{\theta}_{av}(t)}{dt} = kH\tilde{\theta}_{av}(t) \quad (\text{Hessian } H > 0 \text{ and } K < 0)$$

**Estimation error**

$$\tilde{\theta}(t) = \hat{\theta}(t) - \theta^* \quad \text{tends to} \quad \mathcal{O}(a + 1/\omega)$$

(by using Averaging Theorem)

# BASICS OF DETERMINISTIC EXTREMUM SEEKING

## SIMULATION

$$H = 2$$

$$Q^* = 0$$

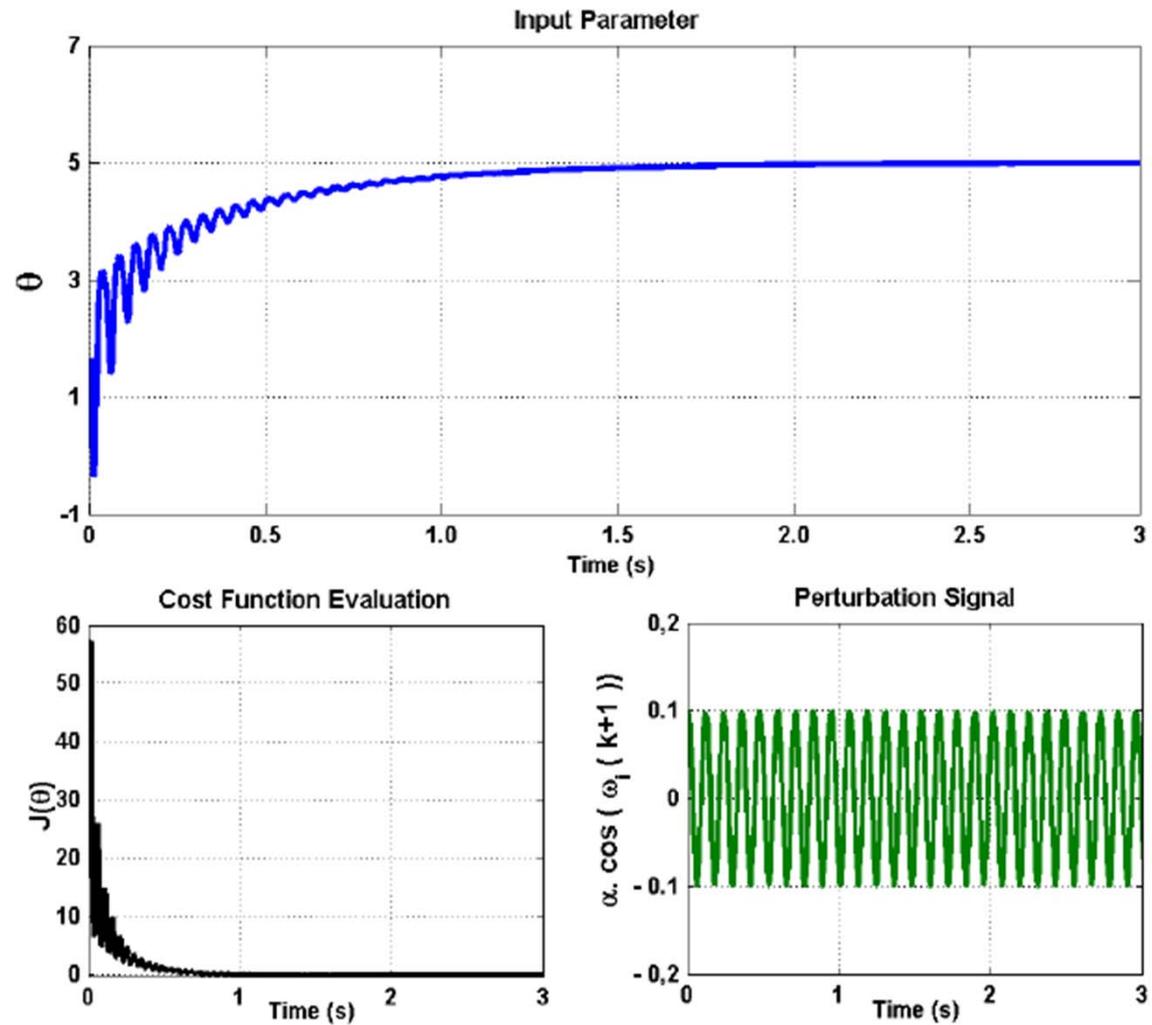
$$\theta^* = 5$$

$$\hat{\theta}(0) = 2$$

$$\omega = 2$$

$$\gamma = 0.01$$

$$a = 1$$



# BASICS OF STOCHASTIC EXTREMUM SEEKING

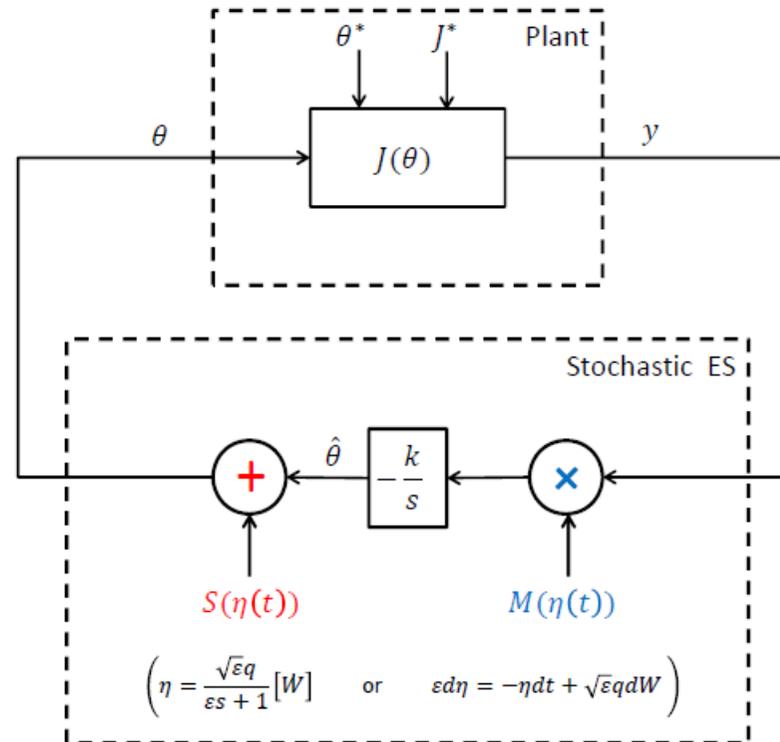
$$S(t) = a\eta t$$

$$M(t) = \frac{2}{a}\eta(t)$$

$$\tilde{\theta}(t) = \theta^* - \hat{\theta}(t)$$

$$\theta(t) = \hat{\theta}(t) + a\eta(t)$$

$$\theta(t) = a\eta(t) - \tilde{\theta}(t)$$



$$\dot{\tilde{\theta}}(t) = -\dot{\hat{\theta}}(t) = k \frac{2}{a} \eta(t) y(t) = k \frac{2}{a} \eta(t) f(\theta(t))$$

# BASICS OF STOCHASTIC EXTREMUM SEEKING

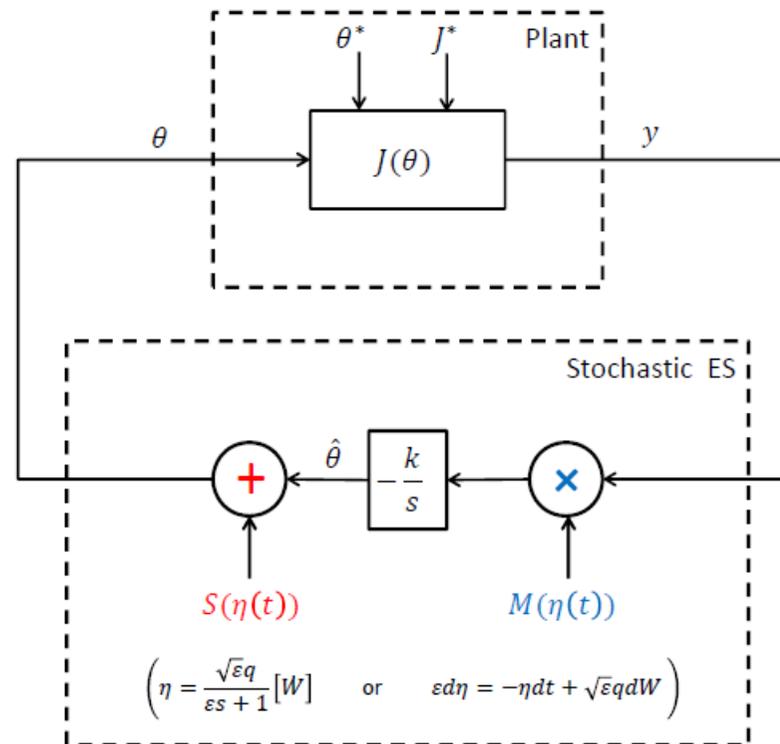
$$S(t) = a\eta t$$

$$M(t) = \frac{2}{a}\eta(t)$$

$$\tilde{\theta}(t) = \theta^* - \hat{\theta}(t)$$

$$\theta(t) = \hat{\theta}(t) + a\eta(t)$$

$$\theta(t) = a\eta(t) - \tilde{\theta}(t)$$



$$\dot{\tilde{\theta}}(t) = -\dot{\hat{\theta}}(t) = k \frac{2}{a} \eta(t) y(t) = k \frac{2}{a} \eta(t) f(\theta(t))$$

# BASICS OF STOCHASTIC EXTREMUM SEEKING

$\eta(t)$   $\longrightarrow$  STOCHASTIC PERTURBATION

$$\varepsilon d\eta = -\eta dt + \sqrt{\varepsilon} q dW$$

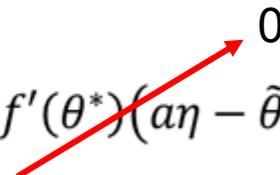
$\dot{W}(t)$  is a Gaussian white noise (with zero expectation and positive variance)

If  $\varepsilon$  is sufficiently small  $\rightarrow \eta$  is a good approximation of the white noise

## BASICS OF STOCHASTIC EXTREMUM SEEKING

$$f(\theta) = f(a\eta - \tilde{\theta}) \approx f(\theta^*) + f'(\theta^*)(a\eta - \tilde{\theta}) + \frac{1}{2}f''(\theta^*)(a\eta - \tilde{\theta})^2$$

If  $f(\theta)$  has a minimum at  $\theta^* \longrightarrow f'(\theta^*) = 0$

$$f(\theta) \approx f(\theta^*) + \cancel{f'(\theta^*)(a\eta - \tilde{\theta})} + \frac{1}{2}f''(\theta^*)(a\eta - \tilde{\theta})^2$$


$$f(\theta) \approx f(\theta^*) + \frac{1}{2}f''(\theta^*)(a\eta - \tilde{\theta})^2 = f(\theta^*) + \frac{1}{2}f''(\theta^*) (a^2\eta^2 - 2a\eta\tilde{\theta} + \tilde{\theta}^2)$$

## BASICS OF STOCHASTIC EXTREMUM SEEKING

$$\dot{\tilde{\theta}}(t) = k \frac{2}{a} \eta(t) f(\theta(t)) \qquad f(\theta) \approx f(\theta^*) + \frac{1}{2} f''(\theta^*) (a^2 \eta^2 - 2a\eta\tilde{\theta} + \tilde{\theta}^2)$$

$$\dot{\tilde{\theta}} \approx k \frac{2}{a} \eta \left\{ f(\theta^*) + \frac{1}{2} f''(\theta^*) [a^2 \eta^2 - 2a\eta\tilde{\theta} + \tilde{\theta}^2] \right\}$$

$$= k \frac{2}{a} \eta \left[ f(\theta^*) + \frac{a^2}{2} f''(\theta^*) \eta^2 - a f''(\theta^*) \eta \tilde{\theta} + \frac{1}{2} f''(\theta^*) \tilde{\theta}^2 \right]$$

$$\dot{\tilde{\theta}}(t) = k \frac{2}{a} \eta(t) \left[ f(\theta^*) + \frac{1}{2} f''(\theta^*) \tilde{\theta}^2(t) \right] - 2k \eta^2(t) f''(\theta^*) \tilde{\theta}(t) + k \eta^3(t) a f''(\theta^*)$$

## BASICS OF STOCHASTIC EXTREMUM SEEKING

$$\dot{\tilde{\theta}}(t) = k \frac{2}{a} \eta(t) \left[ f(\theta^*) + \frac{1}{2} f''(\theta^*) \tilde{\theta}^2(t) \right] - 2k \eta^2(t) f''(\theta^*) \tilde{\theta}(t) + k \eta^3(t) a f''(\theta^*)$$

$$\lim_{t \rightarrow +\infty} E\{\eta(t)\} = 0$$

$$\lim_{t \rightarrow +\infty} E\{\eta^2(t)\} = \frac{q^2}{2}$$

$$\lim_{t \rightarrow +\infty} E\{\eta^3(t)\} = 0$$

## BASICS OF STOCHASTIC EXTREMUM SEEKING

$$\dot{\tilde{\theta}}(t) = k \frac{2}{a} \eta(t) \left[ f(\theta^*) + \frac{1}{2} f''(\theta^*) \tilde{\theta}^2(t) \right] - 2k\eta^2(t) f''(\theta^*) \tilde{\theta}(t) + k\eta^3(t) a f''(\theta^*)$$

$$\lim_{t \rightarrow +\infty} E\{\eta(t)\} = 0 \qquad \lim_{t \rightarrow +\infty} E\{\eta^2(t)\} = \frac{q^2}{2} \qquad \lim_{t \rightarrow +\infty} E\{\eta^3(t)\} = 0$$

$$\dot{\tilde{\theta}}(t) = k \frac{2}{a} \eta(t) \left[ f(\theta^*) + \frac{1}{2} f''(\theta^*) \tilde{\theta}^2(t) \right] - 2k\eta^2(t) f''(\theta^*) \tilde{\theta}(t) + k\eta^3(t) a f''(\theta^*)$$

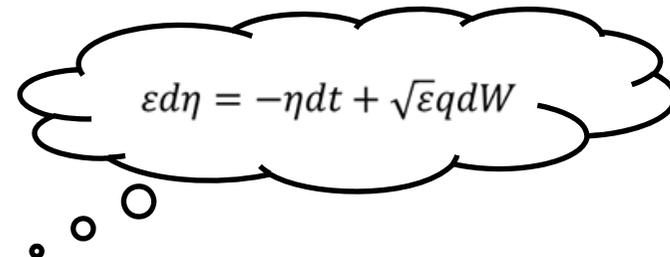
0
0
0

# BASICS OF STOCHASTIC EXTREMUM SEEKING

$$\lim_{t \rightarrow +\infty} E\{\eta(t)\} = 0$$

$$\lim_{t \rightarrow +\infty} E\{\eta^2(t)\} = \frac{q^2}{2}$$

$$\lim_{t \rightarrow +\infty} E\{\eta^3(t)\} = 0$$



$$\epsilon d\eta = -\eta dt + \sqrt{\epsilon} q dW$$

Applying Ito's differentiation rule to  $\eta^2$

we obtain the ordinary differential equation  
with solution being simply:

$$\frac{\epsilon}{2} \frac{dE\{\eta^2\}}{dt} = -E\{\eta^2\} + \frac{q^2}{2}$$

$$E\{\eta^2(t)\} = e^{-2t/\epsilon} E\{\eta^2(0)\} + \frac{q^2}{2} (1 - e^{-2t/\epsilon}) \quad \longrightarrow \quad \frac{q^2}{2} \text{ as } t \rightarrow \infty$$

$$\dot{\tilde{\theta}}(t) \approx -kq^2 f''(\theta^*) \tilde{\theta}(t)$$

$$\frac{\text{speed}_{\sin \eta}}{\text{speed}_{\eta}} = \frac{(1 - e^{-q^2})}{q^2}$$

# BASICS OF STOCHASTIC EXTREMUM SEEKING

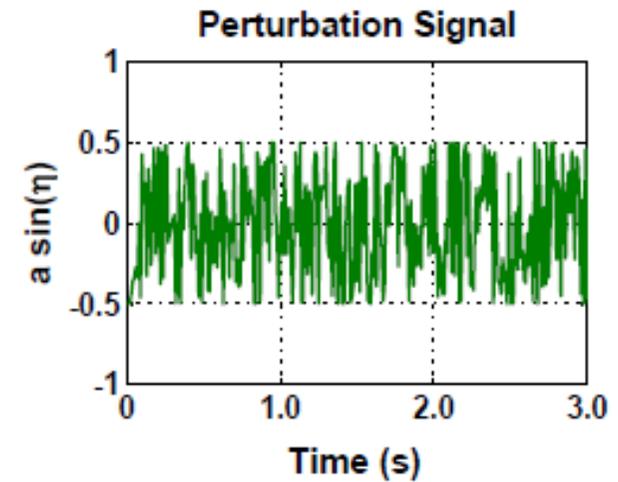
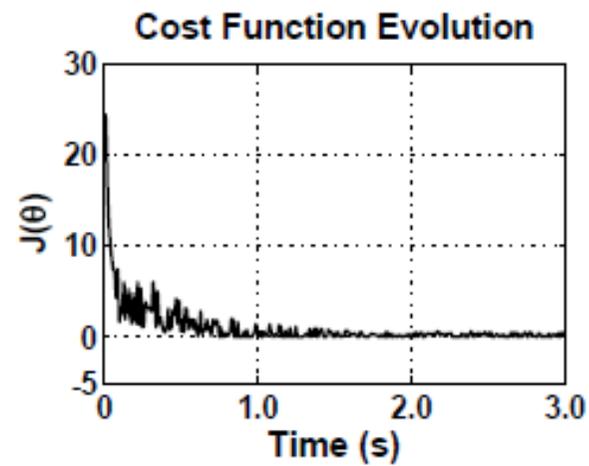
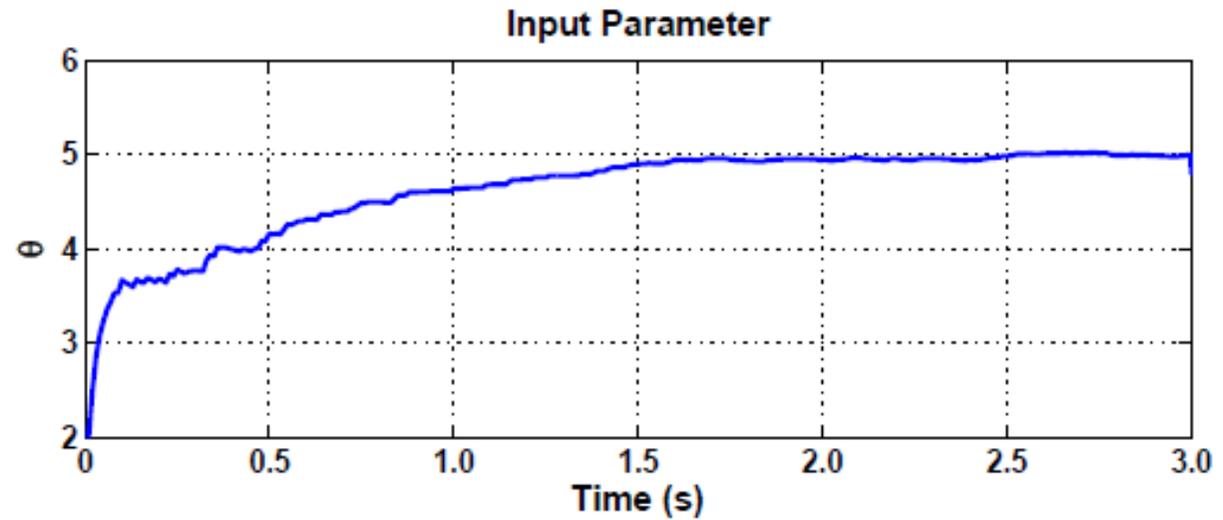
## SIMULATION

$$q = 1$$

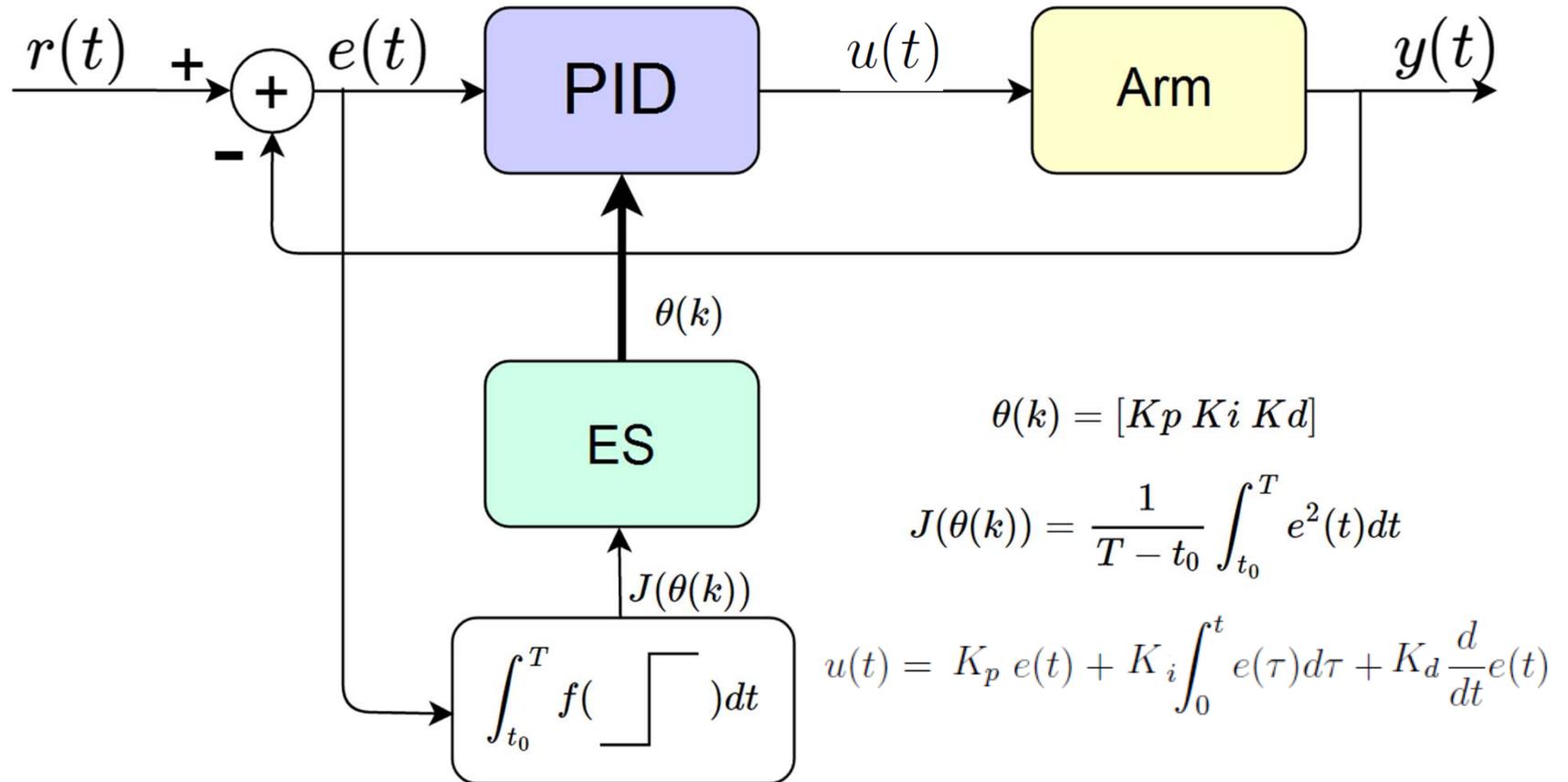
$$\varepsilon = 0,25$$

$$a = 0,5$$

$$k = 10$$



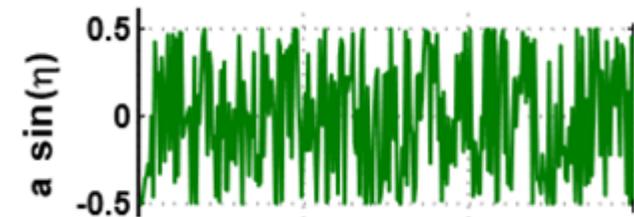
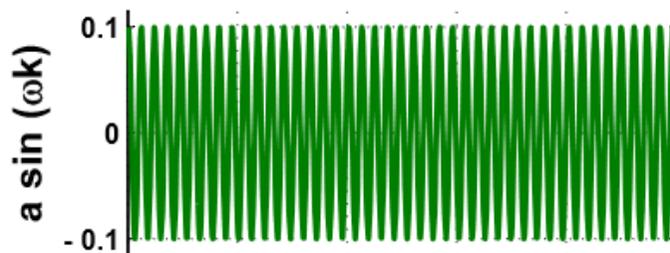
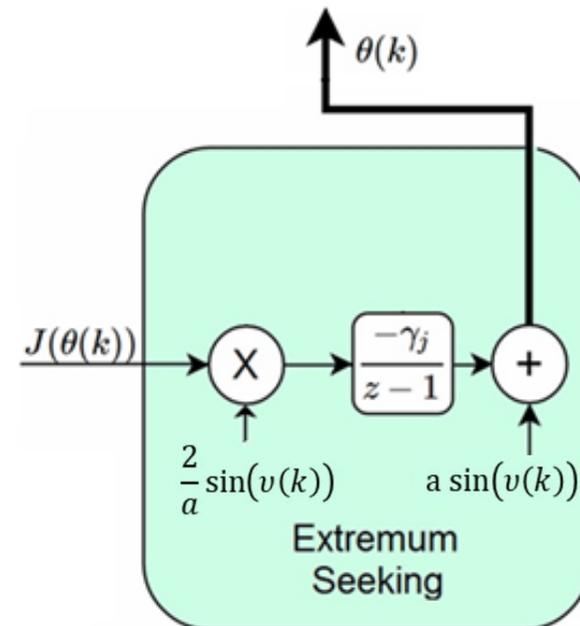
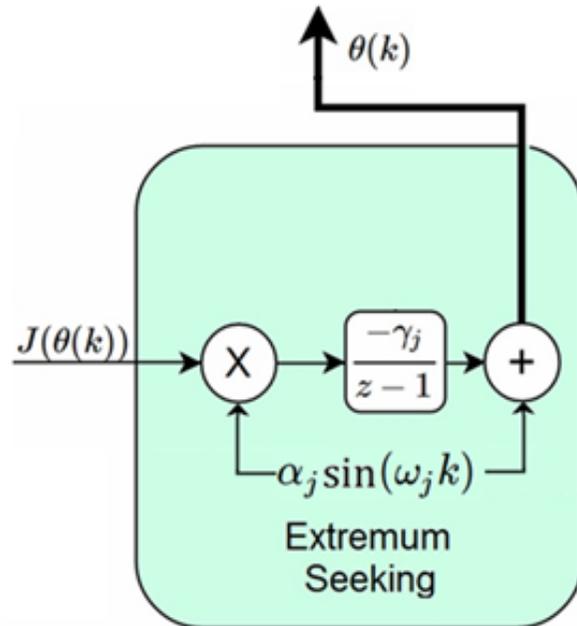
## PROPOSED CONTROLLER (PID + ES)



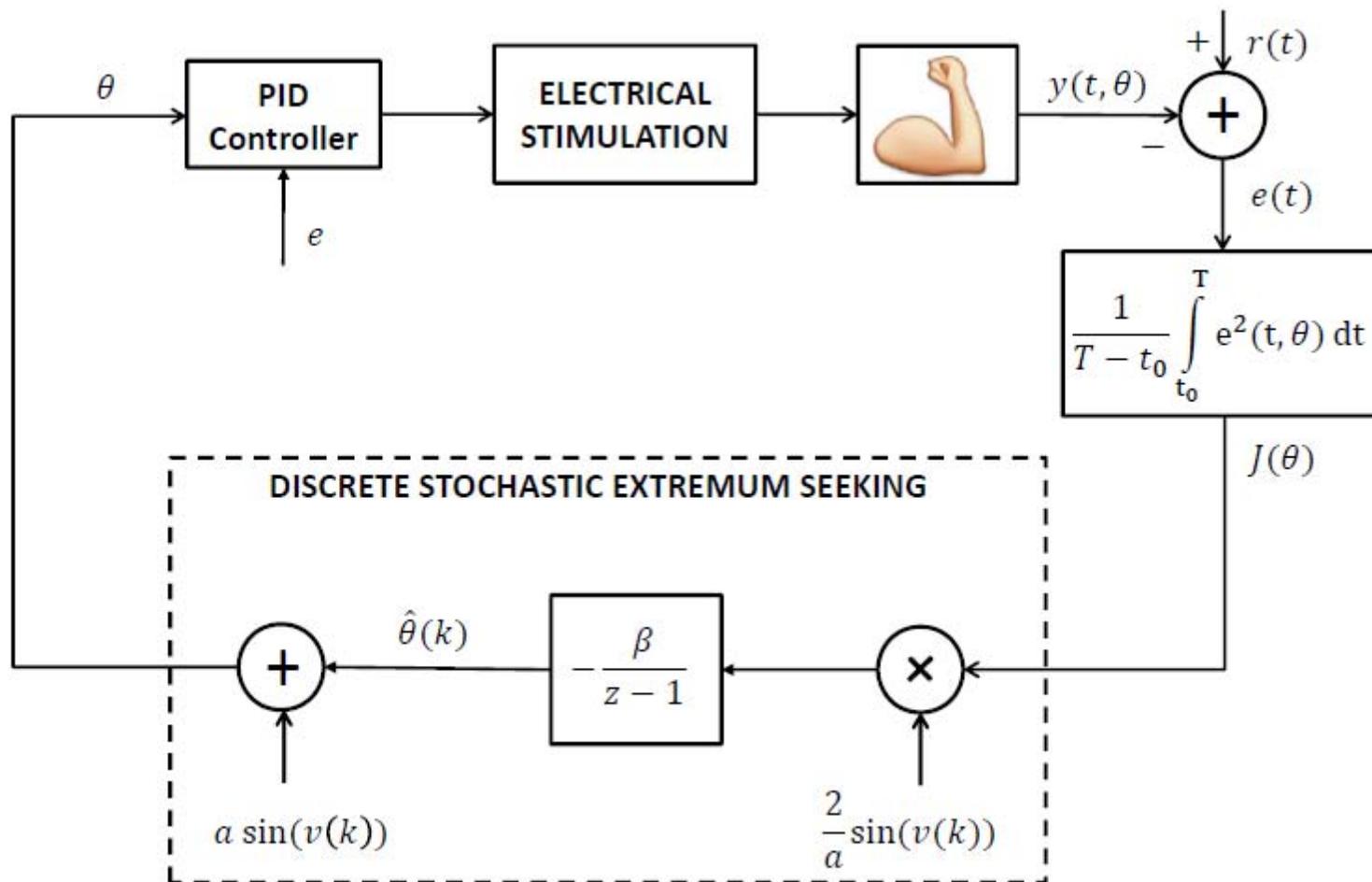
# DETERMINISTIC versus STOCHASTIC EXTREMUM SEEKING

$$\hat{\theta}_i(k+1) = \hat{\theta}_i(k) - \gamma \alpha_i \sin(\omega_i k) [J(\theta(k))]$$

$$\hat{\theta}_i(k+1) = \hat{\theta}_i(k) - \beta \frac{2}{a} \sin(v_i(k)) J(\hat{\theta}(k) + a \sin(v(k)))$$

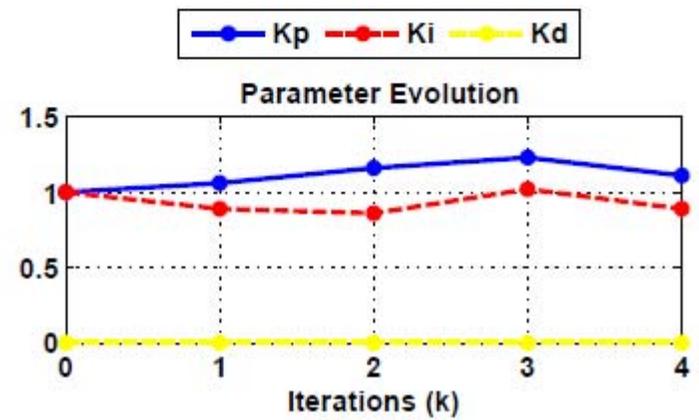
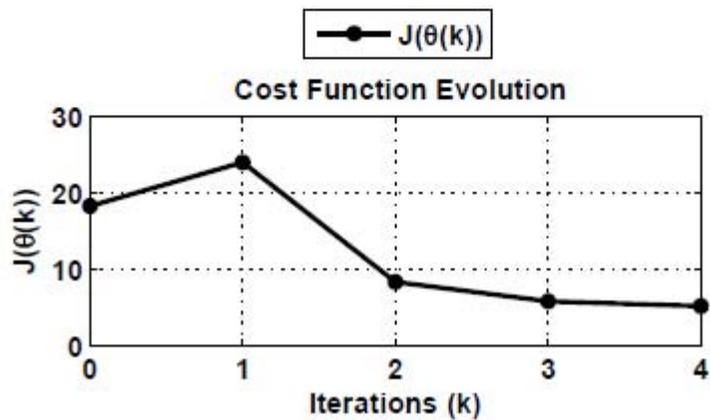


# EXPERIMENTAL RESULTS



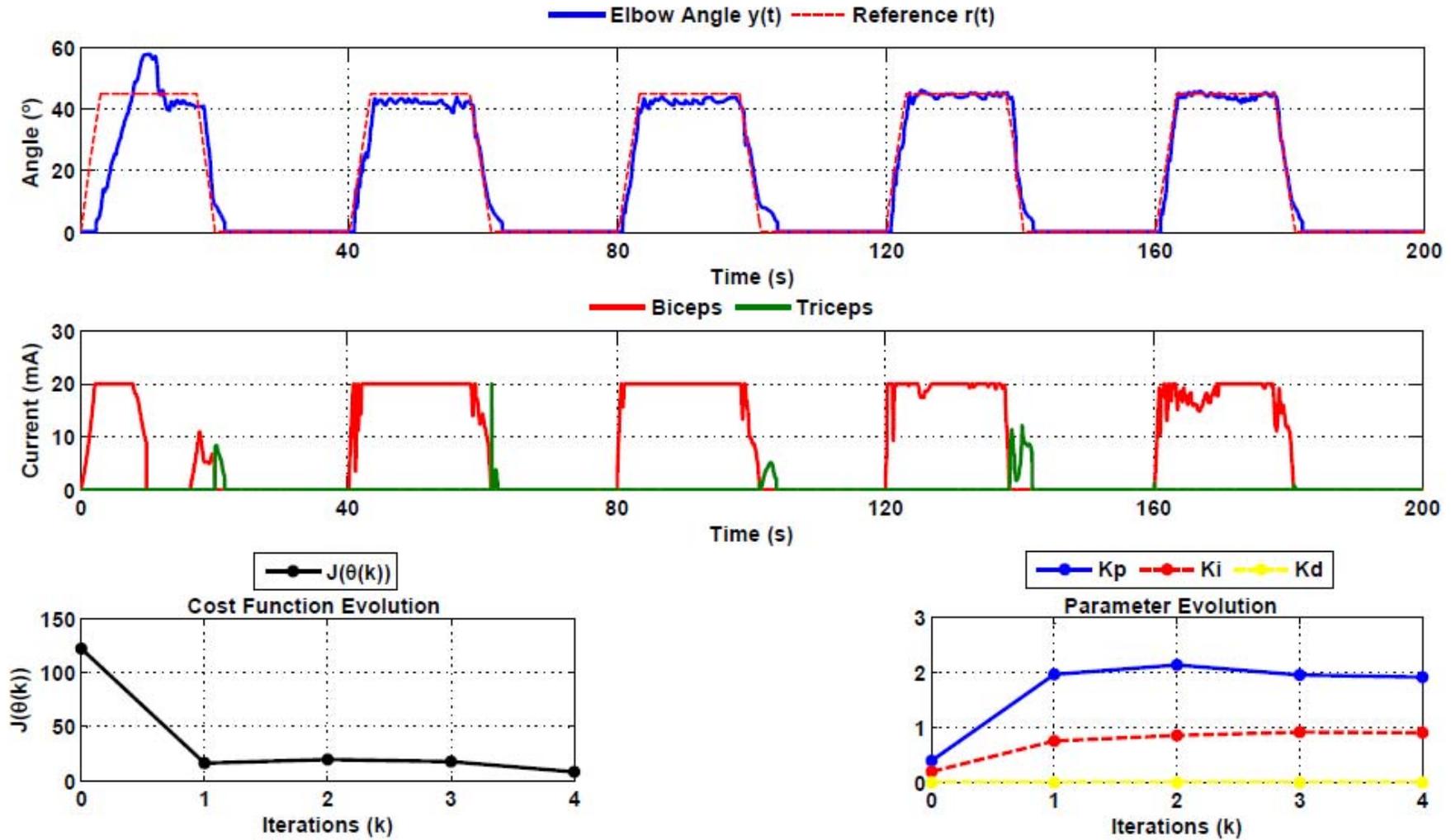
# EXPERIMENTAL RESULTS

## PATIENT 1



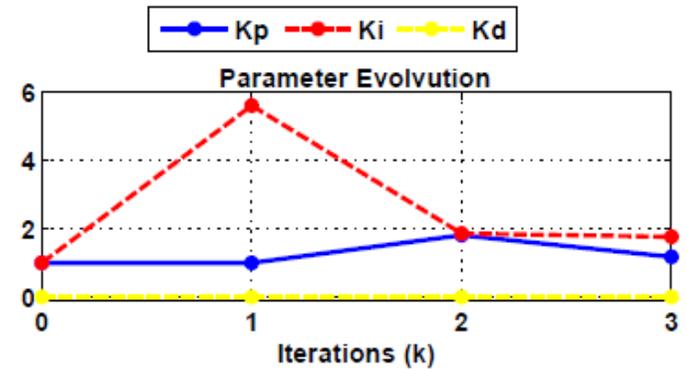
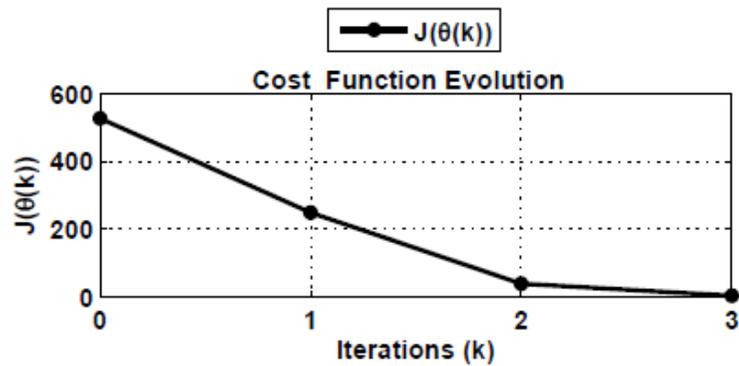
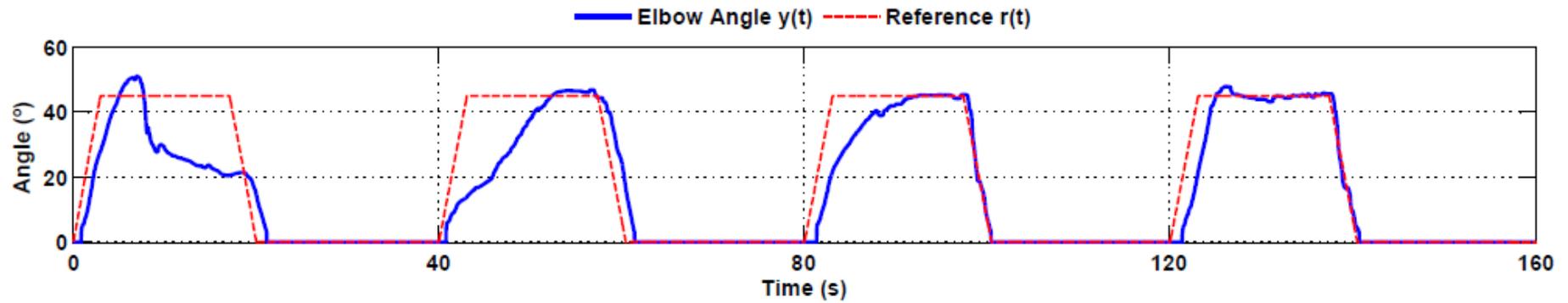
# EXPERIMENTAL RESULTS

## PATIENT 2



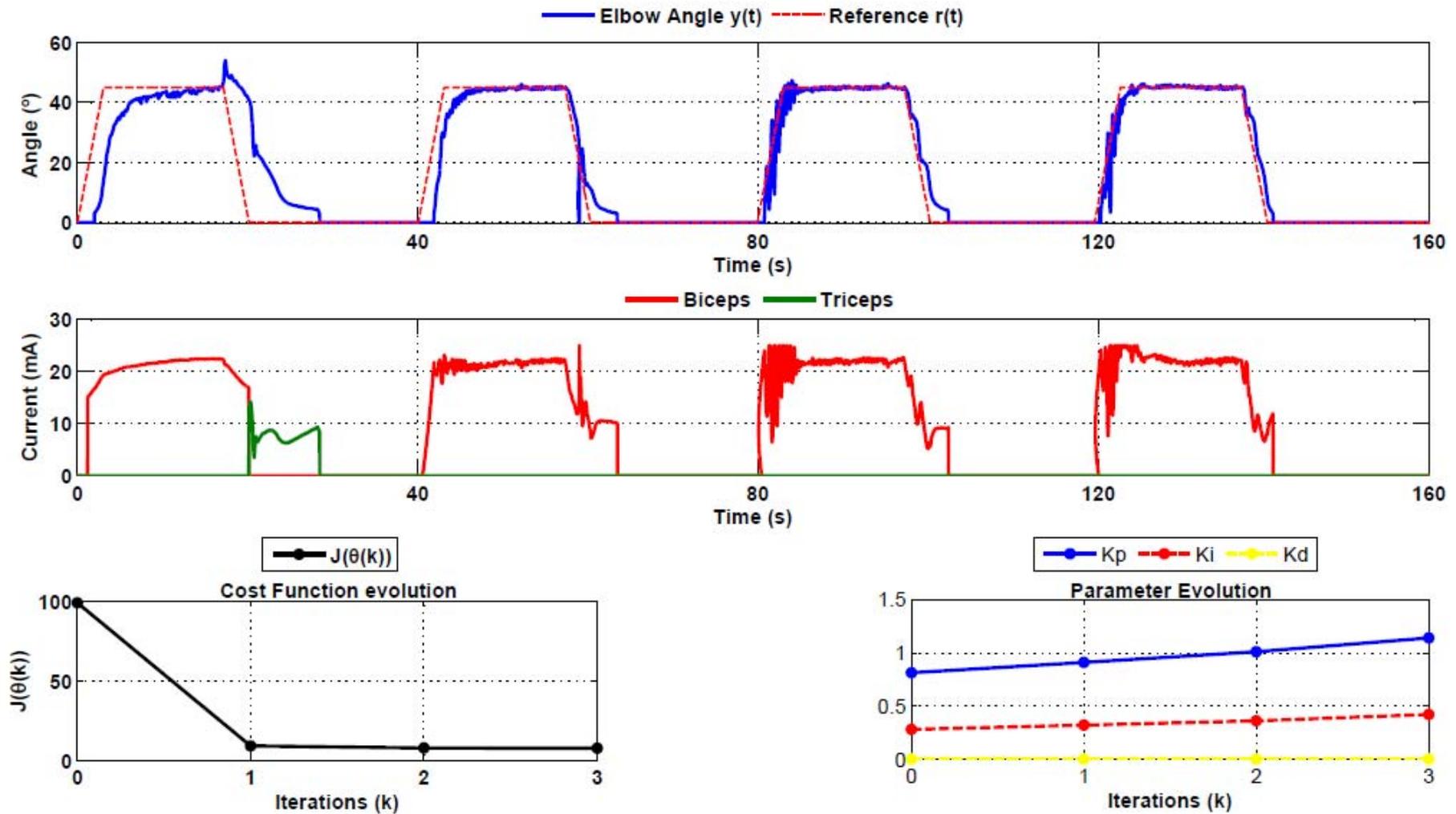
# EXPERIMENTAL RESULTS

## PATIENT 3



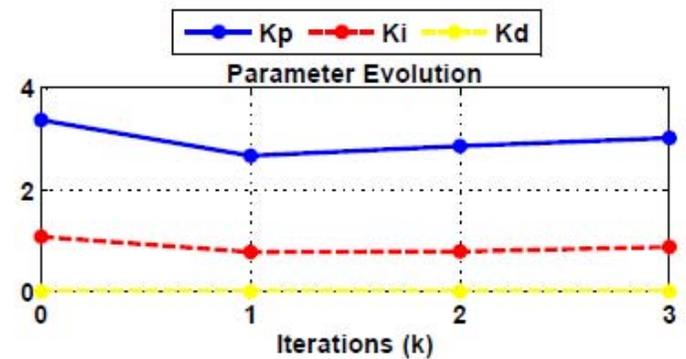
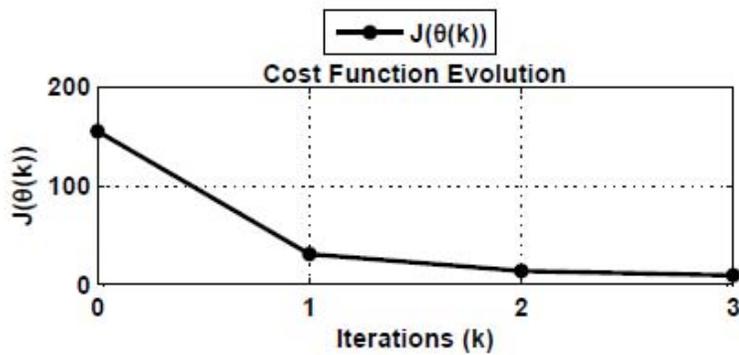
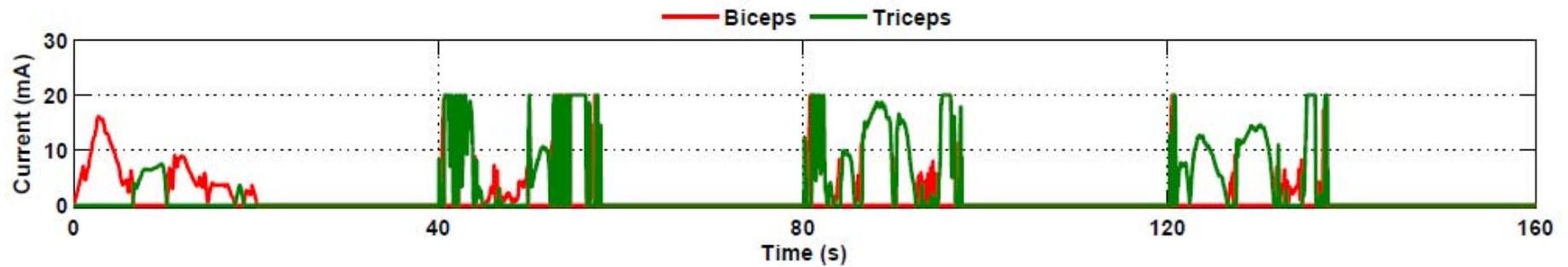
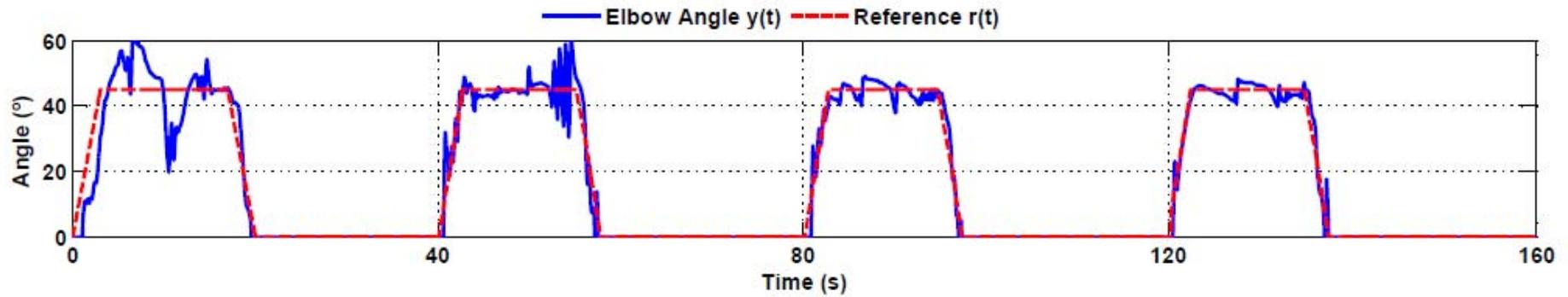
# EXPERIMENTAL RESULTS

## PATIENT 4



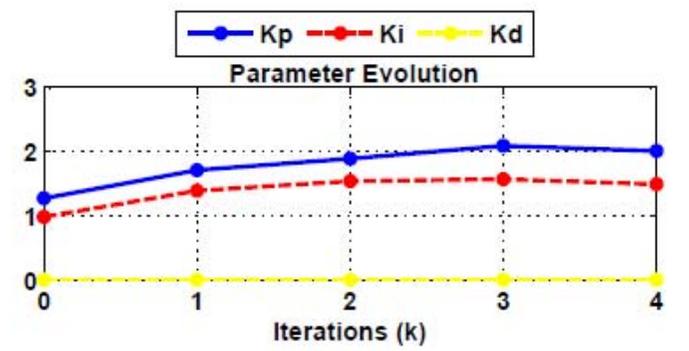
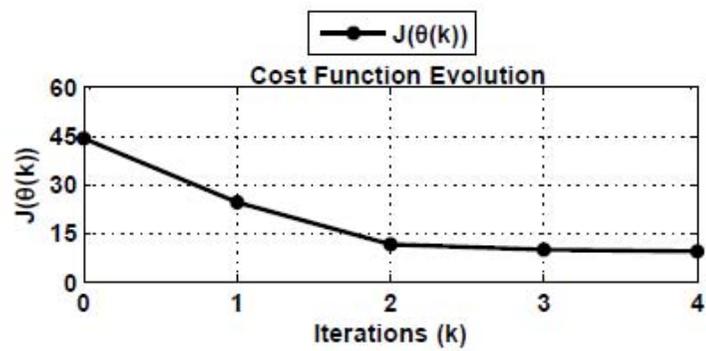
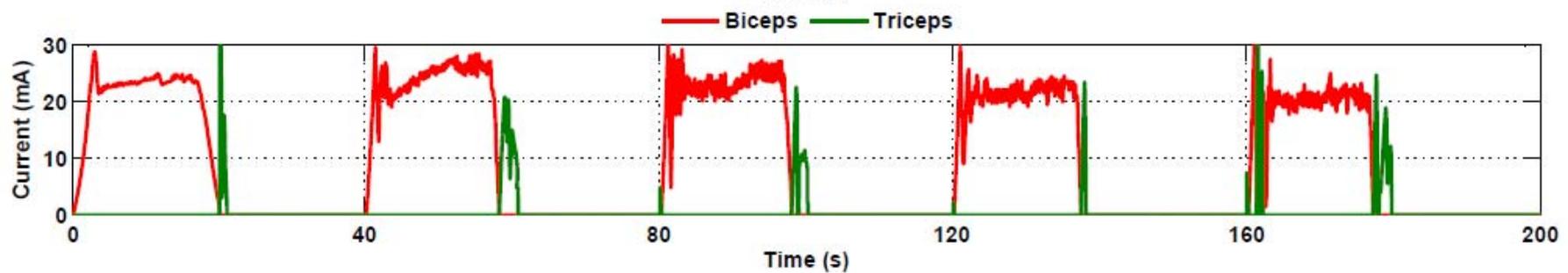
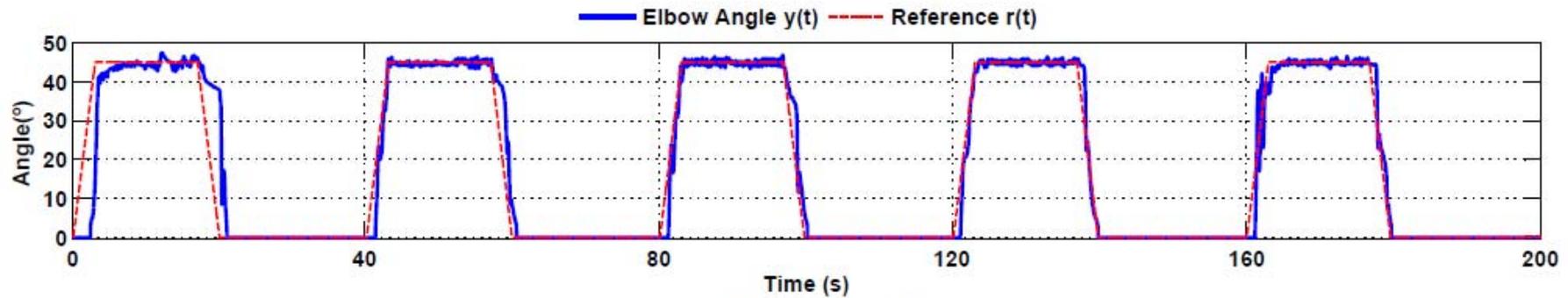
# EXPERIMENTAL RESULTS

## HEALTHY VOLUNTEER 1



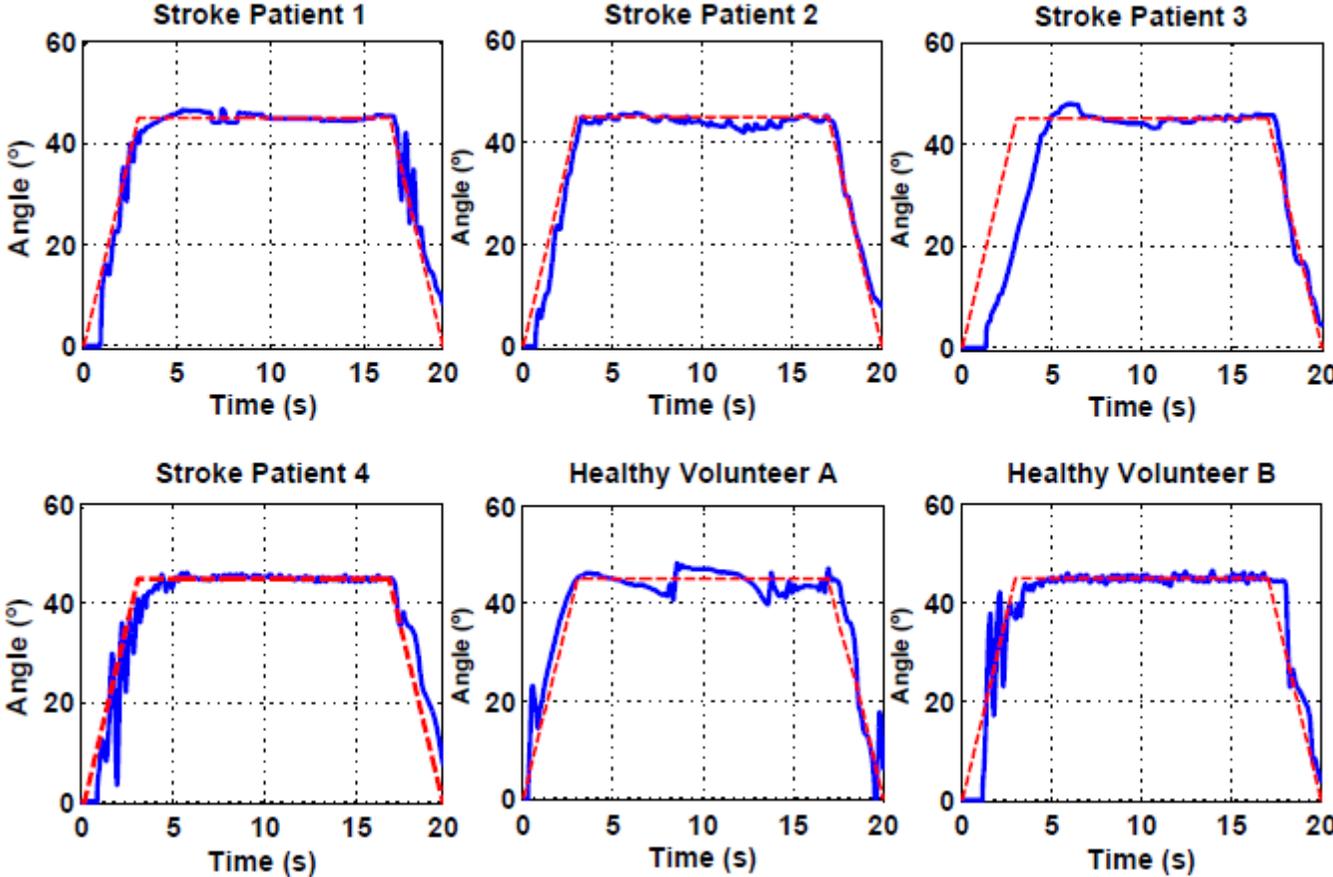
# EXPERIMENTAL RESULTS

## HEALTHY VOLUNTEER 2



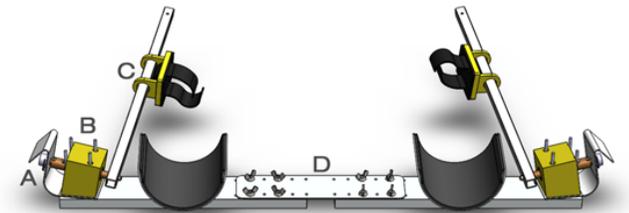
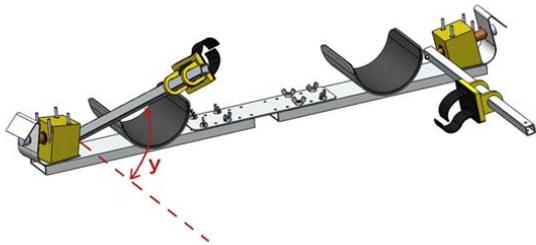
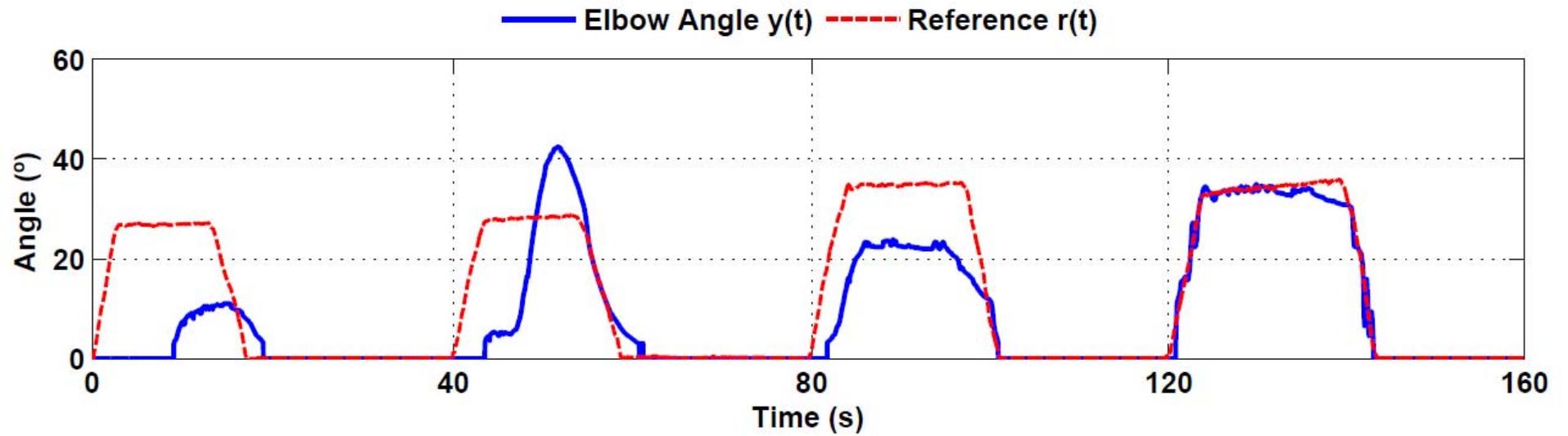
# EXPERIMENTAL RESULTS

## Best Response

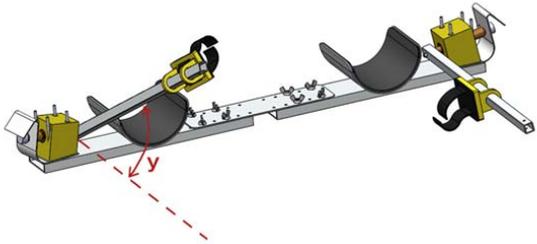
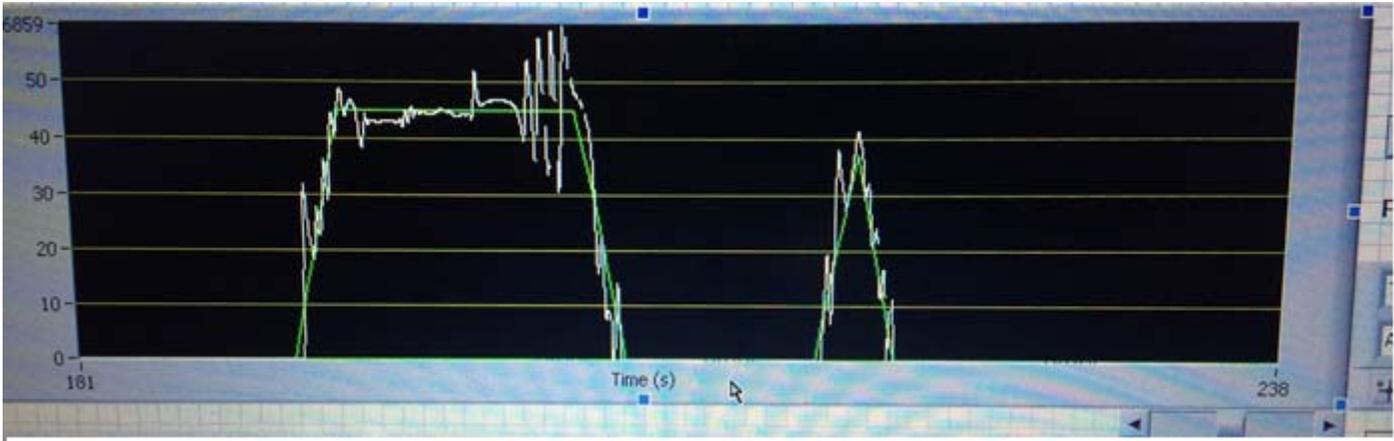


# CONTRALATERAL MOVEMENT

## PATIENT 5



# CONTRALATERAL MOVEMENT



# EXPERIMENTAL RESULTS OF 4 STROKE PATIENTS

CLINICAL DESCRIPTION OF THE STROKE PATIENTS AND BASIC INFORMATION OF THE HEALTHY VOLUNTEERS

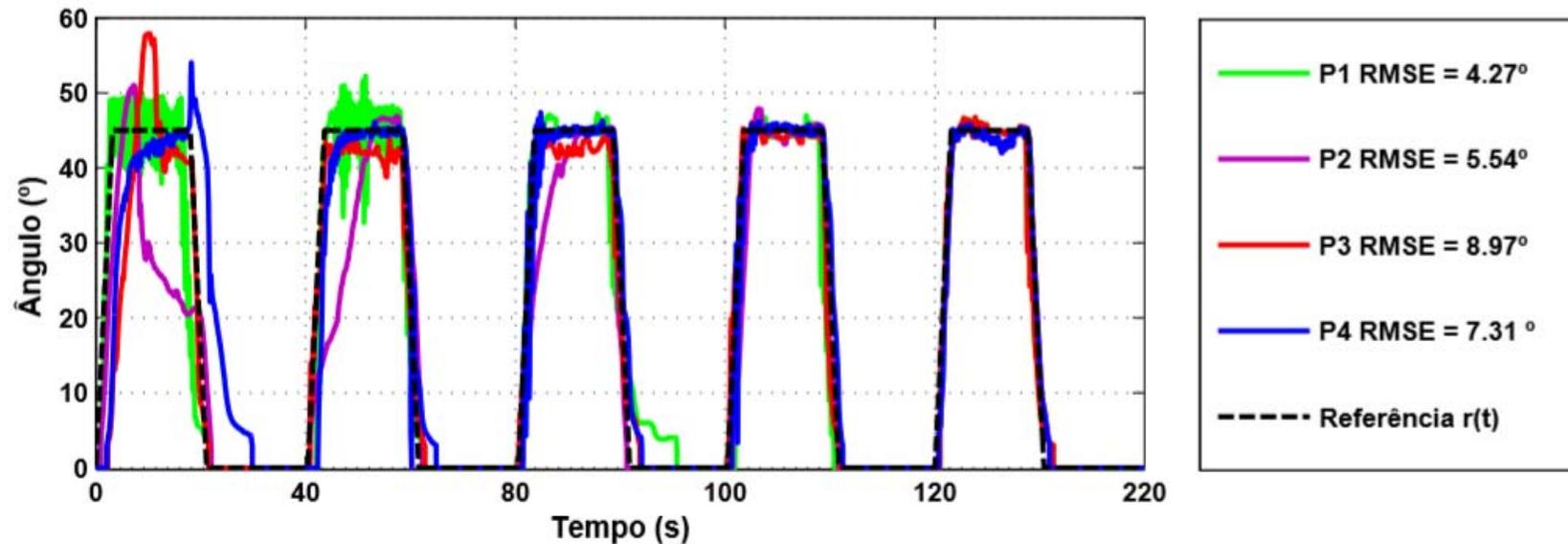
Subject	Age	Gender	Lesion Time (months)	Lesion Side	Stroke Type	MAS Scale <sup>1</sup>	Rankin Scale <sup>2</sup>	FMA-MS <sup>3</sup>
P1	40	M	121	L	H	3	III	14/66
P2	53	M	134	R	I	1+	I	26/66
P3	28	F	69	R	I	2	I	36/66
P4	59	F	162	L	H	2	III	9/66
P5	35	M	18	R	I	1+	I	18/66
VA	33	F	-	-	-	-	-	-
VB	31	M	-	-	-	-	-	-

M - Male, F- Female, R - Right, L - Left, I - Ischemic Stroke, H - Hemorrhagic Stroke

1 - Modified Ashworth Scale

2 - Stroke Severity Scale

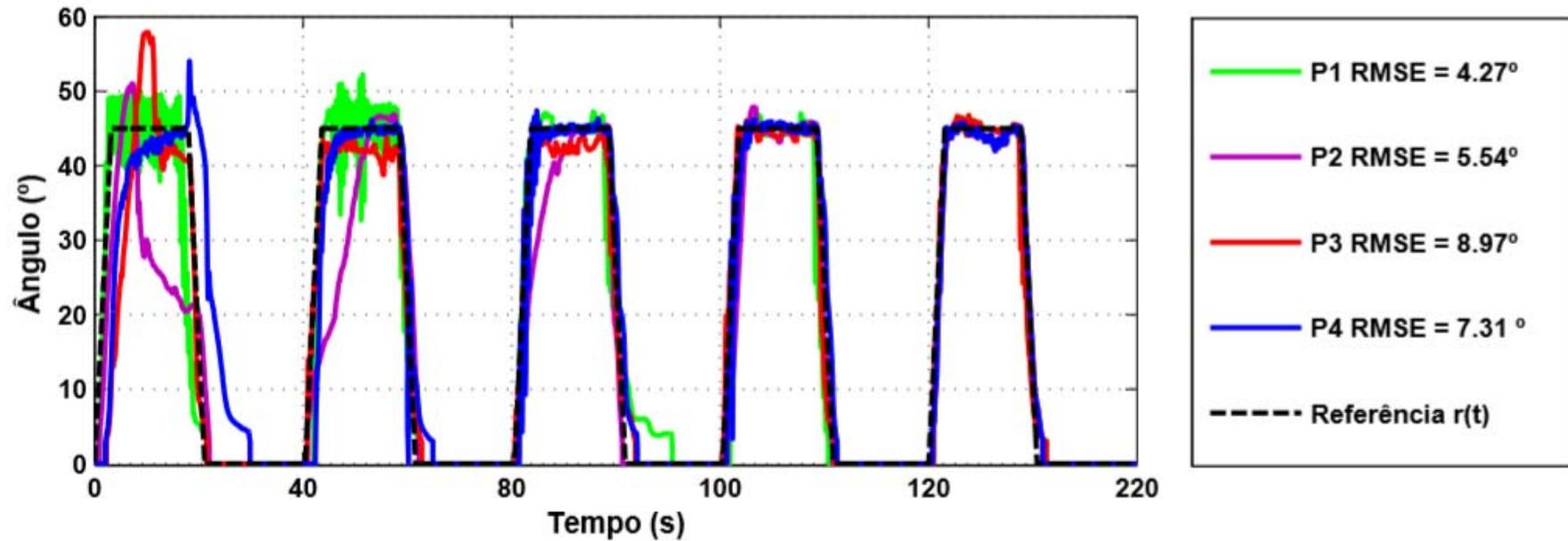
3 - Upper Limb Fugl-Meyer Assessment Scale



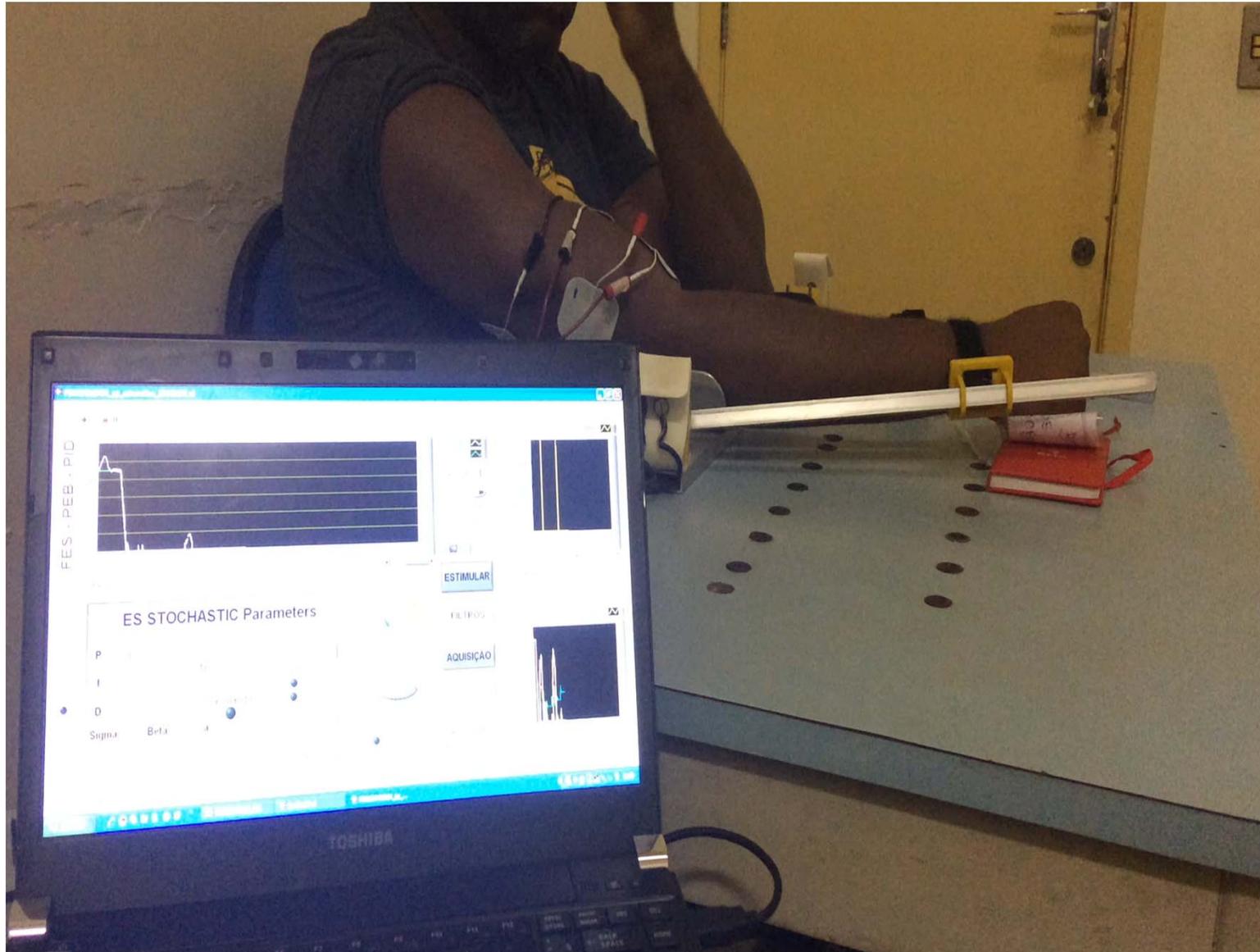
# EXPERIMENTAL RESULTS OF 4 STROKE PATIENTS

ROOT-MEAN-SQUARE ERROR (RMSE) OBTAINED FOR STROKE PATIENTS AND HEALTHY VOLUNTEERS

	Patient 1	Patient 2	Patient 3	Patient 4	Patient 5	Volunteer A	Volunteer B	Mean
Total RMSE	4.27°	5.54°	8.97°	7.31°	4.91°	4.02°	5.13°	5.73°
RMSE of First Cycle	3.62°	10.88°	10.98°	12.61°	8.94°	6.68°	9.49°	9.02°
RMSE of Last Cycle	2.51°	2.26°	5.72°	3.17°	5.22°	2.04°	2.94°	3.40°



# REAL EXPERIMENT WITH STROKE PATIENT



## CONCLUSION

- ✓ Stochastic Extremum Seeking-based PID is a self-tuning, fatigue resistant control method for NMES-based therapies.
- ✓ In spite of the nonlinearities and time-varying properties of the NMES process, it was satisfactorily approached by the proposed adaptive PID controller via stochastic ES.
- ✓ Good tracking performance can be achieved after reduced number of the algorithm iterations.
- ✓ According to our experiments, the proposed adaptive control approach had presented good performance results to reach the target angle.

# TALKS AND PUBLICATIONS



# TALKS AND PUBLICATIONS

## Congresso Brasileiro de Automática

### CBA2018

XXII Congresso Brasileiro de Automática

João Pessoa - PB, Brasil: 9/9/2018 to 12/9/2018

Conference Proceedings ISSN: 2525-8311

### BUSCA EXTREMAL ESTOCÁSTICA APLICADA À ESTIMULAÇÃO ELÉTRICA NEUROMUSCULAR EM PACIENTES COM AVC

Paulo Roberto Souza da Paz<sup>1</sup>; Tiago Roux Oliveira<sup>1</sup>

<sup>1</sup>Universidade do Estado do Rio de Janeiro (UERJ)

doi:10.20906/CPS/CBA2018-0726

#### Abstract

A técnica de Busca Extremal Estocástica (Stochastic Extremum Seeking - ES) é aplicada para adaptar os ganhos de um controlador Proporcional-Integral-Derivativo (PID) na estimulação elétrica neuromuscular. O esquema proposto é aplicado no controle da posição do braço de pacientes com sequelas de Acidente Vascular Cerebral (AVC) para coordenar os movimentos de



# TALKS AND PUBLICATIONS



## Busca Extremal Estocástica Aplicada à Estimulação Elétrica Neuromuscular



Inaiacy Bittencourt Souto<sup>1</sup>; Ana Paula Fontana<sup>1</sup>; Thais Costa Amaral<sup>1</sup>; Tiago Roux Oliveira<sup>2</sup>; Paulo Paz<sup>1</sup>  
E-mail: [inaiaicy@gmail.com](mailto:inaiaicy@gmail.com); [fontanaap@gmail.com](mailto:fontanaap@gmail.com); [thaiscostaamaral@hotmail.com](mailto:thaiscostaamaral@hotmail.com); [tiagoroux@uerj.br](mailto:tiagoroux@uerj.br); [paulinho.paz@gmail.com](mailto:paulinho.paz@gmail.com)

<sup>1</sup> Faculdade de Medicina, Universidade Federal do Rio de Janeiro, Rio de Janeiro, Brasil

<sup>2</sup> Faculdade de Engenharia, Universidade do Estado do Rio de Janeiro, Rio de Janeiro, Brasil

### INTRODUÇÃO

A técnica de Busca Extremal Estocástica (*Stochastic Extremum Seeking - ES*) é aplicada para adaptar os ganhos de um controlador Proporcional-Integral-Derivativo (PID) na estimulação elétrica neuromuscular (NMES). O esquema proposto é aplicado no controle da posição do braço de pacientes com seqüelas de Acidente Vascular Cerebral (AVC) para coordenar os movimentos de flexão e extensão dos braços. Esta abordagem elimina os testes iniciais de sintonia e os parâmetros do controlador são automaticamente computados em tempo real. Os parâmetros PID são ajustados através de uma versão discreta multivariável do ES estocástico para minimizar uma função de custo que representa o desempenho dos requisitos desejados.



Figure 1 - Aparato mecnico para testes experimentais NMES.

### Busca Extremal Estocástica



# TALKS AND PUBLICATIONS

2018 IEEE Conference on Decision and Control (CDC)  
Miami Beach, FL, USA, Dec. 17-19, 2018

## Neuromuscular Electrical Stimulation for Stroke Patients by Deterministic Extremum Seeking

Paulo Paz<sup>1</sup> and Tiago Roux Oliveira<sup>1</sup>

**Abstract**— A multiparameter and deterministic extremum seeking (ES) algorithm is applied to tune Proportional-Integral-Derivative (PID) controllers for functional neuromuscular electrical stimulation (NMES). The proposed scheme controls the patient's arm such that the desired movements of flexion/extension for its elbow can be generated. The PID tuning using ES eliminates initial off-line tests with patients since the control gains are automatically computed in order to minimize a cost function according to the tracking error between the elbow's angle and the reference trajectory. Experiments with eight stroke patients show advances in terms of reduced root-mean-square error (RMSE) and improved ultimate responses when compared to the initial evaluation cycle.

### I. INTRODUCTION

Functional Electrical Stimulation (FES) or Neuromuscular

may be totally unproductive. The adverse environment of modeling inspires the application of adaptive-robust control methodologies and automatic tuning techniques [6].

The purpose of this paper is to develop an adaptive PID control scheme for NMES, aimed to upper limb unilateral exercises, by evaluating its operation with *stroke patients*. The proposed method for online tuning PID parameters using multivariable and deterministic Extremum Seeking (ES) [7] within a closed-loop setting is shown to be importantly fruitful. As discussed in our previous publication [9] with healthy volunteers, there are clear advantages in applying deterministic (periodic) excitation rather than more classical methods for PID tuning when dealing with nonlinear systems [8]. The proposed adaptive algorithm based on periodic



57th IEEE Conference on Decision and Control, Miami Beach, FL, USA, December 17-19, 2018

# TALKS AND PUBLICATIONS

This article has been accepted for inclusion in a future issue of this journal. Content is final as presented, with the exception of pagination.

IEEE TRANSACTIONS ON CONTROL SYSTEMS TECHNOLOGY

1

## Model-Free Neuromuscular Electrical Stimulation by Stochastic Extremum Seeking

Paulo Paz<sup>1</sup>, Tiago Roux Oliveira<sup>1</sup>, Alexandre Visintainer Pino, and Ana Paula Fontana

**Abstract**—Stochastic extremum seeking (ES) approach is employed to adapt the gains of a proportional—integral—derivative (PID) control law for functional neuromuscular electrical stimulation. The proposed scheme is applied to control the position of the arm of healthy volunteers and stroke patients so that coordinated movements of flexion/extension for their elbow can be performed. This approach eliminates the initial tuning tests with patients since the controller parameters are automatically computed in real time. The PID parameters are updated by means of a discrete version of multivariable stochastic ES in order to minimize a cost function which brings the desired performance requirements. Experimental results with healthy volunteers as

stroke patients) to perform movements that would not be able to be executed.

NMES can be separated into two segments: functional substitution and therapeutic intervention. For instance, stroke patients with drop foot [2] use NMES to activate the tibialis anterior muscle during swing phase. In this situation, NMES is used as a functional substitute of a damaged central nervous system which is not able to recruit the necessary muscles during the gait. Differently, patients making repetitive and voluntary training with their paretic arms are able to adapt

IEEE TRANSACTIONS ON CONTROL SYSTEMS TECHNOLOGY



# TALKS AND PUBLICATIONS



Anais da Academia Brasileira de Ciências (2019) 91(Suppl. 1) e20180544  
(Annals of the Brazilian Academy of Sciences)  
Printed version ISSN 0001-3765 / Online version ISSN 1678-2690  
<http://dx.doi.org/10.1590/0001-3765201820180544>  
[www.scielo.br/aabc](http://www.scielo.br/aabc) | [www.fb.com/aabcjournal](http://www.fb.com/aabcjournal)



## Extremum Seeking-based Adaptive PID Control applied to Neuromuscular Electrical Stimulation

TIAGO ROUX-OLIVEIRA<sup>1</sup>, LUIZ R. COSTA<sup>2</sup>, ALEXANDRE V. PINO<sup>2</sup> and PAULO PAZ<sup>1</sup>

<sup>1</sup>Dept. of Electronics and Telecommunication Engineering, State University of Rio de Janeiro (UERJ),  
Rua São Francisco Xavier, 524, sala 5018E, Maracanã, 20550-900 Rio de Janeiro, RJ, Brazil

<sup>2</sup>Biomedical Engineering Program, Federal University of Rio de Janeiro (COPPE/UFRJ),  
P.O. Box 68510, Ilha do Fundão, 21945-970 Rio de Janeiro, RJ, Brazil

*Manuscript received on May 30, 2018; accepted for publication on August 13, 2018*



# Thank You !

## Questions & Comments

Contact: [tiagoroux@uerj.br](mailto:tiagoroux@uerj.br)

Supported by:

